

# Context-Free Parsing: Outside Probabilities, Earley's Algorithm, and Treebank Transformations

Introduction to Natural Language Processing  
Computer Science 585—Fall 2009  
University of Massachusetts Amherst

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# Announcements

- If you haven't gotten your HW #1, please let me know
- HW #2: think of part 2 as tagging when you don't know what the tags mean; please do email source code
- Jason's request: please hand in printout of non-source-code if you want comments
- I'd like to postpone the midterm till next Thursday

# Overview

- Complete inside-outside: outside computations
- Earley's algorithm: combining bottom-up and top-down parsing
- Better treebank grammars: annotating nonterminals

# Inside & Viterbi Algorithms

NB: index *between* words;  
M&S index words

**Let**  $\beta_A(i, j) = p(\text{constit}(A, i, j))$   
 $= p(w_{ij} \mid \text{nonterminal } A \text{ from } i \text{ to } j)$

$$\beta_A(i, k) = \sum_{B, C, j} \beta_B(i, j) \cdot \beta_C(j, k) \cdot p(A \rightarrow B C)$$

**Let**  $\delta_A(i, j) = p_{best}(\text{constit}(A, i, j))$

$$\delta_A(i, k) = \max_{B, C, j} \delta_B(i, j) \cdot \delta_C(j, k) \cdot p(A \rightarrow B C)$$

$$\beta_S(0, n) = ?$$

$$\delta_S(0, n) = ?$$

# Inside & Outside

$\text{constit}(A, i, j)$

$p(\text{words } 0-i, \text{ words } j-n, \text{ constit})$

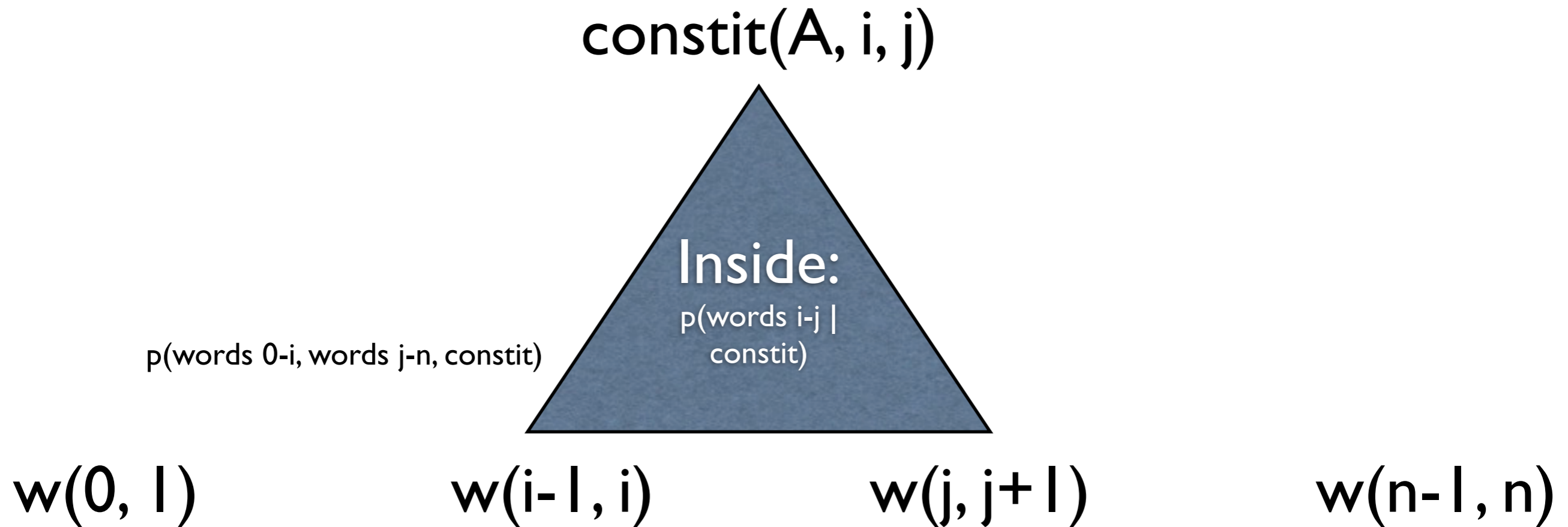
$w(0, 1)$

$w(i-1, i)$

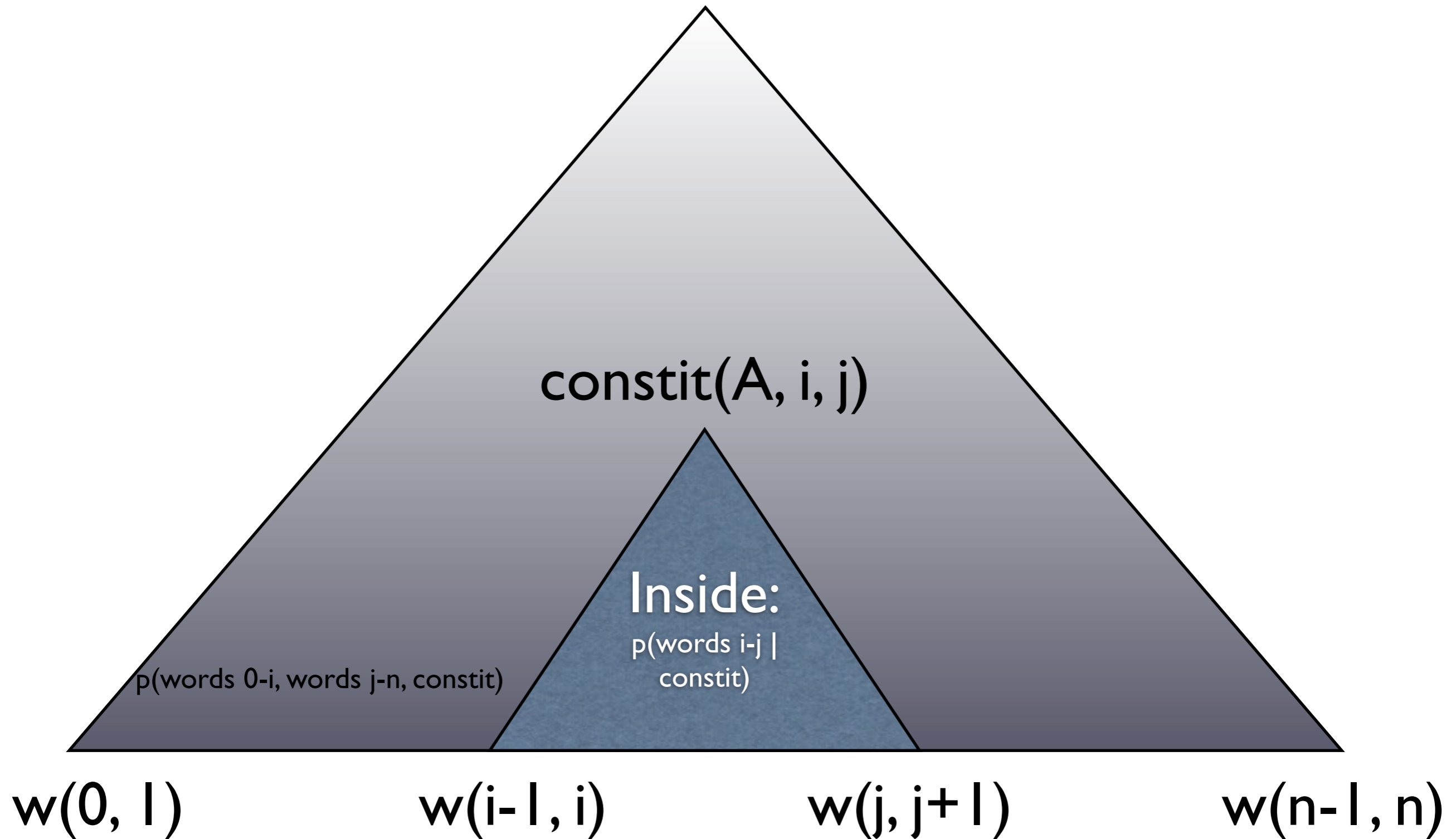
$w(j, j+1)$

$w(n-1, n)$

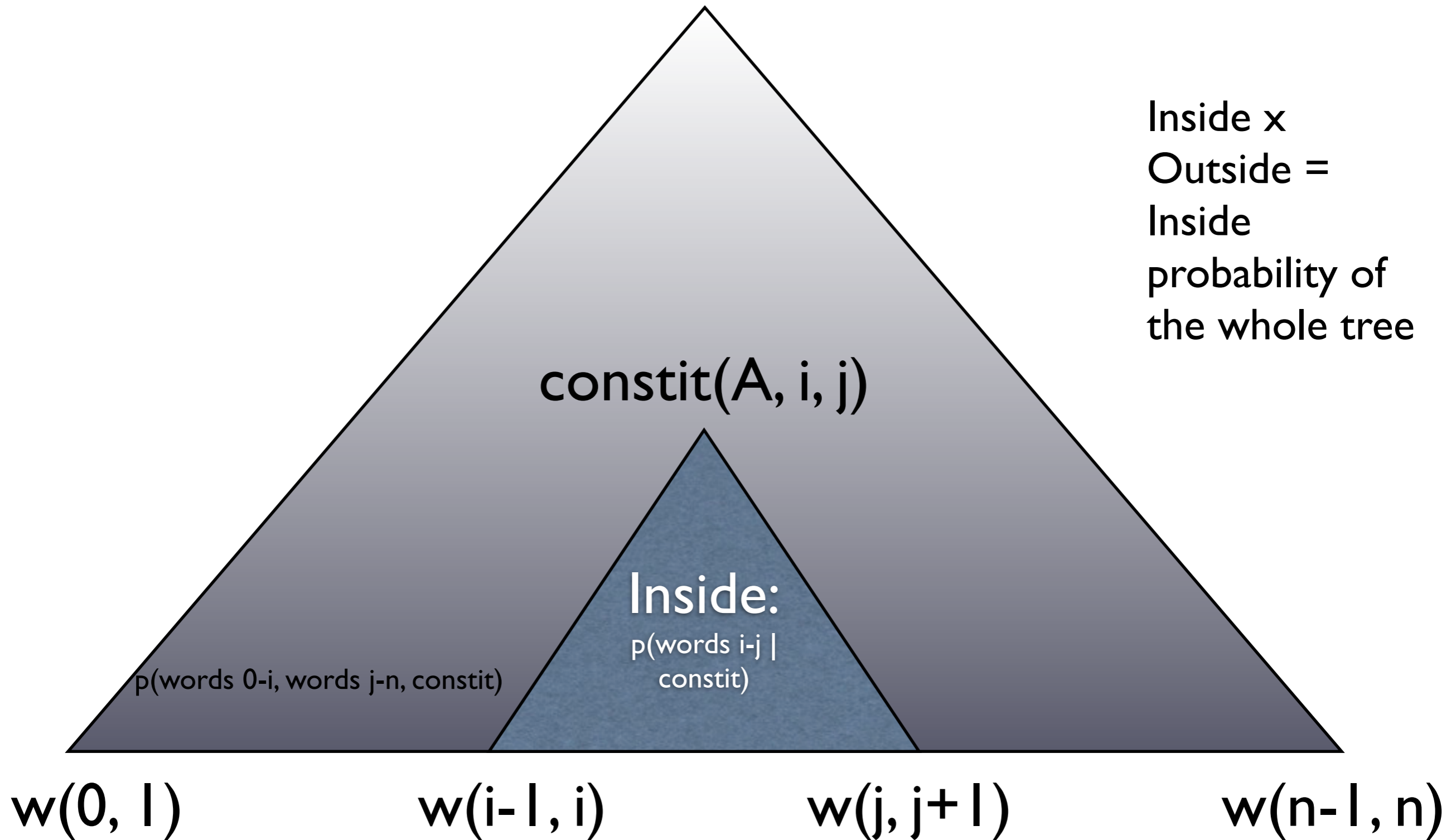
# Inside & Outside



# Inside & Outside



# Inside & Outside





# Outside Algorithm

$$\alpha_A(i, j) = p(w_{0,i}, A_{i,j}, w_{j,n})$$

Uses inside  
probs.

$$\alpha_A(i, j) = \sum_{B, C, k=j}^n \alpha_B(i, k) \cdot \beta_C(j, k) \cdot p(B \rightarrow A C) \\ + \sum_{B, C, k=0}^i \alpha_B(k, j) \cdot \beta_C(k, i) \cdot p(B \rightarrow C A)$$

$$\alpha_S(0, n) = ?$$

$$\alpha_{PP}(0, n) = ?$$

Some  
resemblance  
to derivative  
product rule

# Top-Down/Bottom-Up

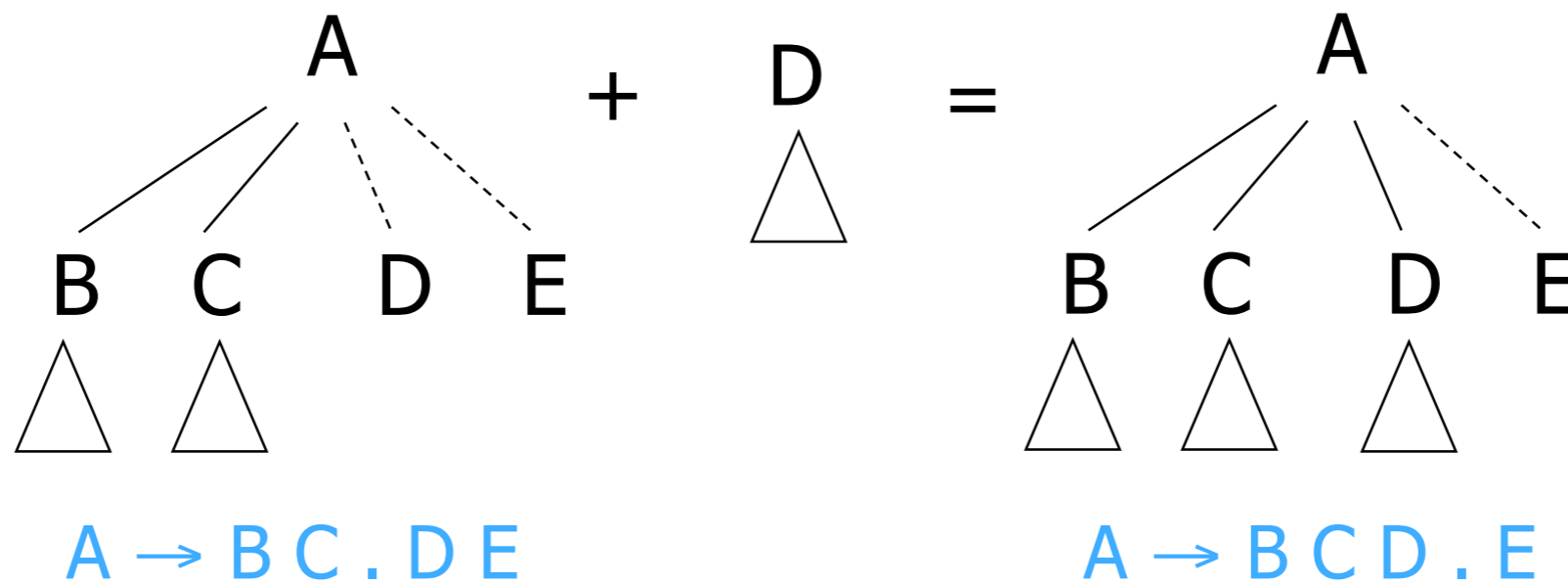
- Top-down parsers
  - Can get caught in infinite loops
  - Take exponential time backtracking
- CKY
  - Needs Chomsky normal form
  - Builds all possible constituents

## Earley Parser (1970)

- Nice combination of
  - dynamic programming
  - incremental interpretation
  - avoids infinite loops
  - no restrictions on the form of the context-free grammar.  
 **$A \rightarrow B C \textit{ the D of}$**  causes no problems
  - $O(n^3)$  worst case, but faster for many grammars
  - Uses left context and optionally right context to constrain search.

# Overview of the Algorithm

- Finds constituents and partial constituents in input
  - $A \rightarrow B C . D E$  is partial: only the first half of the  $A$



# Overview of the Algorithm

- Proceeds incrementally left-to-right
  - Before it reads word 5, it has already built all hypotheses that are consistent with first 4 words
  - Reads word 5 & attaches it to immediately preceding hypotheses. Might yield new constituents that are then attached to hypotheses immediately preceding *them* ...
  - E.g., attaching **D** to  $A \rightarrow B C . D E$  gives  $A \rightarrow B C D . E$
  - Attaching **E** to that gives  $A \rightarrow B C D E .$
  - Now we have a complete **A** that we can attach to hypotheses immediately preceding the **A**, etc.

# The Parse Table

- Columns 0 through n corresponding to the gaps between words
- Entries in column 5 look like (3, NP → NP . PP)
  - (but we'll omit the → etc. to save space)
  - Built while processing word 5
  - Means that the input substring from 3 to 5 matches the initial NP portion of a NP → NP PP rule
  - Dot shows how much we've matched as of column 5
  - Perfectly fine to have entries like (3, VP → is it . true that S)

# The Parse Table

- Entries in column 5 look like (3, NP → NP . PP)
- What will it mean that we have this entry?
  - *Unknown right context: Doesn't* mean we'll necessarily be able to find a VP starting at column 5 to complete the S.
  - *Known left context: Does* mean that some dotted rule back in column 3 is looking for an S that starts at 3.
    - So if we actually do find a VP starting at column 5, allowing us to complete the S, then we'll be able to attach the S to something.
    - And when that something is complete, it too will have a customer to *its* left ...
    - In short, a top-down (i.e., goal-directed) parser: it chooses to start building a constituent not because of the input but because that's what the left context needs. In **the spoon**, won't build **spoon** as a verb because there's no way to use a verb there.
    - So any hypothesis in column 5 *could* get used in the correct parse, if words 1-5 are continued in just the right way by words 6-n.

# Earley's Algorithm, recognizer version

- Add **ROOT**  $\rightarrow$  **. S** to column 0.
- For each  $j$  from 0 to  $n$ :
  - For each dotted rule in column  $j$ , (including those we add as we go!) look at what's after the dot:
    - If it's a word  $w$ , SCAN:
      - If  $w$  matches the input word between  $j$  and  $j+1$ , advance the dot and add the resulting rule to column  $j+1$
    - If it's a non-terminal  $X$ , PREDICT:
      - Add all rules for  $X$  to the bottom of column  $j$ , with the dot at the start: e.g. **X**  $\rightarrow$  **. Y Z**
    - If there's nothing after the dot, ATTACH:
      - We've finished some constituent,  $A$ , that started in column  $l < j$ . So for each rule in column  $j$  that has  $A$  after the dot: Advance the dot and add the result to the bottom of column  $j$ .
- Output “yes” just if last column has **ROOT**  $\rightarrow$  **S .**
- **NOTE: Don't add an entry to a column if it's already there!**



## Summary of the Algorithm

- Process all hypotheses one at a time in order. (Current hypothesis is shown in blue.)
- This may add **new hypotheses** to the end of the to-do list, or try to add **old hypotheses** again.
- Process a hypothesis according to what follows the dot:
  - If a word, **scan** input and see if it matches
  - If a nonterminal, **predict** ways to match it
    - (we'll predict blindly, but could reduce # of predictions by *looking ahead* k symbols in the input and only making predictions that are compatible with this limited *right context*)
  - If nothing, then we have a complete constituent, so **attach** it to all its customers

## A Grammar

$S \rightarrow NP VP$

$NP \rightarrow Det N$

$NP \rightarrow NP PP$

$VP \rightarrow V NP$

$VP \rightarrow VP PP$

$PP \rightarrow P NP$

$NP \rightarrow Papa$

$N \rightarrow caviar$

$N \rightarrow spoon$

$V \rightarrow ate$

$P \rightarrow with$

$Det \rightarrow the$

$Det \rightarrow a$

## An Input Sentence

*Papa ate the caviar with a spoon.*

0
0 ROOT . S

**initialize**



*Remember this stands for (0, ROOT → . S)*

0
0 ROOT . S
0 S . NP VP

**predict** the kind of S we are looking for



*Remember this stands for (0, S → . NP VP)*

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa

**predict** the kind of NP we are looking for  
*(actually we'll look for 3 kinds: any of the 3 will do)*

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa
0 Det . the
0 Det . a

**predict** the kind of Det we are looking for (*2 kinds*)

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa
0 Det . the
0 Det . a

**predict** the kind of NP we're looking for  
*but we were already looking for these so  
 don't add duplicate goals! Note that this happened  
 when we were processing a left-recursive rule.*

0	Papa	1
0 ROOT . S	0 NP Papa .	
0 S . NP VP		
0 NP . Det N		
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a		

**scan:** the desired word is in the input!



0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		
0 NP . Det N		
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a		

scan: failure

0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		
0 NP . Det N		
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a		

**scan: failure**

0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		0 S NP . VP
0 NP . Det N		0 NP NP . PP
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a		

**attach** the newly created NP  
 (which starts at 0) to its **customers**  
 (incomplete constituents that *end* at 0  
 and have NP after the dot)

0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		0 S NP . VP
0 NP . Det N		0 NP NP . PP
0 NP . NP PP		1 VP . V NP
0 NP . Papa		1 VP . VP PP
0 Det . the		
0 Det . a		

predict

0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		0 S NP . VP
0 NP . Det N		0 NP NP . PP
0 NP . NP PP		1 VP . V NP
0 NP . Papa		1 VP . VP PP
0 Det . the		1 PP . P NP
0 Det . a		

predict

0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		0 S NP . VP
0 NP . Det N		0 NP NP . PP
0 NP . NP PP		1 VP . V NP
0 NP . Papa		1 VP . VP PP
0 Det . the		1 PP . P NP
0 Det . a		1 V . ate

predict

0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		0 S NP . VP
0 NP . Det N		0 NP NP . PP
0 NP . NP PP		1 VP . V NP
0 NP . Papa		1 VP . VP PP
0 Det . the		1 PP . P NP
0 Det . a		1 V . ate

predict

0	Papa	1
0 ROOT . S		0 NP Papa .
0 S . NP VP		0 S NP . VP
0 NP . Det N		0 NP NP . PP
0 NP . NP PP		1 VP . V NP
0 NP . Papa		1 VP . VP PP
0 Det . the		1 PP . P NP
0 Det . a		1 V . ate
		1 P . with

predict



0	Papa	1	ate	2
0 ROOT . S	0 NP Papa .	1 V ate .		
0 S . NP VP	0 S NP . VP			
0 NP . Det N	0 NP NP . PP			
0 NP . NP PP	1 VP . V NP			
0 NP . Papa	1 VP . VP PP			
0 Det . the	1 PP . P NP			
0 Det . a	1 V . ate	scan: success!		
	1 P . with			

0	Papa	1	ate	2
0 ROOT . S	0 NP Papa .	1 V ate .		
0 S . NP VP	0 S NP . VP			
0 NP . Det N	0 NP NP . PP			
0 NP . NP PP	1 VP . V NP			
0 NP . Papa	1 VP . VP PP			
0 Det . the	1 PP . P NP			
0 Det . a	1 V . ate			
	1 P . with	scan: failure		

0	Papa	1	ate	2
0 ROOT . S	0 NP Papa .		1 V ate .	
0 S . NP VP	0 S NP . VP		1 VP V . NP	
0 NP . Det N	0 NP NP . PP			
0 NP . NP PP	1 VP . V NP			
0 NP . Papa	1 VP . VP PP			
0 Det . the	1 PP . P NP			
0 Det . a	1 V . ate			
	1 P . with			

attach

0	Papa	1	ate	2
0 ROOT . S	0 NP Papa .	1 V ate .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP			
0 Det . a	1 V . ate			
	1 P . with			

predict

0	Papa	1	ate	2
0 ROOT . S	0 NP Papa .	1 V ate .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

**predict** (these next few steps should look familiar)

0	Papa	1	ate	2
0 ROOT . S	0 NP Papa .	1 V ate .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

predict

0	Papa	1	ate	2
0 ROOT . S	0 NP Papa .	1 V ate .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

**scan** (*this time we fail since Papa is not the next word*)

0	Papa	1	ate	2	the	3
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .			
0 S . NP VP	0 S NP . VP	1 VP V . NP				
0 NP . Det N	0 NP NP . PP	2 NP . Det N				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa				
0 Det . the	1 PP . P NP	2 Det . the				scan: success!
0 Det . a	1 V . ate	2 Det . a				
	1 P . with					



0	Papa	1	ate	2	the	3
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .			
0 S . NP VP	0 S NP . VP	1 VP V . NP				
0 NP . Det N	0 NP NP . PP	2 NP . Det N				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa				
0 Det . the	1 PP . P NP	2 Det . the				
0 Det . a	1 V . ate	2 Det . a				
	1 P . with					

0	Papa	1	ate	2	the	3
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		
0 NP . Det N	0 NP NP . PP	2 NP . Det N				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa				
0 Det . the	1 PP . P NP	2 Det . the				
0 Det . a	1 V . ate	2 Det . a				
	1 P . with					

0	Papa	1	ate	2	the	3
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .			
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N			
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar			
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon			
0 NP . Papa	1 VP . VP PP	2 NP . Papa				
0 Det . the	1 PP . P NP	2 Det . the				
0 Det . a	1 V . ate	2 Det . a				
	1 P . with					

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon					
0 NP . Papa	1 VP . VP PP	2 NP . Papa						
0 Det . the	1 PP . P NP	2 Det . the						
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon					
0 NP . Papa	1 VP . VP PP	2 NP . Papa						
0 Det . the	1 PP . P NP	2 Det . the						
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	3 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon					
0 NP . Papa	1 VP . VP PP	2 NP . Papa						
0 Det . the	1 PP . P NP	2 Det . the						
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

attach

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa						
0 Det . the	1 PP . P NP	2 Det . the						
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

**attach**  
*(again!)*

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa					0 S NP VP .	
0 Det . the	1 PP . P NP	2 Det . the					1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

**attach**  
*(again!)*



0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa						0 S NP VP .
0 Det . the	1 PP . P NP	2 Det . the						1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a						4 PP . P NP
	1 P . with							

	0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .		1 V ate .		2 Det the .		3 N caviar .		
0 S . NP VP	0 S NP . VP		1 VP V . NP		2 NP Det . N		2 NP Det N .		
0 NP . Det N	0 NP NP . PP		2 NP . Det N		3 N . caviar		1 VP V NP .		
0 NP . NP PP	1 VP . V NP		2 NP . NP PP		3 N . spoon		2 NP NP . PP		
0 NP . Papa	1 VP . VP PP		2 NP . Papa				0 S NP VP .		
0 Det . the	1 PP . P NP		2 Det . the				1 VP VP . PP		
0 Det . a	1 V . ate		2 Det . a				4 PP . P NP		
	1 P . with						0 ROOT S .		

**attach**  
*(again!)*

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP				
	1 P . with			0 ROOT S .				

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP				
	1 P . with			0 ROOT S .				
				4 P . with				

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP				
	1 P . with							0 ROOT S .
								4 P . with

0	Papa	1	ate	2	the	3	caviar	4	with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .					
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .						
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .						
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP						
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .						
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP						
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP						
	1 P . with			0 ROOT S .						
				4 P . with						

0	Papa	1	ate	2	the	3	caviar	4	with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .					
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .						
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP						
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .						
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP						
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP						
	1 P . with			0 ROOT S .						
				4 P . with						

0	Papa	1	ate	2	the	3	caviar	4	with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .					
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP					
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .	5 NP . Papa					
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP						
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP						
	1 P . with			0 ROOT S .						
				4 P . with						



0	Papa	1	ate	2	the	3	caviar	4	with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .					
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP					
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .	5 NP . Papa					
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the					
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a					
	1 P . with			0 ROOT S .						
				4 P . with						

0	Papa	1	ate	2	the	3	caviar	4	with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .					
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP					
0 NP . Papa	1 VP . VP PP	2 NP . Papa			0 S NP VP .	5 NP . Papa				
0 Det . the	1 PP . P NP	2 Det . the			1 VP VP . PP	5 Det . the				
0 Det . a	1 V . ate	2 Det . a			4 PP . P NP	5 Det . a				
	1 P . with				0 ROOT S .					
					4 P . with					

0	Papa	1	ate	2	the	3	caviar	4	with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .					
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP					
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .	5 NP . Papa					
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the					
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a					
	1 P . with			0 ROOT S .						
				4 P . with						

0	Papa	1	ate	2	the	3	caviar	4	with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .					
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP					
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N					
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP					
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .	5 NP . Papa					
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the					
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a					
	1 P . with							0 ROOT S .		
								4 P . with		

e	2	the	3	caviar	4	with	5	a	6
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .				
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP					
P	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N					
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP					
ρ	2 NP . Papa		0 S NP VP .	5 NP . Papa					
	2 Det . the		1 VP VP . PP	5 Det . the					
	2 Det . a		4 PP . P NP	5 Det . a					
			0 ROOT S .						
			4 P . with						

	<b>e</b>	<b>2</b>	<b>the</b>	<b>3</b>	<b>caviar</b>	<b>4</b>	<b>with</b>	<b>5</b>	<b>a</b>	<b>6</b>	
		1 V	ate .	2 Det	the .	3 N	caviar .	4 P	with .	5 Det	a .
		1 VP	V . NP	2 NP	Det . N	2 NP	Det N .	4 PP	P . NP	5 NP	Det . N
P		2 NP	. Det N	3 N	. caviar	1 VP	V NP .	5 NP	. Det N		
		2 NP	. NP PP	3 N	. spoon	2 NP	NP . PP	5 NP	. NP PP		
ɔ		2 NP	. Papa			0 S	NP VP .	5 NP	. Papa		
		2 Det	. the			1 VP	VP . PP	5 Det	. the		
		2 Det	. a			4 PP	. P NP	5 Det	. a		
						0 ROOT	S .				
						4 P	. with				

	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
<b>e</b>	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N
P	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon
ɔ	2 NP . Papa		0 S NP VP .	5 NP . Papa	
	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S .		
			4 P . with		

	<b>e</b>	<b>2</b>	<b>the</b>	<b>3</b>	<b>caviar</b>	<b>4</b>	<b>with</b>	<b>5</b>	<b>a</b>	<b>6</b>	
		1 V	ate .	2 Det	the .	3 N	caviar .	4 P	with .	5 Det	a .
		1 VP	V . NP	2 NP	Det . N	2 NP	Det N .	4 PP	P . NP	5 NP	Det . N
P		2 NP	. Det N	3 N	. caviar	1 VP	V NP .	5 NP	. Det N	6 N	. caviar
		2 NP	. NP PP	3 N	. spoon	2 NP	NP . PP	5 NP	. NP PP	6 N	. spoon
ɔ		2 NP	. Papa			0 S	NP VP .	5 NP	. Papa		
		2 Det	. the			1 VP	VP . PP	5 Det	. the		
		2 Det	. a			4 PP	. P NP	5 Det	. a		
						0 ROOT	S .				
						4 P	. with				



	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>
e	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon .
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	
P	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	
ρ	2 NP . Papa		0 S NP VP .	5 NP . Papa		
	2 Det . the		1 VP VP . PP	5 Det . the		
	2 Det . a		4 PP . P NP	5 Det . a		
			0 ROOT S .			
			4 P . with			

	<b>e</b>	<b>2</b>	<b>the</b>	<b>3</b>	<b>caviar</b>	<b>4</b>	<b>with</b>	<b>5</b>	<b>a</b>	<b>6</b>	<b>spoon</b>	<b>7</b>
		1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon .					
		1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	5 NP Det N .					
P		2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar						
		2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon						
ɔ		2 NP . Papa		0 S NP VP .	5 NP . Papa							
		2 Det . the		1 VP VP . PP	5 Det . the							
		2 Det . a		4 PP . P NP	5 Det . a							
				0 ROOT S .								
				4 P . with								

	<b>e</b>	<b>2</b>	<b>the</b>	<b>3</b>	<b>caviar</b>	<b>4</b>	<b>with</b>	<b>5</b>	<b>a</b>	<b>6</b>	<b>spoon</b>	<b>7</b>	
		1 V	ate .	2 Det	the .	3 N	caviar .	4 P	with .	5 Det	a .	6 N	spoon .
		1 VP	V . NP	2 NP	Det . N	2 NP	Det N .	4 PP	P . NP	5 NP	Det . N	5 NP	Det N .
P		2 NP	. Det N	3 N	. caviar	1 VP	V NP .	5 NP	. Det N	6 N	. caviar	4 PP	P NP .
		2 NP	. NP PP	3 N	. spoon	2 NP	NP . PP	5 NP	. NP PP	6 N	. spoon	5 NP	NP . PP
ɔ		2 NP	. Papa			0 S	NP VP .	5 NP	. Papa				
		2 Det	. the			1 VP	VP . PP	5 Det	. the				
		2 Det	. a			4 PP	. P NP	5 Det	. a				
						0	ROOT S .						
						4 P	. with						

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa				2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP				
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP				
	1 P . with					0 ROOT S .				
						4 P . with				

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S .		
				4 P . with		

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				



0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				
						0 ROOT S .				

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				
						0 ROOT S .				

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S .		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP .
						1 VP VP . PP
						7 P . with
						0 ROOT S .

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S .		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP .
						1 VP VP . PP
						7 P . with
						0 ROOT S .

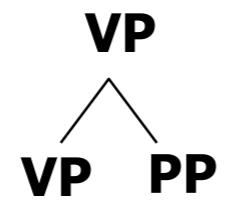
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0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				
						0 ROOT S .				

# Left Recursion Kills Pure Top-Down Parsing ...

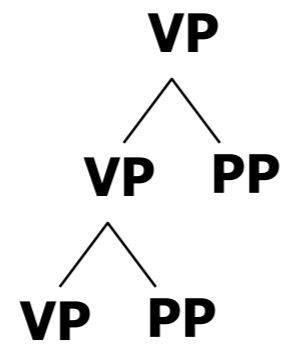
**VP**



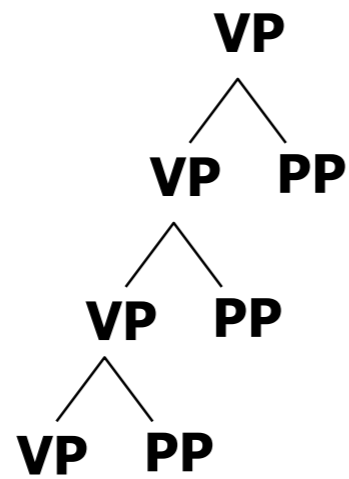
# Left Recursion Kills Pure Top-Down Parsing ...



# Left Recursion Kills Pure Top-Down Parsing ...



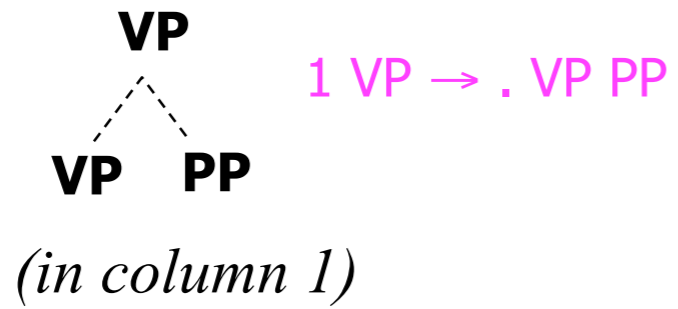
## Left Recursion Kills Pure Top-Down Parsing ...



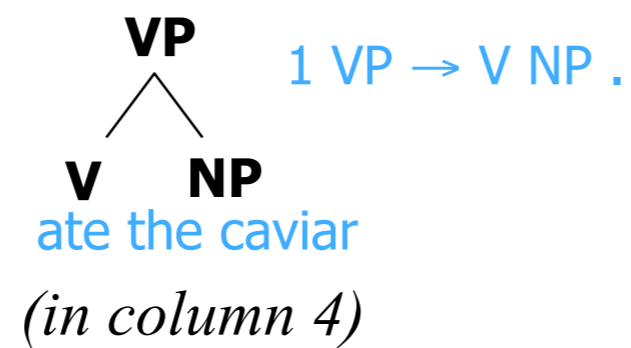
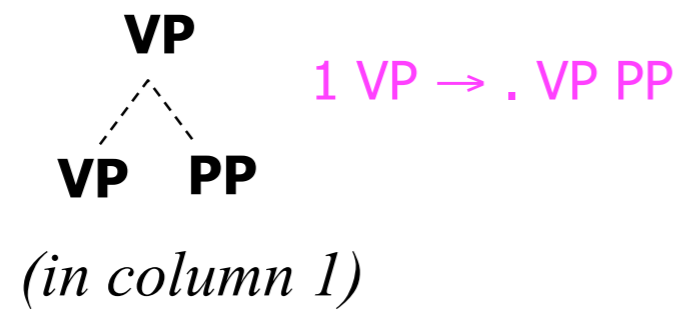
makes new hypotheses  
ad infinitum before we've  
seen the PPs at all

hypotheses try to predict  
in advance how many  
PP's will arrive in input

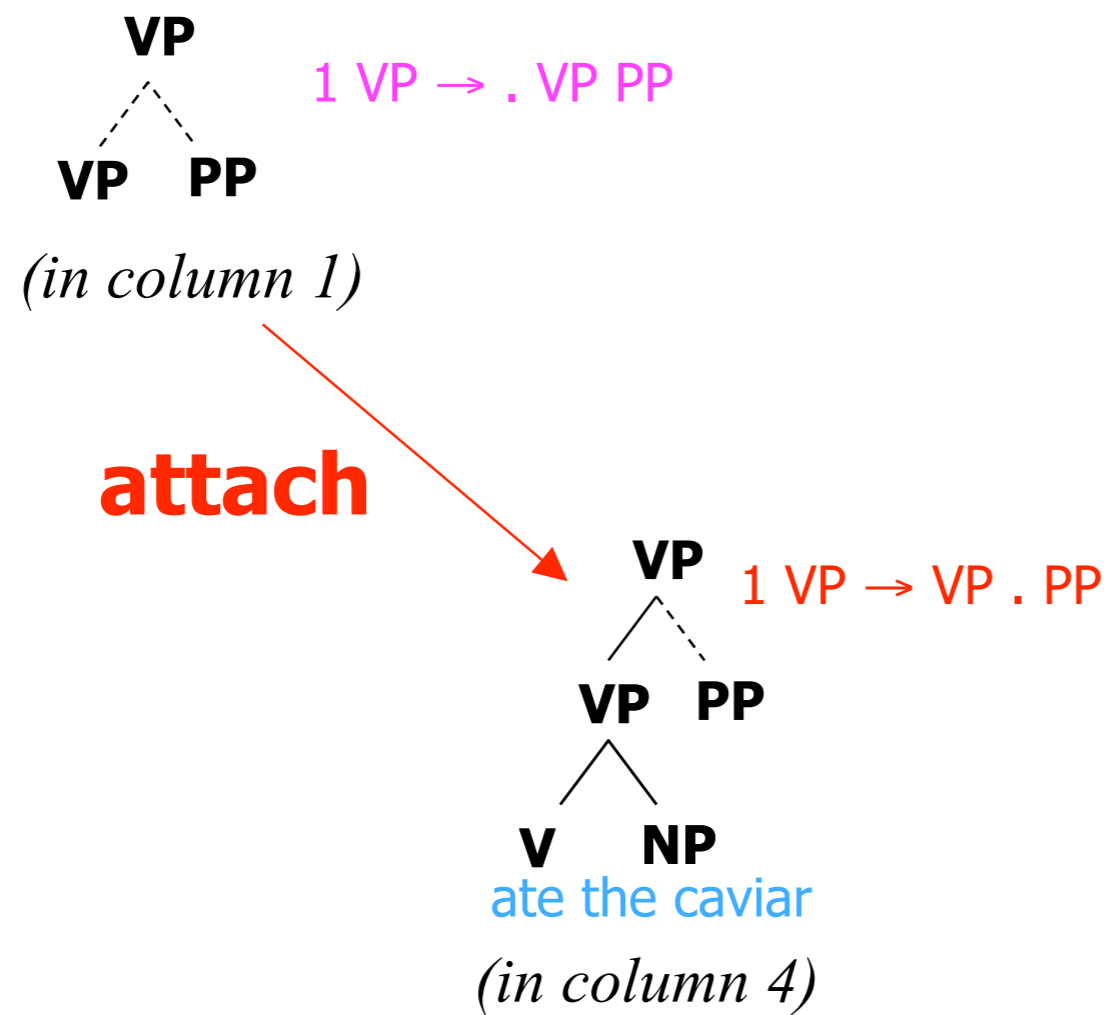
... but Earley's Alg is Okay!



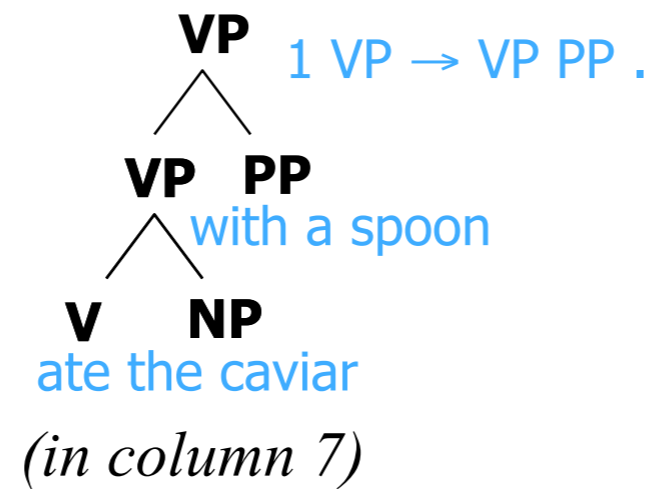
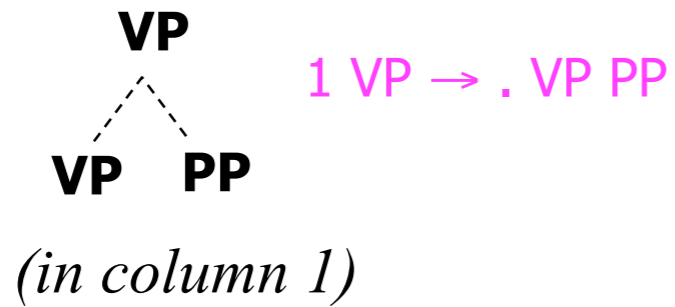
## ... but Earley's Alg is Okay!



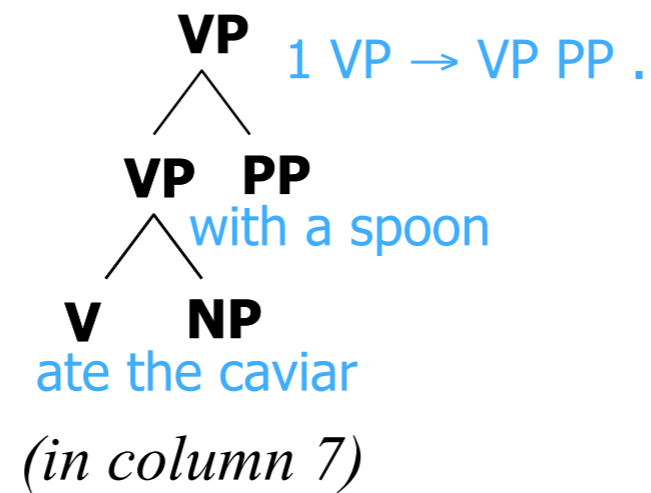
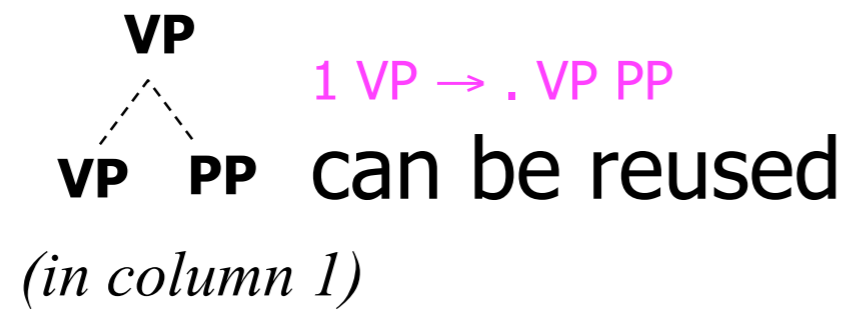
## ... but Earley's Alg is Okay!



## ... but Earley's Alg is Okay!

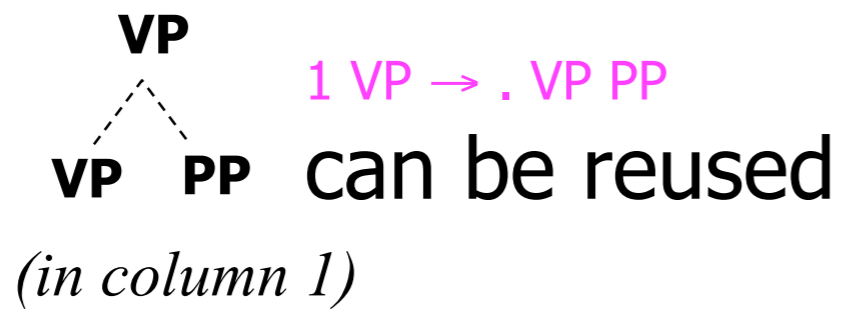


## ... but Earley's Alg is Okay!

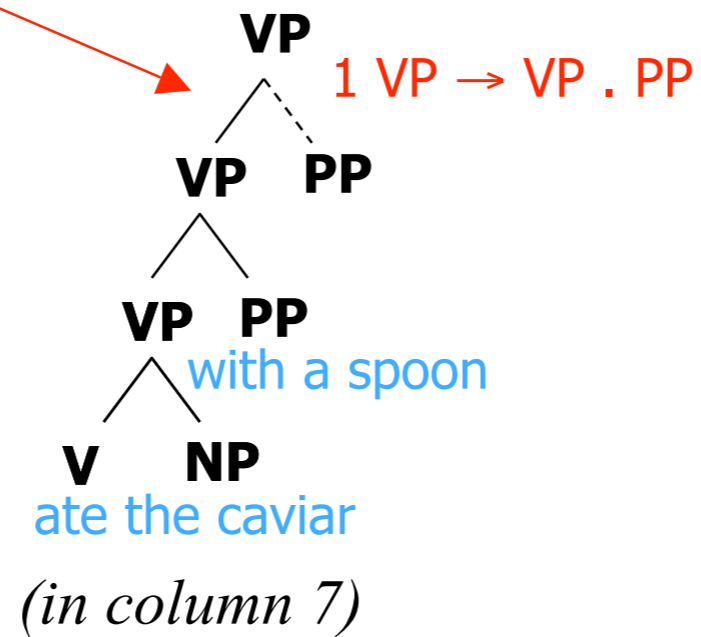




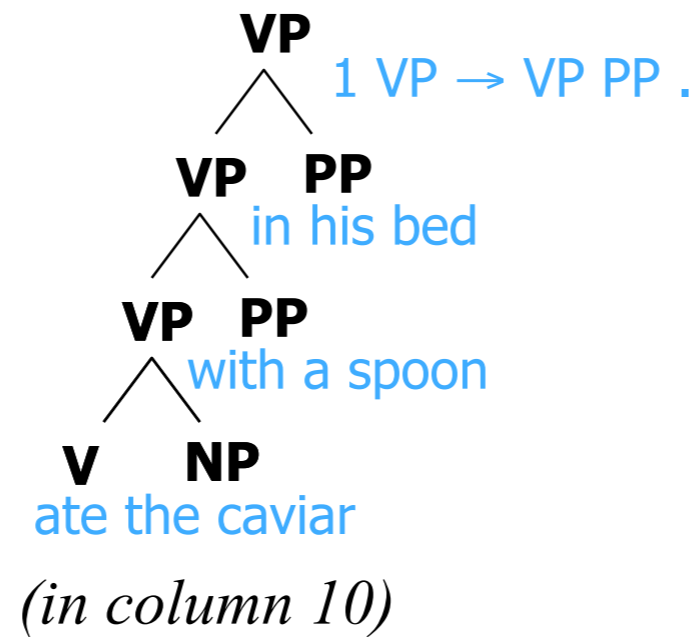
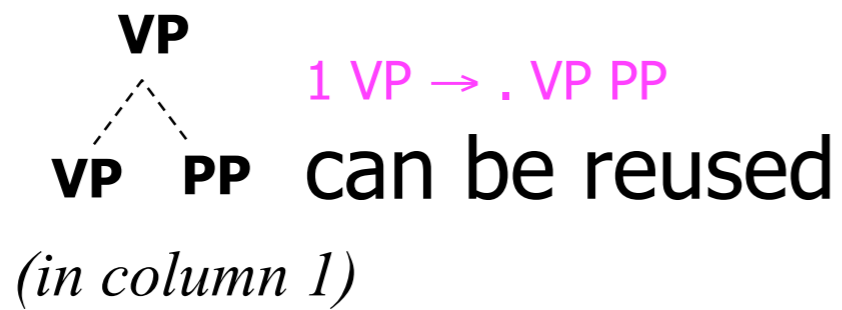
## ... but Earley's Alg is Okay!



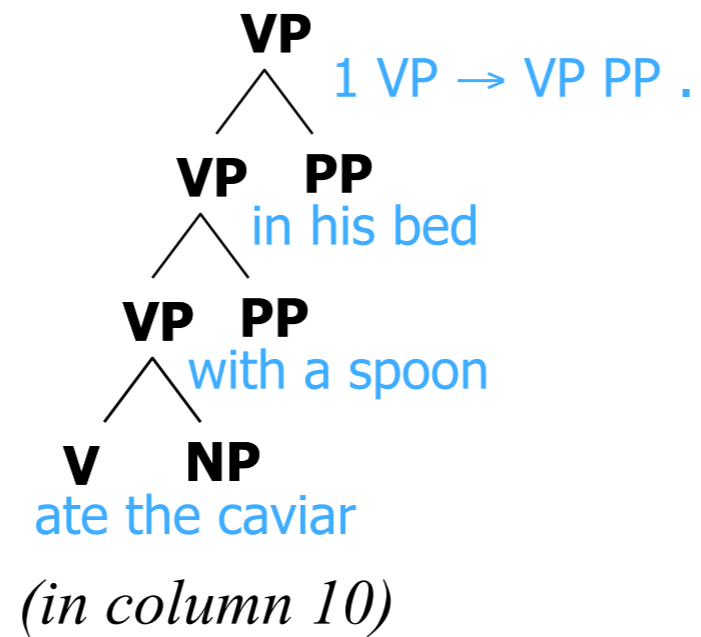
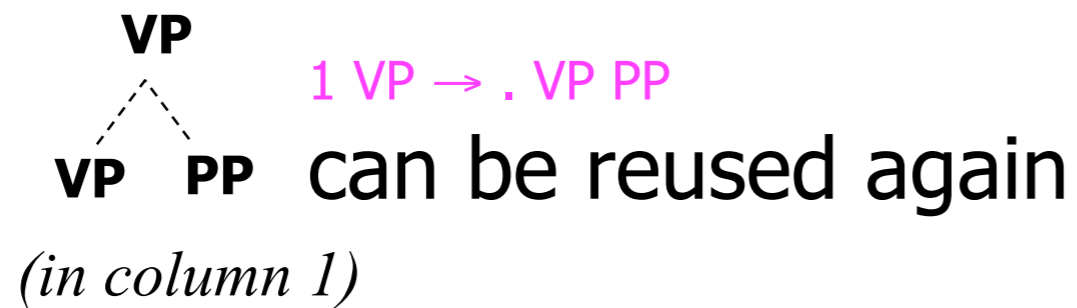
**attach**



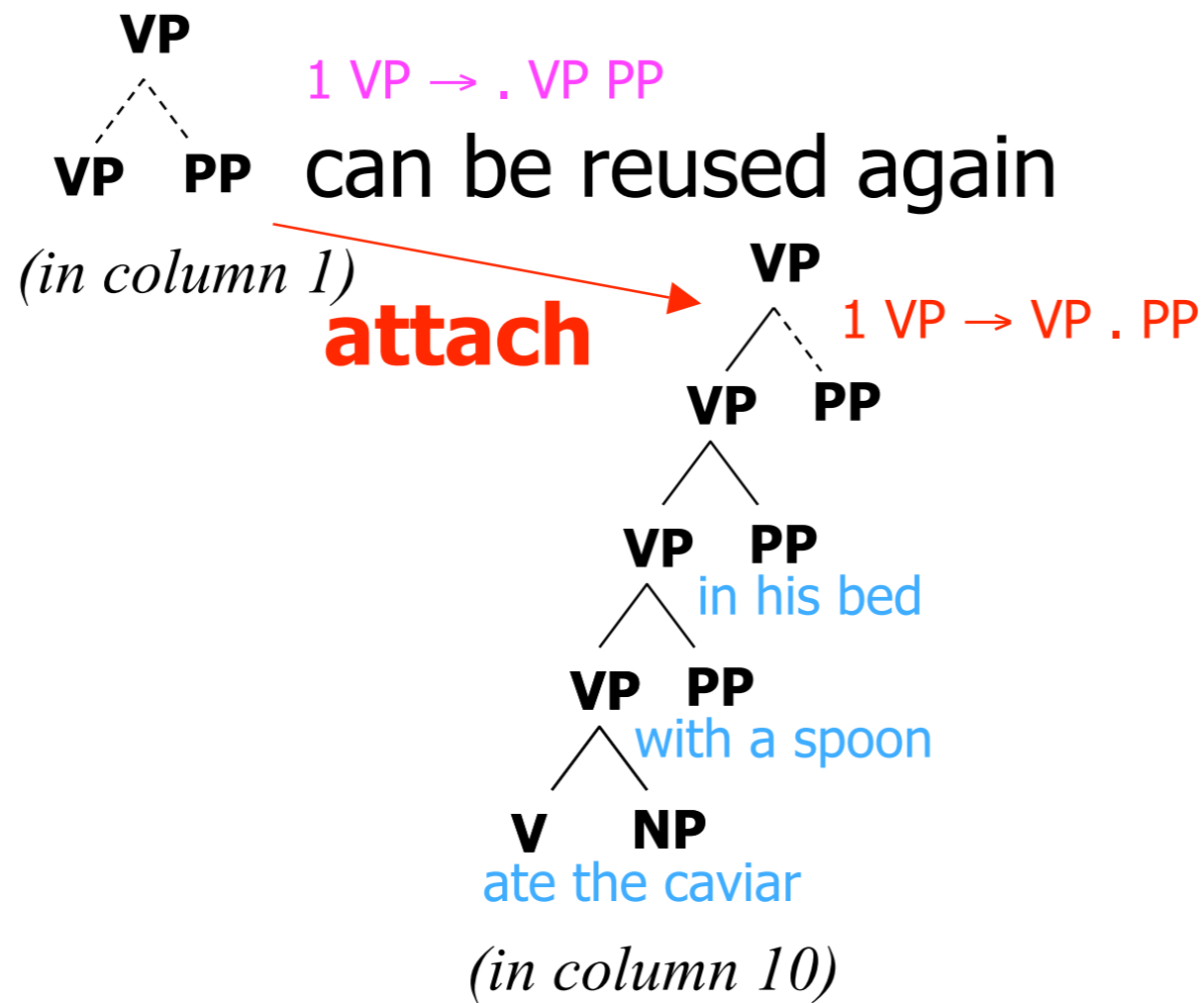
## ... but Earley's Alg is Okay!



## ... but Earley's Alg is Okay!



## ... but Earley's Alg is Okay!



0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				
						0 ROOT S .				

completed a VP in col 4  
col 1 lets us use it in a VP PP structure

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	...	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP .		2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP				
	1 P . with			0 ROOT S .		1 VP V NP .				
				4 P . with		2 NP NP . PP				
						0 S NP VP .				
						1 VP VP . PP				
						7 P . with				
						0 ROOT S .				

completed that VP = VP PP in col 7  
col 1 would let us use *it* in a VP PP structure  
can reuse col 1 as often as we need

# Beyond Recognition

- So far, we've described an Earley *recognizer*
- Note what we did when we tried to create entries that already existed
- What should we do when combining items?
- How to derive outside algorithm?

# Better Treebank Grammars

- Last time: CNF conversion, Markovization
- Clustering and splitting nonterminals
- Grandparent annotation
- Lexicalization