

# Sequence Labeling

- Inputs:  $x = (x_1, \dots, x_n)$
- Labels:  $y = (y_1, \dots, y_n)$
- Typical goal: Given  $x$ , predict  $y$
  
- Example sequence labeling tasks
  - Part-of-speech tagging
  - Named-entity-recognition (NER)
    - Label people, places, organizations

# NER Example:

## Red Sox and Their Fans Let Loose



Elise Amendola/Associated Press

Fans of the slugger David Ortiz in Boston's Copley Square.

By [PETE THAMEL](#)

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[BOSTON](#), Oct. 30 — [Jonathan Papelbon](#) turned Boston's World Series victory parade into a full-scale dance party Tuesday as the [Red Sox](#) put an exclamation point on the 2007 season.

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# First Solution:

## Maximum Entropy Classifier

- Conditional model  $p(y|x)$ .
  - Do not waste effort modeling  $p(x)$ , since  $x$  is given at test time anyway.
  - Allows more complicated input features, since we do not need to model dependencies between them.
- Feature functions  $f(x,y)$ :
  - $f_1(x,y) = \{ \text{word is Boston} \ \& \ y=\text{Location} \}$
  - $f_2(x,y) = \{ \text{first letter capitalized} \ \& \ y=\text{Name} \}$
  - $f_3(x,y) = \{ x \text{ is an HTML link} \ \& \ y=\text{Location} \}$

# First Solution: MaxEnt Classifier

- How should we choose a classifier?
- Principle of maximum entropy
  - We want a classifier that:
    - Matches feature constraints from training data.
    - Predictions maximize entropy.
- There is a unique, exponential family distribution that meets these criteria.

# First Solution: MaxEnt Classifier

- $p(y|x;\theta)$ , inference, learning, and gradient.
- (ON BOARD)

# First Solution: MaxEnt Classifier

- Problem with using a maximum entropy classifier for sequence labeling:
- It makes decisions at each position independently!

# Second Solution: HMM

$$P(\mathbf{y}, \mathbf{x}) = \prod_t P(y_t | y_{t-1}) P(x | y_t)$$

- Defines a generative process.
- Can be viewed as a weighted finite state machine.

# Second Solution: HMM

- HMM problems: (ON BOARD)
  - Probability of an input sequence.
  - Most likely label sequence given an input sequence.
  - Learning with known label sequences.
  - Learning with unknown label sequences?



# Second Solution: HMM

- How can represent we multiple features in an HMM?
  - Treat them as conditionally independent given the class label?
    - The example features we talked about are not independent.
  - Try to model a more complex generative process of the input features?
    - We may lose tractability (i.e. lose a dynamic programming for exact inference).

# Second Solution: HMM

- Let's use a conditional model instead.

# Third Solution: MEMM

- Use a series of maximum entropy classifiers that know the previous label.
- Define a Viterbi algorithm for inference.

$$P(\mathbf{y} \mid \mathbf{x}) = \prod_t P_{y_{t-1}}(y_t \mid \mathbf{x})$$

# Third Solution: MEMM

- Finding the most likely label sequence given an input sequence and learning.
- (ON BOARD)

# Third Solution: MEMM

- Combines the advantages of maximum entropy and HMM!
- But there is a problem...

# Problem with MEMMs: Label Bias

- In some state space configurations, MEMMs essentially completely ignore the inputs.
- Example (ON BOARD).
- This is not a problem for HMMs, because the input sequence is generated by the model.

# Fourth Solution: Conditional Random Field

- Conditionally-trained, undirected graphical model.
- For a standard linear-chain structure:

$$P(\mathbf{y} \mid \mathbf{x}) = \prod_t \Psi_k(y_t, y_{t-1}, \mathbf{x})$$

$$\Psi_k(y_t, y_{t-1}, \mathbf{x}) = \exp\left(\sum_k \lambda_k f(y_t, y_{t-1}, \mathbf{x})\right)$$

# Fourth Solution: CRF

- Finding the most likely label sequence given an input sequence and learning.  
(ON BOARD)



# Fourth Solution: CRF

- Have the advantages of MEMMs, but avoid the label bias problem.
- CRFs are globally normalized, whereas MEMMs are locally normalized.
- Widely used and applied. CRFs give state-the-art results in many domains.

# Example Applications

- CRFs have been applied to:
  - Part-of-speech tagging
  - Named-entity-recognition
  - Table extraction
  - Gene prediction
  - Chinese word segmentation
  - Extracting information from research papers.
  - Many more...