

■ Light and Optics

- Pinhole camera model
- Perspective projection
- Thin lens model
- Fundamental equation
- Distortion: spherical & chromatic aberration, radial distortion
- Reflection and Illumination: color, Lambertian and specular surfaces, Phong, BRDF

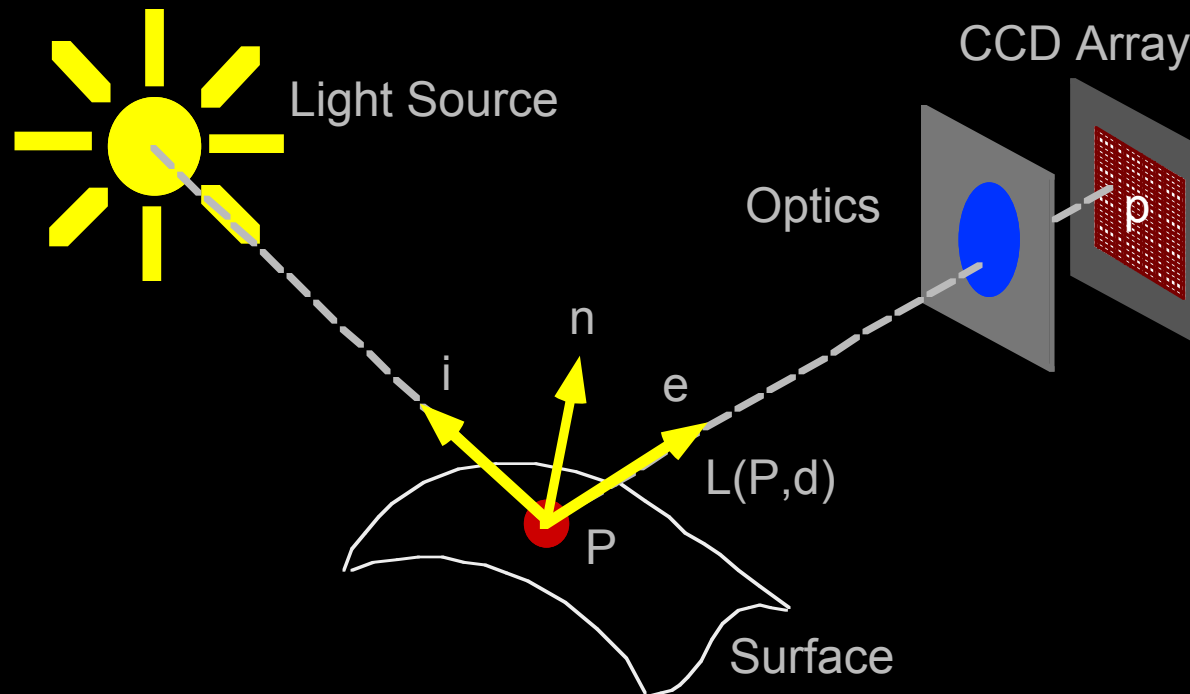
■ Sensing Light

■ Conversion to Digital Images

■ Sampling Theorem

■ Other Sensors: frequency, type,

- Radiometry is the part of image formation concerned with the relation among the amounts of light energy emitted from light sources, reflected from surfaces, and registered by sensors.



- Typical imaging scenario:
 - visible light
 - ideal lenses
 - standard sensor (e.g. TV camera)
 - opaque objects
- Goal

To create 'digital' images which can be processed to recover some of the characteristics of the 3D world which was imaged.



World	reality
Optics	focus light from world on sensor
Sensor	converts light to electrical energy
Signal	representation of incident light as continuous electrical energy
Digitizer	converts continuous signal to discrete signal
Digital Rep.	final representation of reality in computer memory

■ Geometry

- concerned with the relationship between points in the three-dimensional world and their images

■ Radiometry

- concerned with the relationship between the amount of light radiating from a surface and the amount incident at its image

■ Photometry

- concerned with ways of measuring the intensity of light

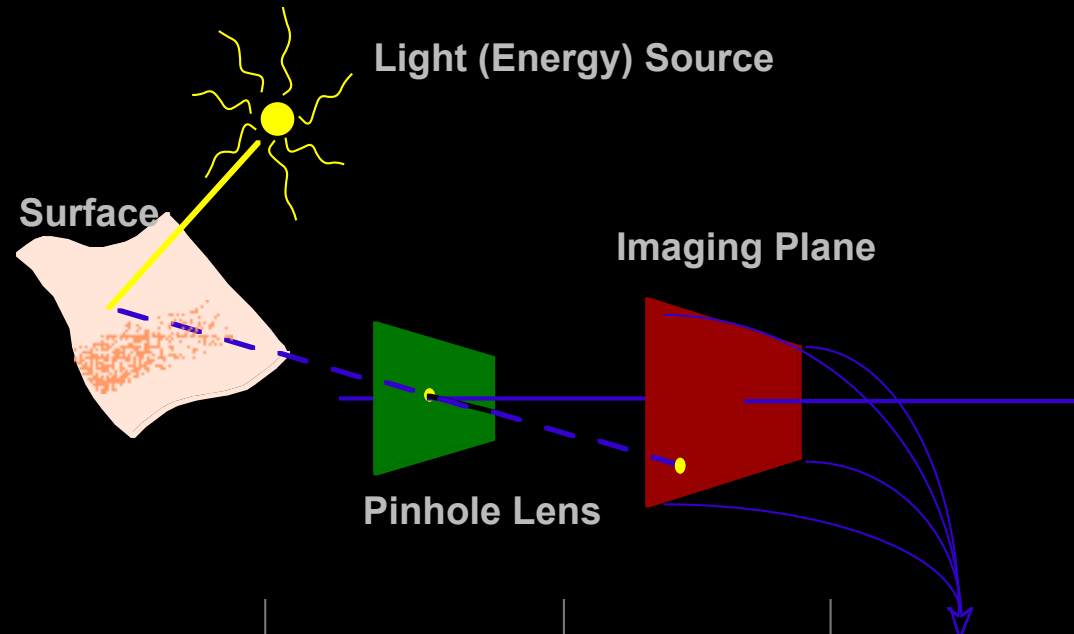
■ Digitization

- concerned with ways of converting continuous signals (in both space and time) to digital approximations

Introduction to

Computer Vision

Image Formation



World

Optics

Sensor

Signal

B&W Film

Silver Density

Color Film

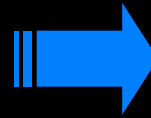
Silver density
in three color
layers

TV Camera

Electrical

- Geometry describes the projection of:

three-dimensional
(3D) world



two-dimensional
(2D) image plane.

- Typical Assumptions

- Light travels in a straight line

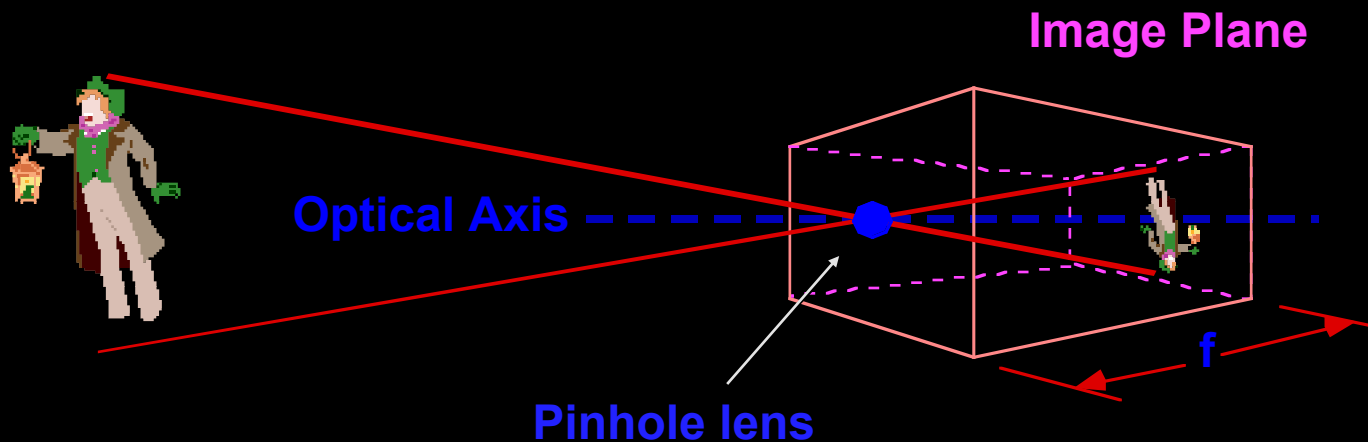
- Optical Axis: the perpendicular from the image plane through the pinhole (also called the central projection ray)

- Each point in the image corresponds to a particular direction defined by a ray from that point through the pinhole.

- Various kinds of projections:

- - perspective - oblique
- - orthographic - isometric
- - spherical

- Two camera models are commonly used:
 - Pin-hole camera
 - Optical system composed of lenses
- Pin-hole is the basis for most graphics and vision
 - Derived from physical construction of early cameras
 - Mathematics is very straightforward
- Thin lens model is first of the lens models
 - Mathematical model for a physical lens
 - Lens gathers light over area and focuses on image plane.



- World projected to 2D Image
 - Image inverted
 - Size reduced (usually)
 - Image is dim
 - No direct depth information
- f called the focal length of the “lens”
- Known as perspective projection

Amsterdam

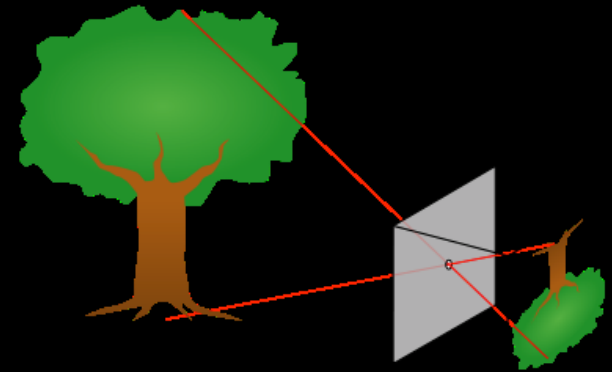
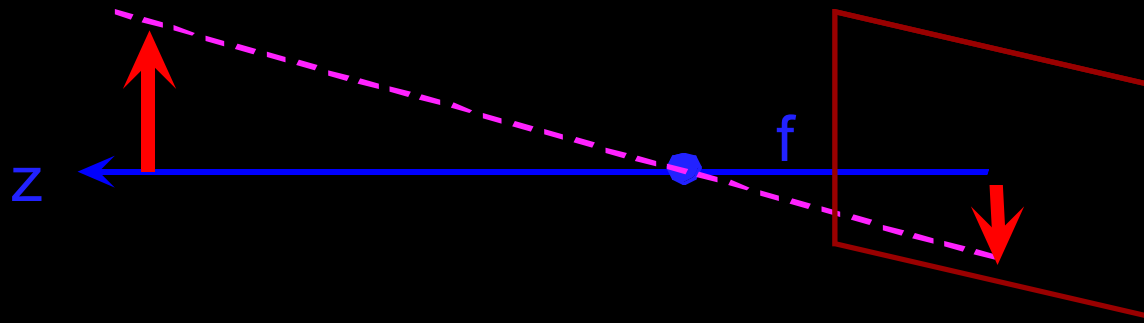
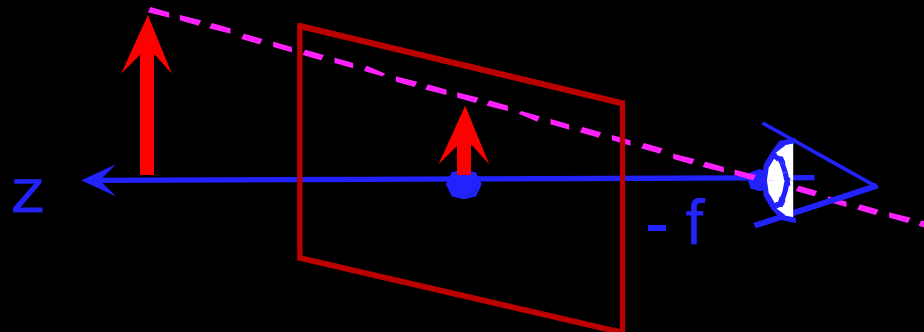


Photo by Robert Kosara, robert@kosara.net
<http://www.kosara.net/gallery/pinholeamsterdam/pic01.html>

- Consider case with object on the optical axis:



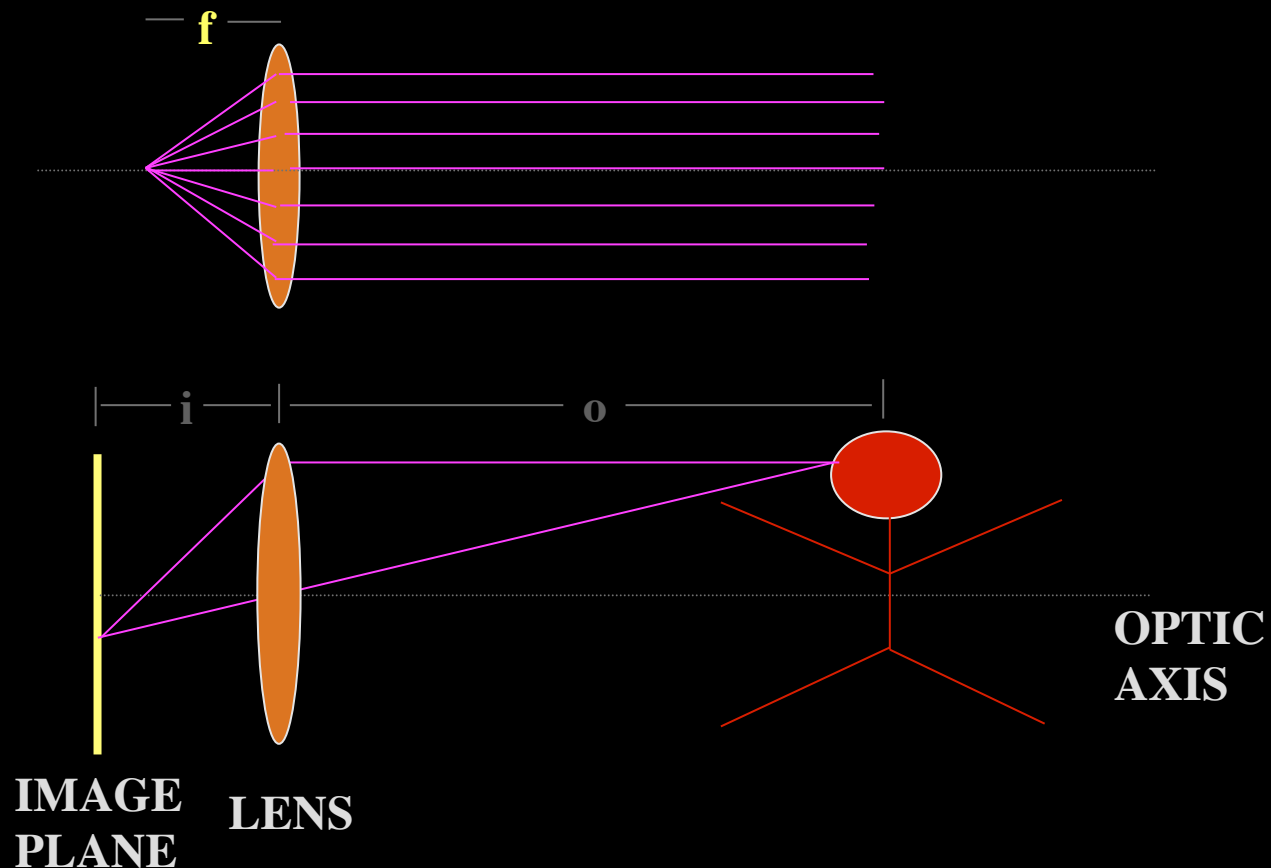
- More convenient with upright image:



Projection plane $z = 0$

- Equivalent mathematically

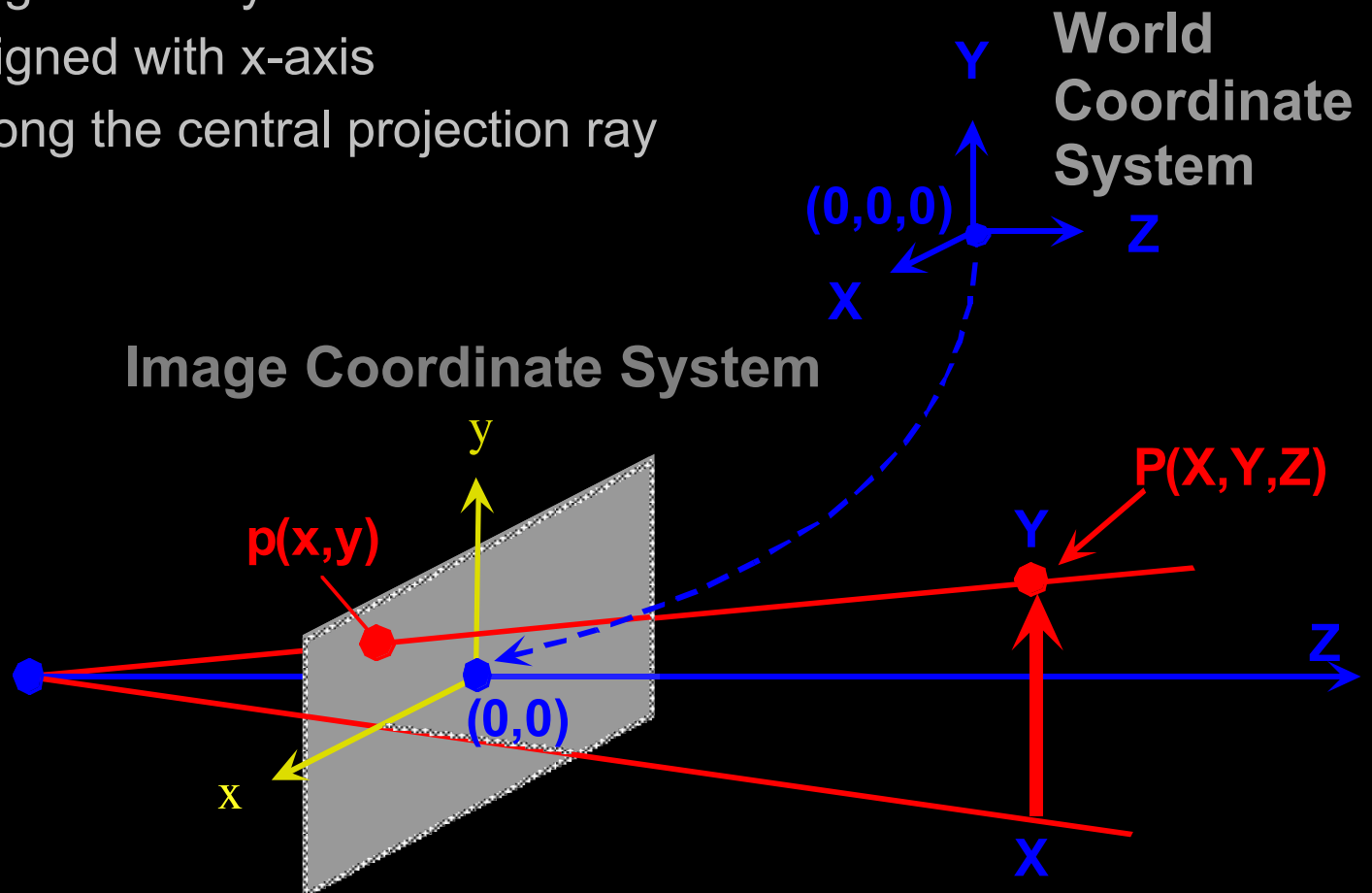
- Rays entering parallel on one side converge at focal point.
- Rays diverging from the focal point become parallel.



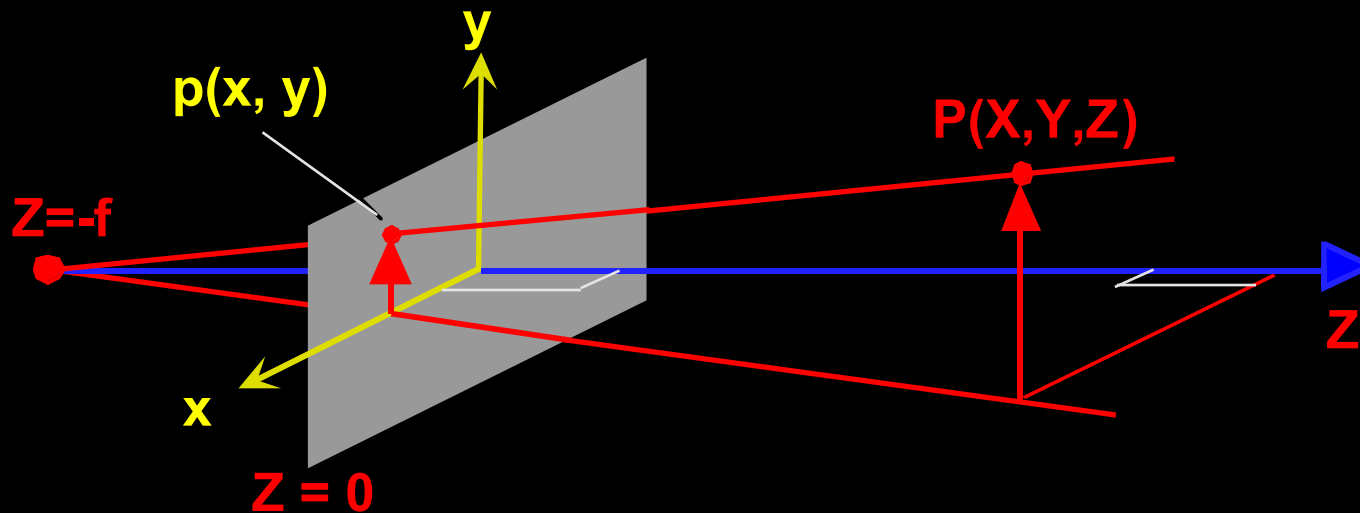
$$\frac{1}{f} = \frac{1}{i} + \frac{1}{o} \quad \text{'THIN LENS LAW'}$$

■ Simplified Case:

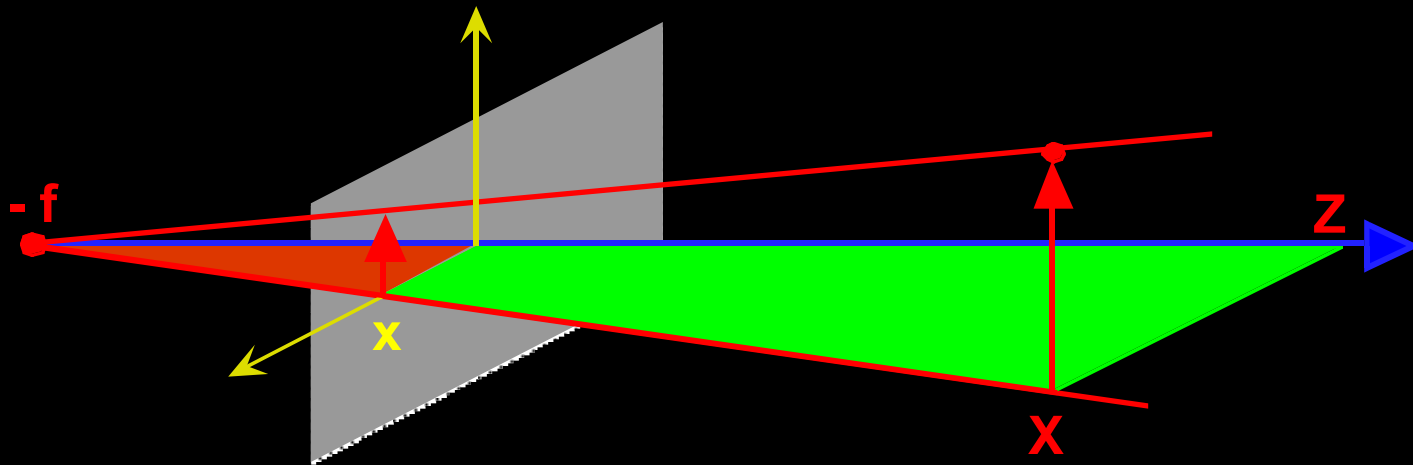
- Origin of world and image coordinate systems coincide
- Y-axis aligned with y -axis
- X-axis aligned with x -axis
- Z-axis along the central projection ray



- Compute the image coordinates of p in terms of the world coordinates of P .

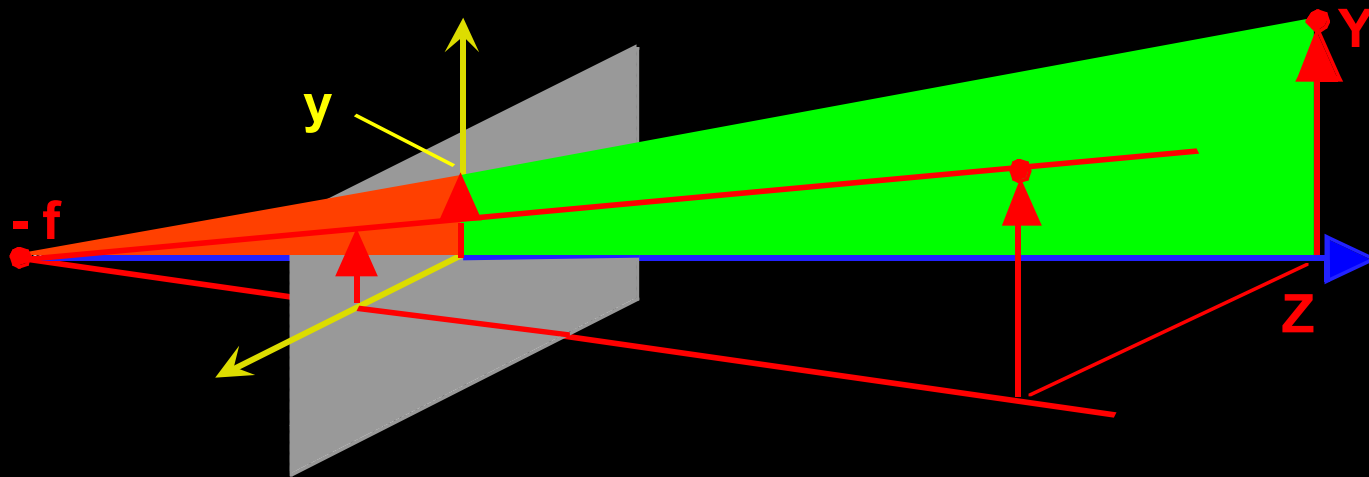


- Look at projections in x - z and y - z planes



■ By similar triangles: $\frac{x}{f} = \frac{X}{Z+f}$

$$x = \frac{fX}{Z+f}$$



■ By similar triangles: $\frac{y}{f} = \frac{Y}{Z+f}$

$$y = \frac{fY}{Z+f}$$

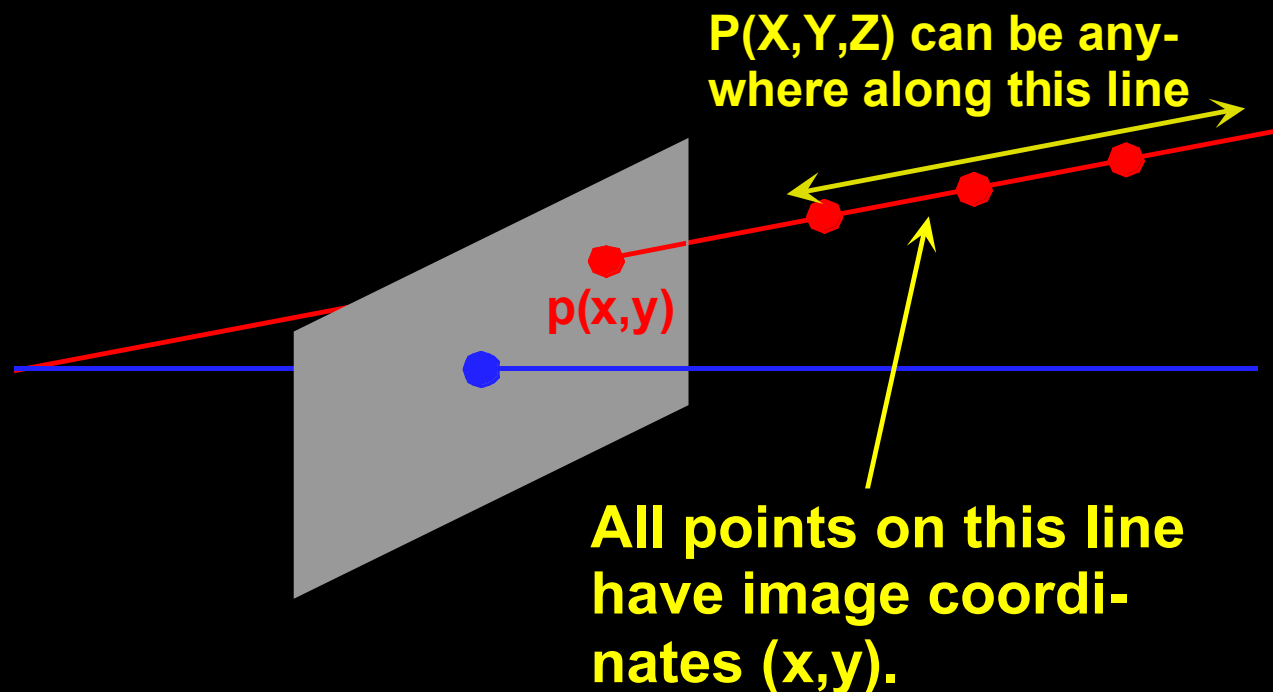
- Given point $P(X, Y, Z)$ in the 3D world
- The two equations:

$$x = \frac{fX}{Z+f}$$

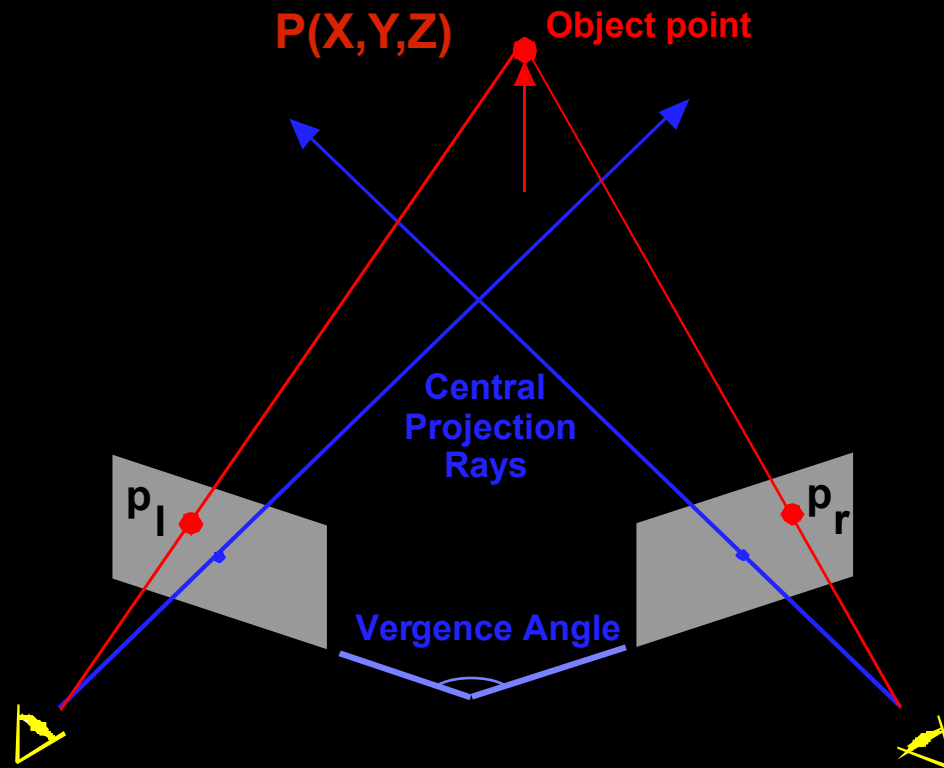
$$y = \frac{fY}{Z+f}$$

- transform world coordinates (X, Y, Z)
into image coordinates (x, y)

- Given a center of projection and image coordinates of a point, it is not possible to recover the 3D depth of the point from a single image.



In general, at least two images of the same point taken from two different locations are required to recover depth.



- Depth obtained by triangulation
- Correspondence problem: p_l and p_r must correspond to the left and right projections of P , respectively.

- Consequences of image formation geometry for computer vision
 - What set of shapes can an object take on if it is:
 - rigid
 - non-rigid
 - planar
 - non-planar
 - SIFT features:
 - Deals with variability of rigid, planar shapes under perspective distortion, or piecewise rigid, planar shapes.
- Sensitivity to errors.

  Introduction to

  Computer Vision

Radiometry and Light Sources

- **Brightness**: informal notion used to describe both scene and image brightness.
- **Image brightness**: related to energy flux incident on the image plane:

IRRADIANCE (illuminance)

“It’s a bright day.”

- **Scene brightness**: brightness related to energy flux emitted (radiated) from a surface.

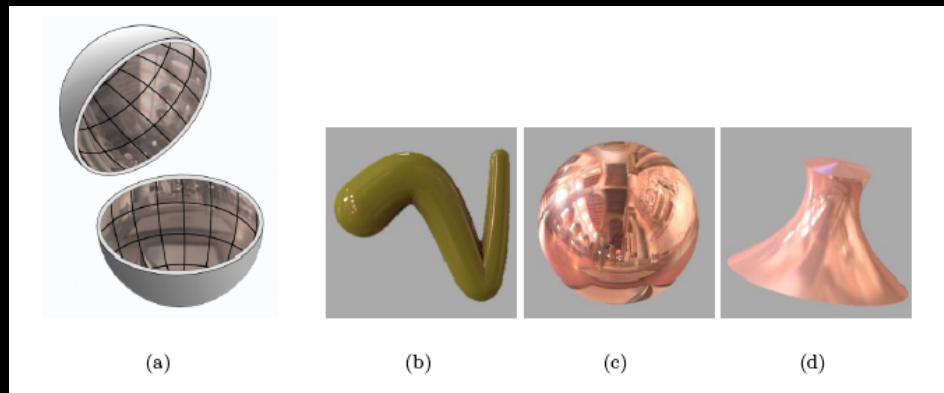
RADIANCE (luminance)

“Yikes, that shirt is way too bright!”



- Reflection
 - mirrors
 - highlights
 - specularities
- Scattering
 - Lambertian
 - matte
 - diffuse

- Point source
- Extended source
- Single wavelength
- Multi-wavelength
- Uniform
- Non-uniform



■ Linearity

● definition: For a linear function $f(x)$, we have:

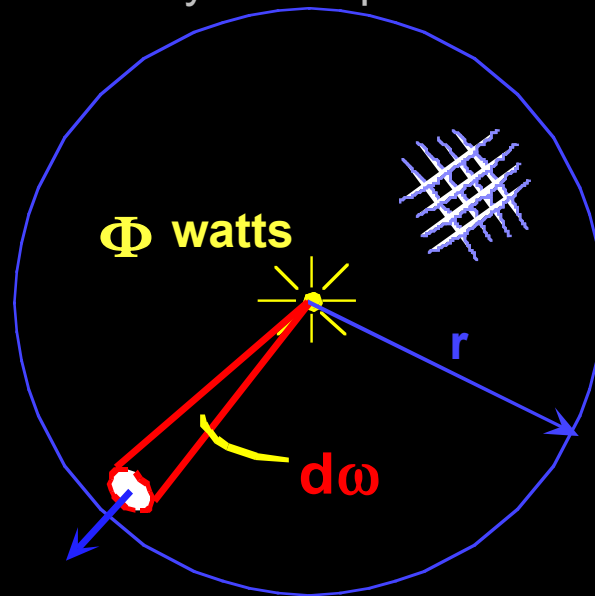
- Additivity: $f(x+y) = f(x) + f(y)$.
- Homogeneity : $f(ax) = a f(x)$.

■ For extended sources

■ For multiple wavelengths

■ Across time

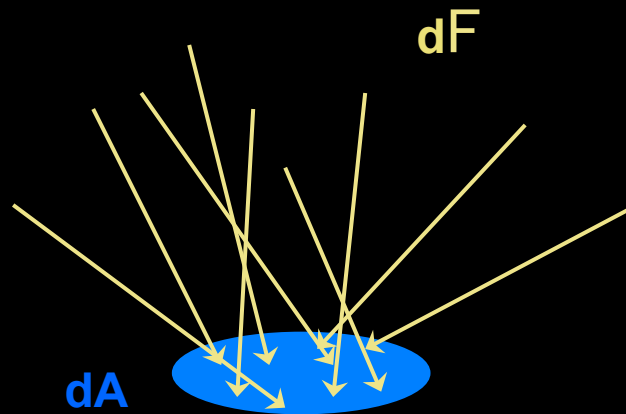
- Point source power: watts.
- F watts radiated into 4π steradians
- Point source radiant intensity: watts per steradian.



$$F = \int_{\text{sphere}} dF$$

R = Point Source Radiant Intensity = $\frac{dF}{d\omega}$ Watts/unit solid angle (steradian)
(of source)

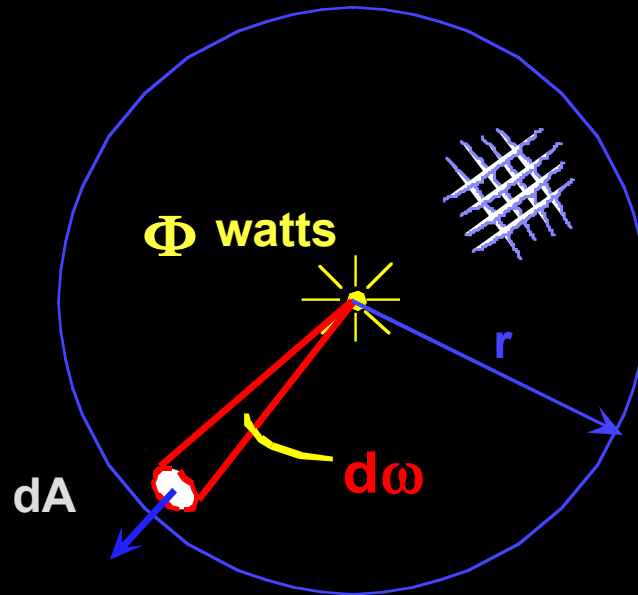
- Light falling on a surface from all directions.
- How much?



- Irradiance: power per unit area falling on a surface.

$$\text{Irradiance } E = \frac{dF}{dA} \quad \text{watts/m}^2$$

- Relationship between point source radiance (radiant intensity) and irradiance



$$dw = \frac{dA}{r^2}$$

$$E = \frac{dF}{dA}$$

R: Radiant Intensity

E: Irradiance

F: Watts

w : Steradians

$$R = \frac{dF}{dw} = \frac{r^2 dF}{dA} = r^2 E$$

$$E = \frac{R}{r^2}$$

Introduction to

Computer Vision

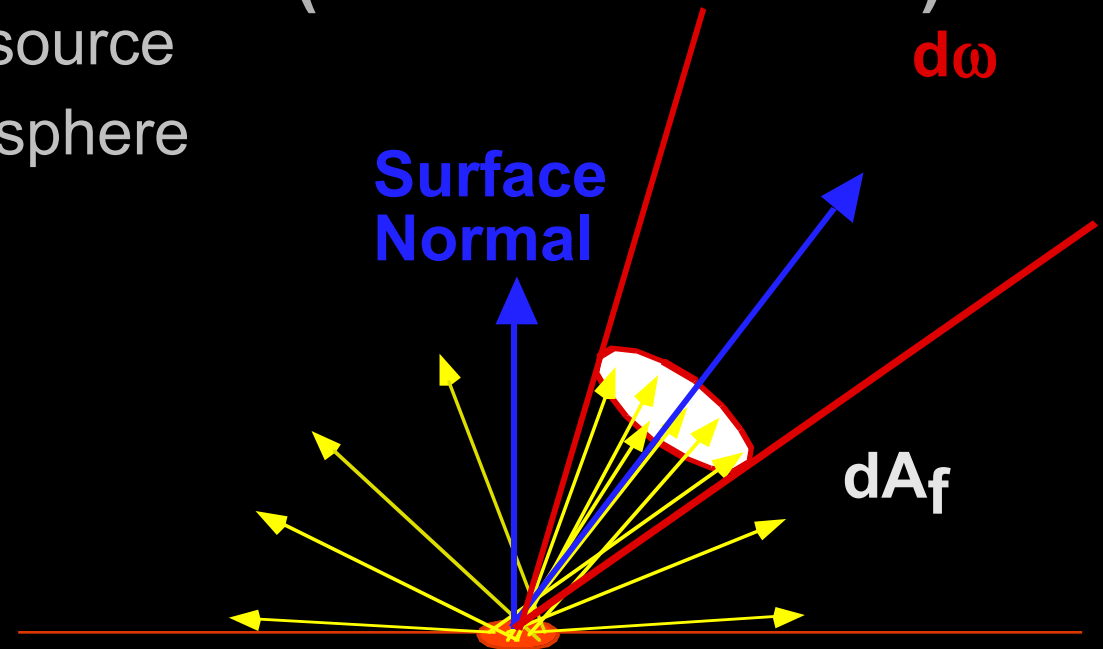
Surface Radiance (Extended source)

- Surface acts as light source
- Radiates over a hemisphere

R: Radiant Intensity

E: Irradiance

L: Surface radiance



- Surface Radiance: power per unit foreshortened area emitted into a solid angle

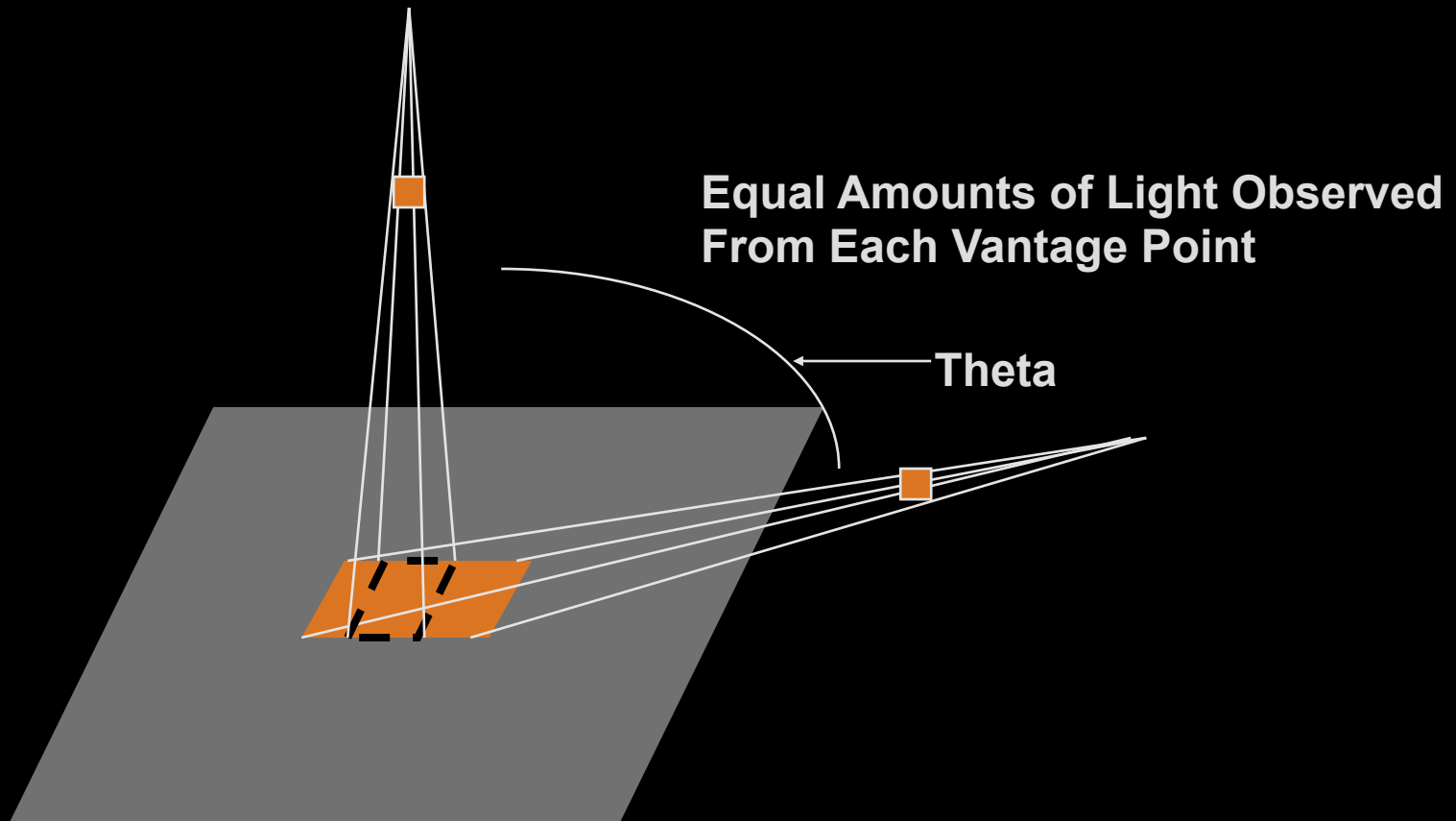
$$L = \frac{dF}{dA_f d\omega}$$

(watts/m² steradian)

- Consider two definitions:
 - Radiance:
power per unit foreshortened area emitted into a solid angle
 - Pseudo-radiance
power per unit area emitted into a solid angle

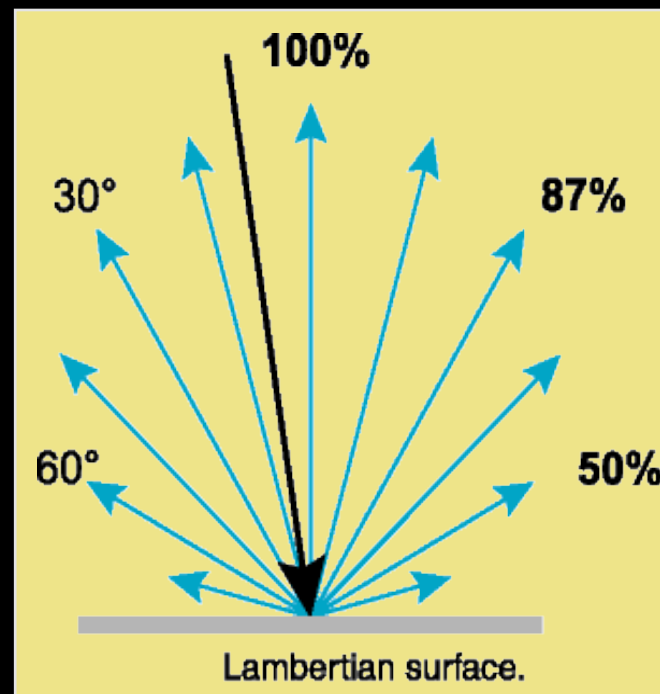
- Why should we work with radiance rather than pseudo-radiance?
 - Only reason: Radiance is more closely related to our intuitive notion of “brightness”.

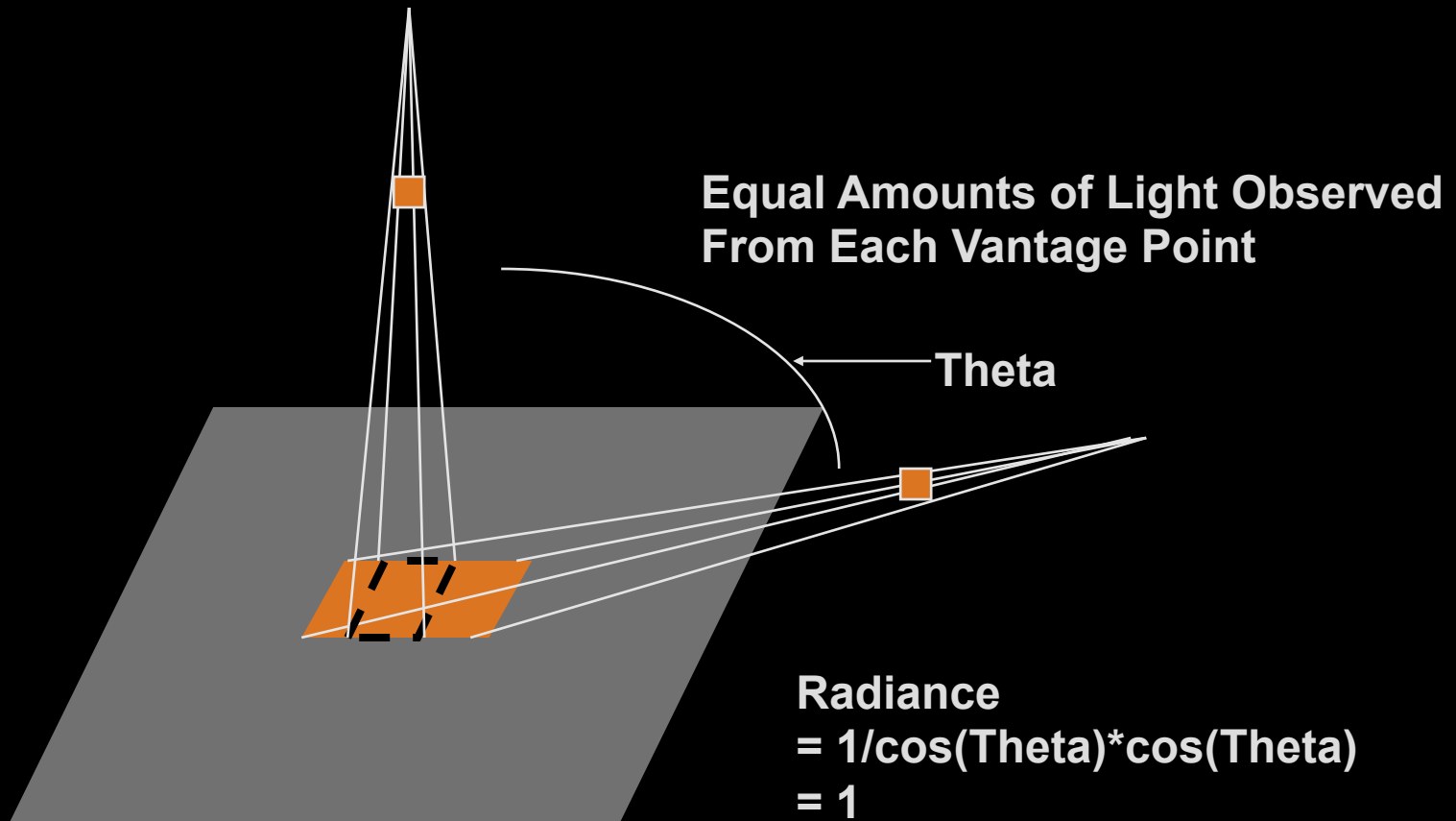
- A particular point P on a Lambertian (perfectly matte) surface appears to have the same brightness no matter what angle it is viewed from.
 - Piece of paper
 - Matte paint
- Doesn't depend upon incident light angle.
- What does this say about how they emit light?



Area of black box = 1
Area of orange box = $1/\cos(\text{Theta})$
Foreshortening rule.

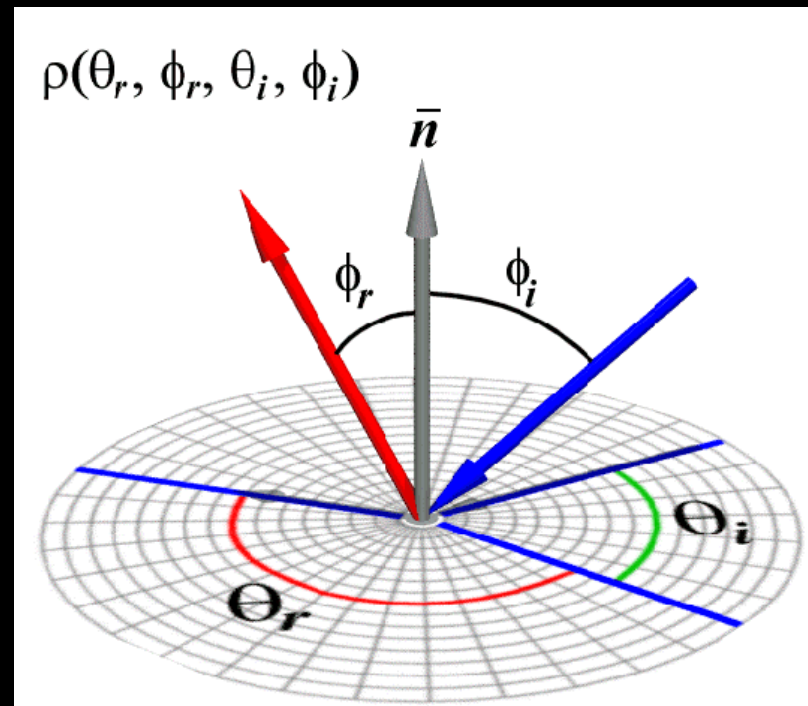
Relative magnitude of light scattered in each direction.
Proportional to $\cos(\theta)$.



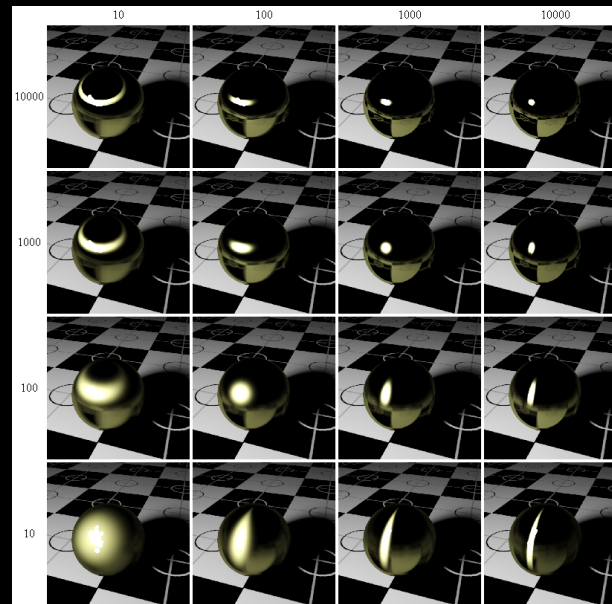


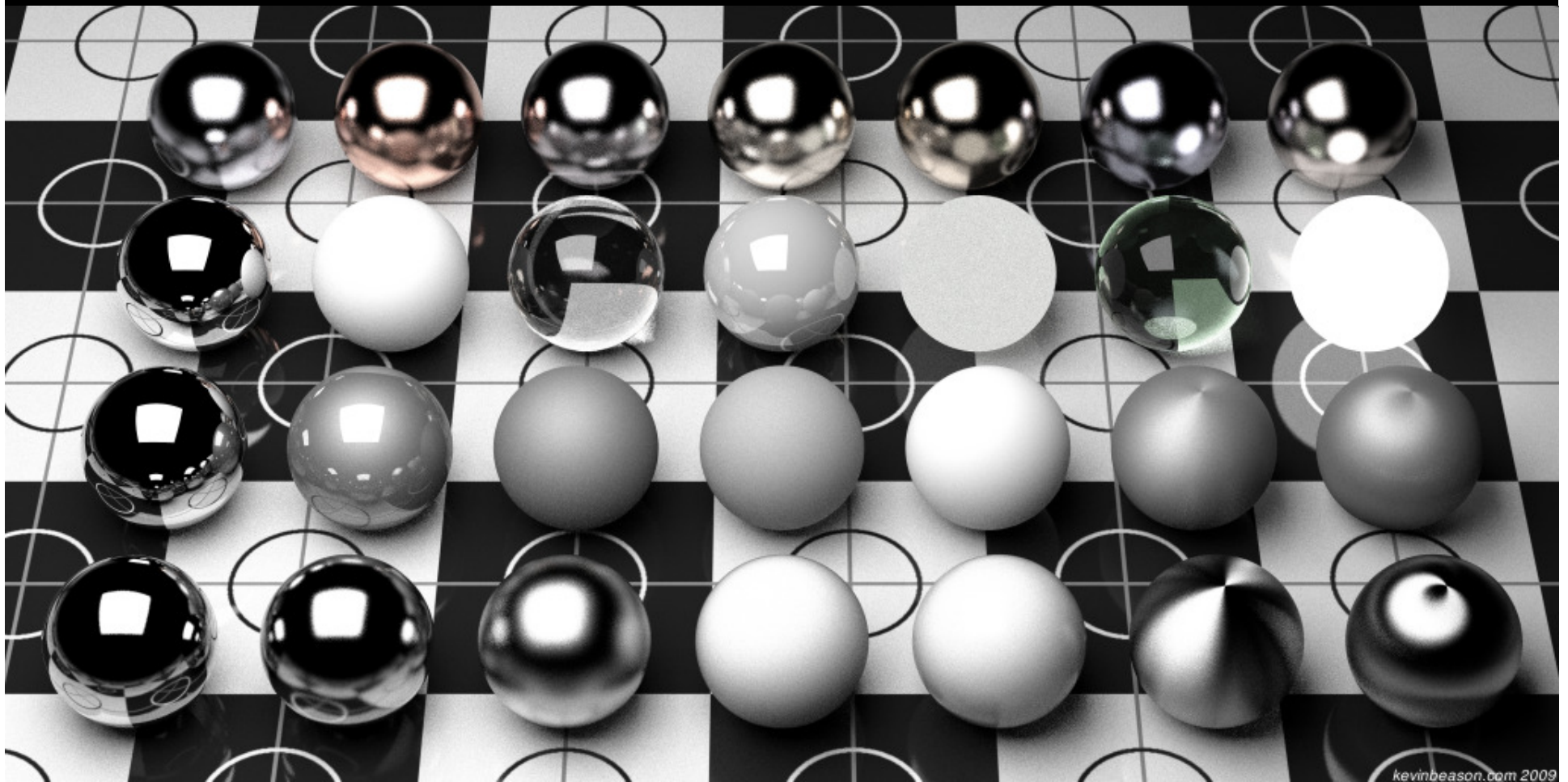
Area of black box = 1
Area of orange box = $1/\cos(\text{Theta})$
Foreshortening rule.

- Bidirectional Reflectance Distribution Function
 - a function of 2 directions (or 4 scalar values)



- Bidirectional Reflectance Distribution Function
 - a function of 2 directions (or 4 scalar values)





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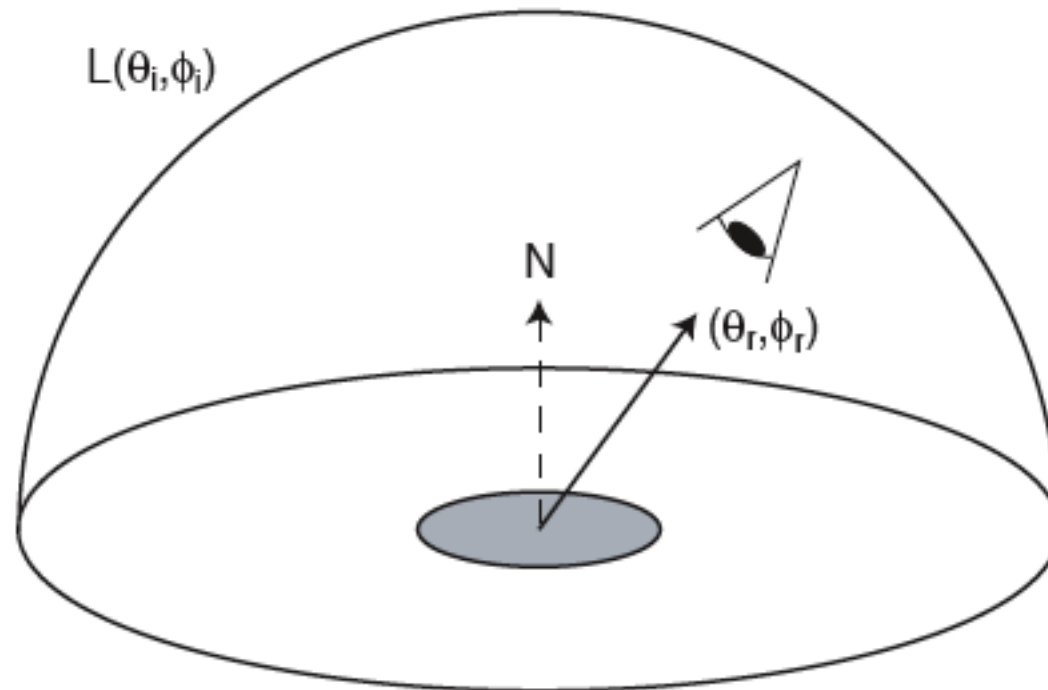
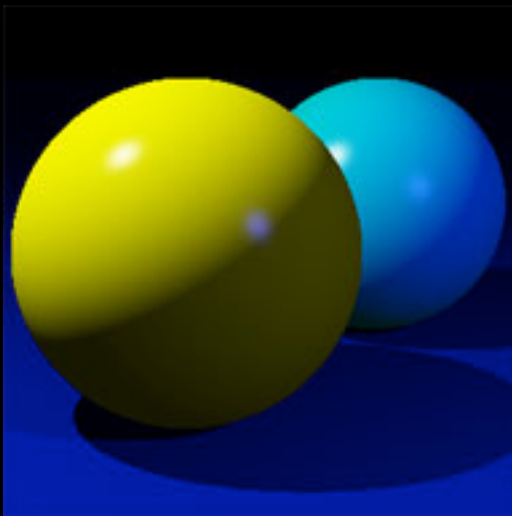


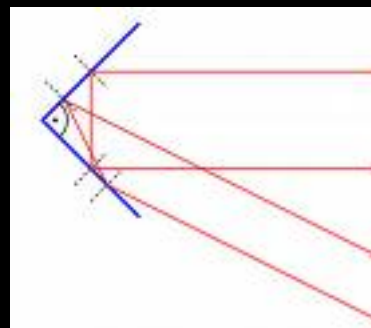
Figure 3.1. A viewer observes a surface patch with normal N from direction (θ_r, ϕ_r) . $L(\theta_i, \phi_i)$ represents radiance of illumination from direction (θ_i, ϕ_i) . The coordinate system is such that N points in direction $(0, 0)$.

$$B(\theta_r, \phi_r) = \int_{\phi_i=0}^{2\pi} \int_{\theta_i=0}^{\pi/2} L(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r) \cos \theta_i \sin \theta_i d\theta_i d\phi_i,$$

The bidirectional reflectance distribution function.



SWISSPEARL CARAT SL			
Alu 001	7002	Reps 001	7008
Alu 002	7003	Reps 002	7009
Alu 003	7004	Reps 003	7010
Alu 004	7005	Reps 004	7011
Alu 005	7006	Reps 005	7012
Alu 006	7007	Reps 006	7013
Alu 007	7008	Reps 007	7014
Alu 008	7009	Reps 008	7015
Alu 009	7010	Reps 009	7016
Alu 010	7011	Reps 010	7017
Alu 011	7012	Reps 011	7018
Alu 012	7013	Reps 012	7019
Alu 013	7014	Reps 013	7020
Alu 014	7015	Reps 014	7021
Alu 015	7016	Reps 015	7022
Alu 016	7017	Reps 016	7023
Alu 017	7018	Reps 017	7024
Alu 018	7019	Reps 018	7025
Alu 019	7020	Reps 019	7026
Alu 020	7021	Reps 020	7027
Alu 021	7022	Reps 021	7028
Alu 022	7023	Reps 022	7029
Alu 023	7024	Reps 023	7030
Alu 024	7025	Reps 024	7031
Alu 025	7026	Reps 025	7032
Alu 026	7027	Reps 026	7033
Alu 027	7028	Reps 027	7034
Alu 028	7029	Reps 028	7035
Alu 029	7030	Reps 029	7036
Alu 030	7031	Reps 030	7037
Alu 031	7032	Reps 031	7038
Alu 032	7033	Reps 032	7039
Alu 033	7034	Reps 033	7040
Alu 034	7035	Reps 034	7041
Alu 035	7036	Reps 035	7042
Alu 036	7037	Reps 036	7043
Alu 037	7038	Reps 037	7044
Alu 038	7039	Reps 038	7045
Alu 039	7040	Reps 039	7046
Alu 040	7041	Reps 040	7047
Alu 041	7042	Reps 041	7048
Alu 042	7043	Reps 042	7049
Alu 043	7044	Reps 043	7050
Alu 044	7045	Reps 044	7051
Alu 045	7046	Reps 045	7052
Alu 046	7047	Reps 046	7053
Alu 047	7048	Reps 047	7054
Alu 048	7049	Reps 048	7055
Alu 049	7050	Reps 049	7056
Alu 050	7051	Reps 050	7057
Alu 051	7052	Reps 051	7058
Alu 052	7053	Reps 052	7059
Alu 053	7054	Reps 053	7060
Alu 054	7055	Reps 054	7061
Alu 055	7056	Reps 055	7062
Alu 056	7057	Reps 056	7063
Alu 057	7058	Reps 057	7064
Alu 058	7059	Reps 058	7065
Alu 059	7060	Reps 059	7066
Alu 060	7061	Reps 060	7067
Alu 061	7062	Reps 061	7068
Alu 062	7063	Reps 062	7069
Alu 063	7064	Reps 063	7070
Alu 064	7065	Reps 064	7071
Alu 065	7066	Reps 065	7072
Alu 066	7067	Reps 066	7073
Alu 067	7068	Reps 067	7074
Alu 068	7069	Reps 068	7075
Alu 069	7070	Reps 069	7076
Alu 070	7071	Reps 070	7077
Alu 071	7072	Reps 071	7078
Alu 072	7073	Reps 072	7079
Alu 073	7074	Reps 073	7080
Alu 074	7075	Reps 074	7081
Alu 075	7076	Reps 075	7082
Alu 076	7077	Reps 076	7083
Alu 077	7078	Reps 077	7084
Alu 078	7079	Reps 078	7085
Alu 079	7080	Reps 079	7086
Alu 080	7081	Reps 080	7087
Alu 081	7082	Reps 081	7088
Alu 082	7083	Reps 082	7089
Alu 083	7084	Reps 083	7090
Alu 084	7085	Reps 084	7091
Alu 085	7086	Reps 085	7092
Alu 086	7087	Reps 086	7093
Alu 087	7088	Reps 087	7094
Alu 088	7089	Reps 088	7095
Alu 089	7090	Reps 089	7096
Alu 090	7091	Reps 090	7097
Alu 091	7092	Reps 091	7098
Alu 092	7093	Reps 092	7099
Alu 093	7094	Reps 093	7100
Alu 094	7095	Reps 094	7101
Alu 095	7096	Reps 095	7102
Alu 096	7097	Reps 096	7103
Alu 097	7098	Reps 097	7104
Alu 098	7099	Reps 098	7105
Alu 099	7100	Reps 099	7106
Alu 100	7101	Reps 100	7107



■ ■ Introduction to

■ ■ Computer Vision

■ ■

BRDF

- Ron Dror's thesis

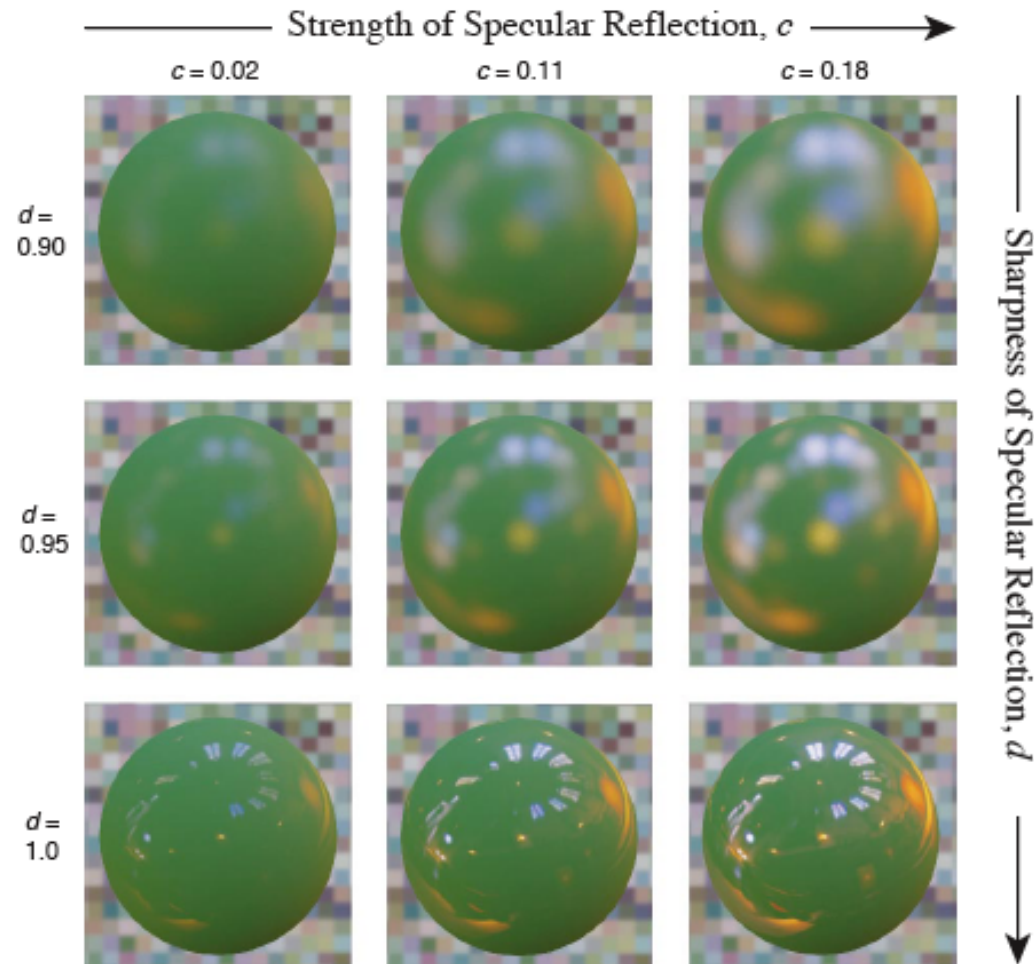
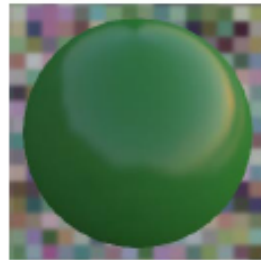
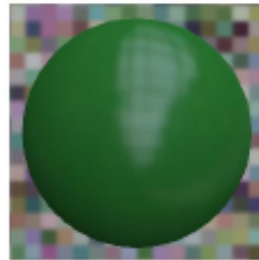


Figure 2.6. Grid showing range of reflectance properties used in the experiments for a particular real-world illumination map. All the spheres shown have an identical diffuse component. In Pellacini's reparameterization of the Ward model, the specular component depends on the c and d parameters. The strength of specular reflection, c , increases with ρ_s , while the sharpness of specular reflection, d , decreases with α . The images were rendered in *Radiance*, using the techniques described in Appendix B.

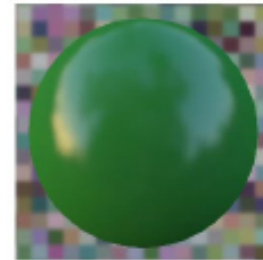
Real World Illuminations



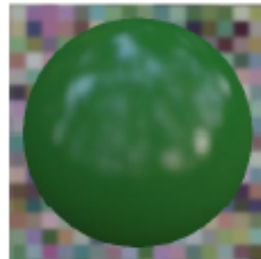
(a) "Beach"



(b) "Building"



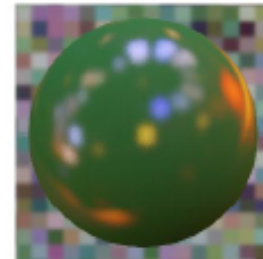
(c) "Campus"



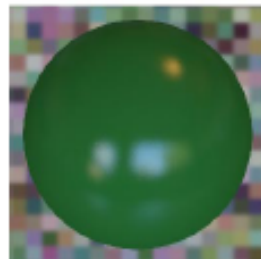
(d) "Eucalyptus"



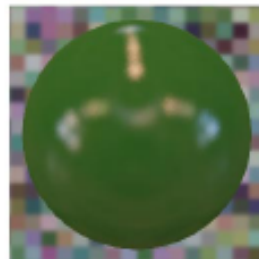
(e) "Galileo"



(f) "Grace"



(g) "Kitchen"

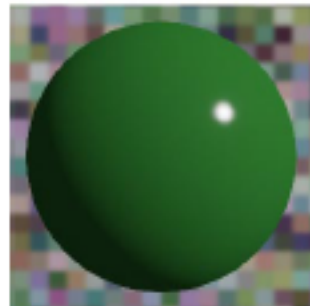


(h) "St. Peter's"

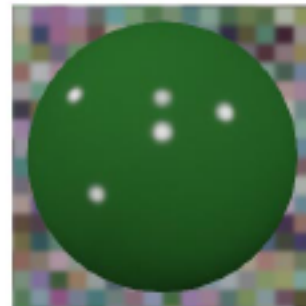


(i) "Uffizi"

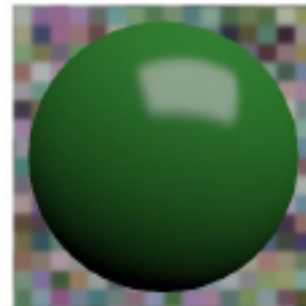
Artificial Illuminations



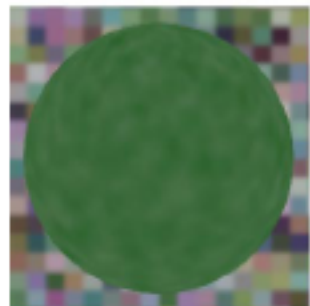
(a) Point source



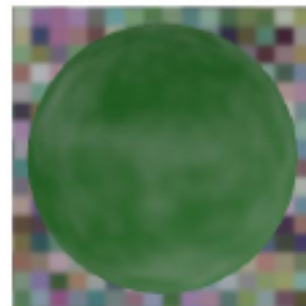
(b) Multiple points



(c) Extended



(d) White noise



(e) Pink noise



(a)



(b)

Figure 2.9. (a) A shiny sphere rendered under illumination by a point light source. (b) The same sphere rendered under photographically-acquired real-world illumination. Humans perceive reflectance properties more accurately in (b).

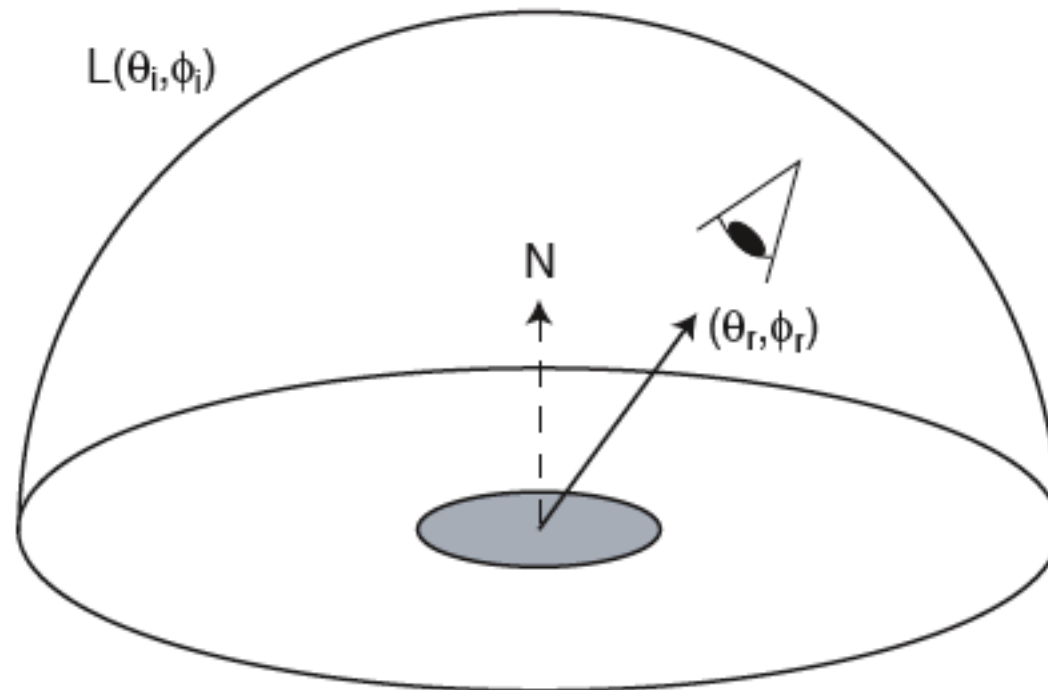


Figure 3.1. A viewer observes a surface patch with normal N from direction (θ_r, ϕ_r) . $L(\theta_i, \phi_i)$ represents radiance of illumination from direction (θ_i, ϕ_i) . The coordinate system is such that N points in direction $(0, 0)$.

$$B(\theta_r, \phi_r) = \int_{\phi_i=0}^{2\pi} \int_{\theta_i=0}^{\pi/2} L(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r) \cos \theta_i \sin \theta_i d\theta_i d\phi_i,$$

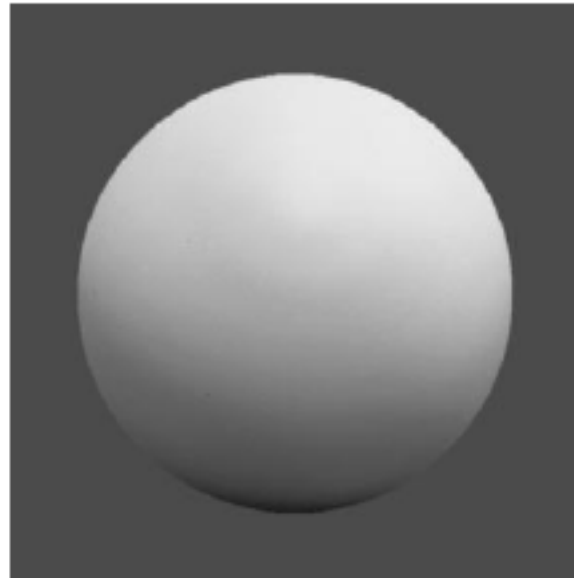


Figure 3.6. A photograph of a matte sphere, shown against a uniform gray background. This image could also be produced by a chrome sphere under appropriate illumination, but that scenario is highly unlikely.

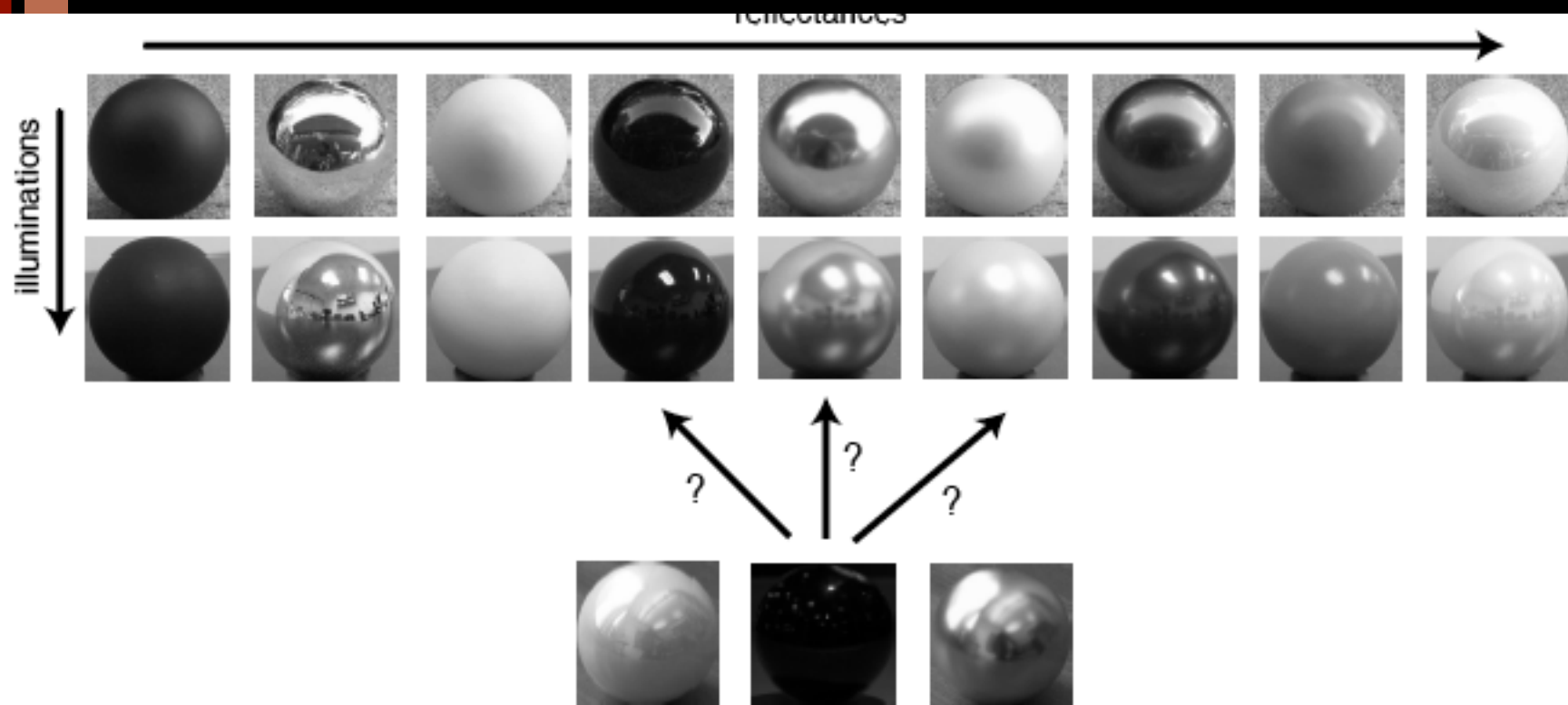
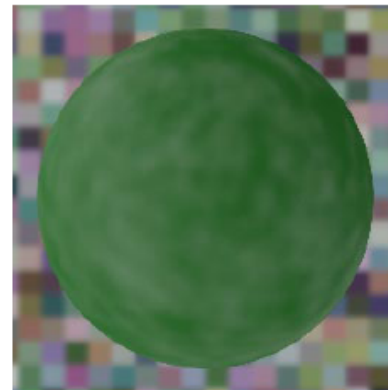


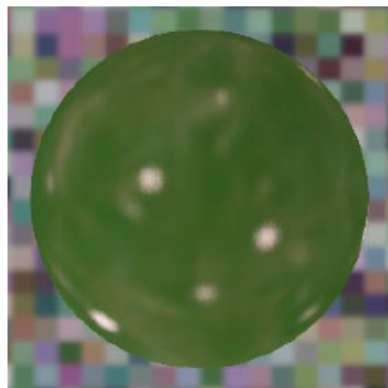
Figure 3.7. The problem addressed by a classifier of Chapter 6, illustrated using a database of photographs. Each of nine spheres was photographed under seven different illuminations. We trained a nine-way classifier using the images corresponding to several illuminations, and then used it to classify individual images under novel illuminations.



(a) Original



(b) $1/f^2$ power spectrum

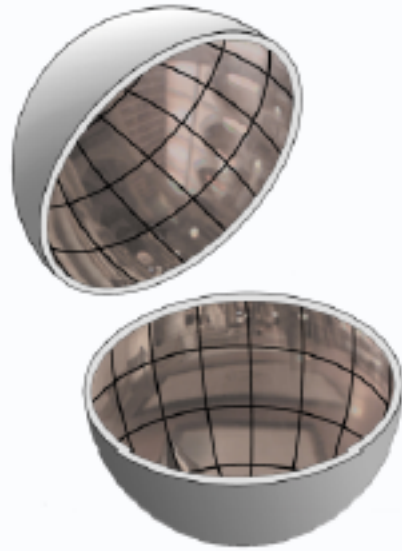


(c) Heeger and Bergen texture



(d) Portilla and Simoncelli texture

Figure 4.14. Spheres of identical reflectance properties rendered under a photographically-acquired illumination map (a) and three synthetic illumination maps (b-d). The illumination in (b) is Gaussian noise with a $1/f^2$ power spectrum. The illumination in (c) was synthesized with the procedure of Heeger and Bergen [43] to match the pixel histogram and marginal wavelet histograms of the illumination in (a). The illumination in (d) was synthesized using the technique of Portilla and Simoncelli, which also enforces conditions on the joint wavelet histograms. The illumination map of (a) is due to Debevec [24].



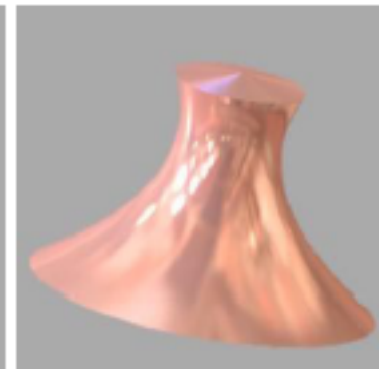
(a)



(b)



(c)



(d)

Figure 5.2. (a) A photographically-acquired illumination map, illustrated on the inside of a spherical shell. The illumination map is identical to that of Figure 4.1d. (b-d) Three surfaces of different geometry and reflectance rendered under this illumination map using the methods of Appendix B.

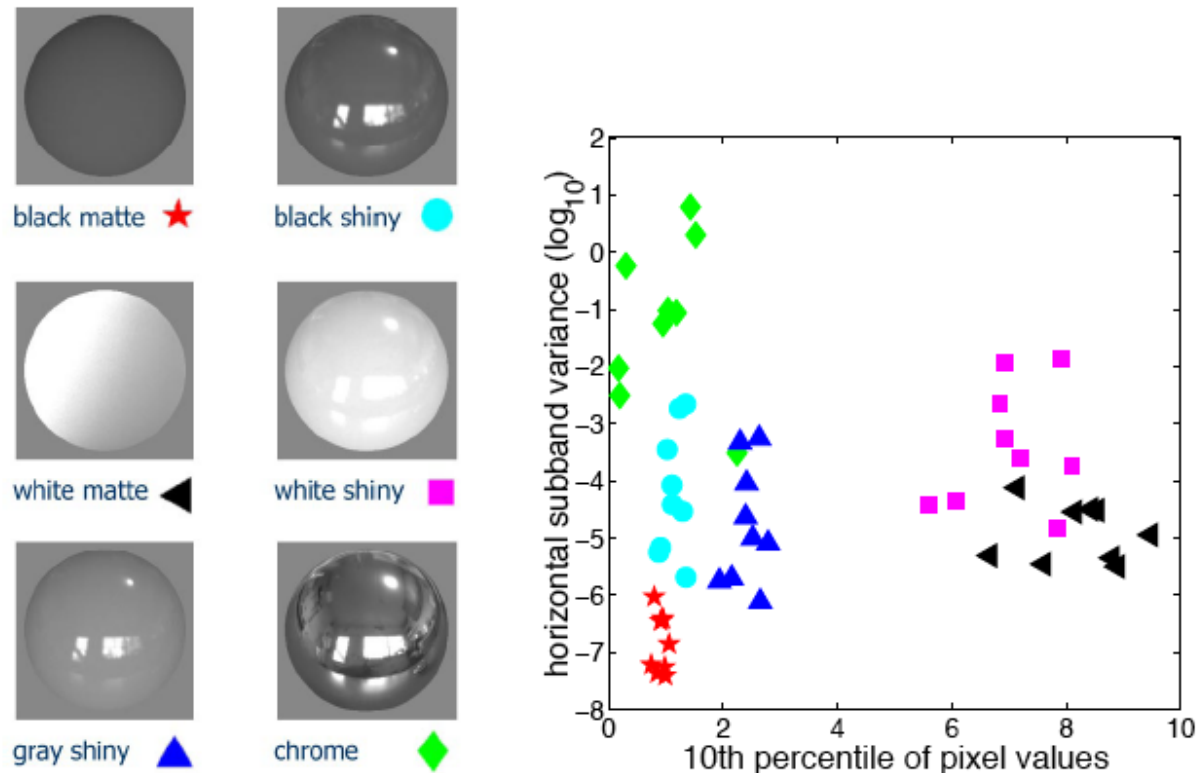


Figure 5.11. At left, synthetic spheres of 6 different reflectances, each rendered under one of Debevec's illumination maps. Ward model parameters are as follows: black matte, $\rho_d = .1$, $\rho_s = 0$; black shiny, $\rho_d = .1$, $\rho_s = .1$, $\alpha = .01$; white matte, $\rho_d = .9$, $\rho_s = 0$; white shiny, $\rho_d = .7$, $\rho_s = .25$, $\alpha = .01$; chrome, $\rho_d = 0$, $\rho_s = .75$, $\alpha = 0$; gray shiny, $\rho_d = .25$, $\rho_s = .05$, $\alpha = .01$. We rendered each sphere under the nine photographically-acquired illuminations depicted in Figure 2.7 and plotted a symbol corresponding to each in the two-dimensional feature space at right. The horizontal axis represents the 10th percentile of pixel intensity, while the vertical axis is the log variance of horizontally-oriented QMF wavelet coefficients at the second-finest scale, computed after geometrically distorting the original image as described in Section 6.1.2.

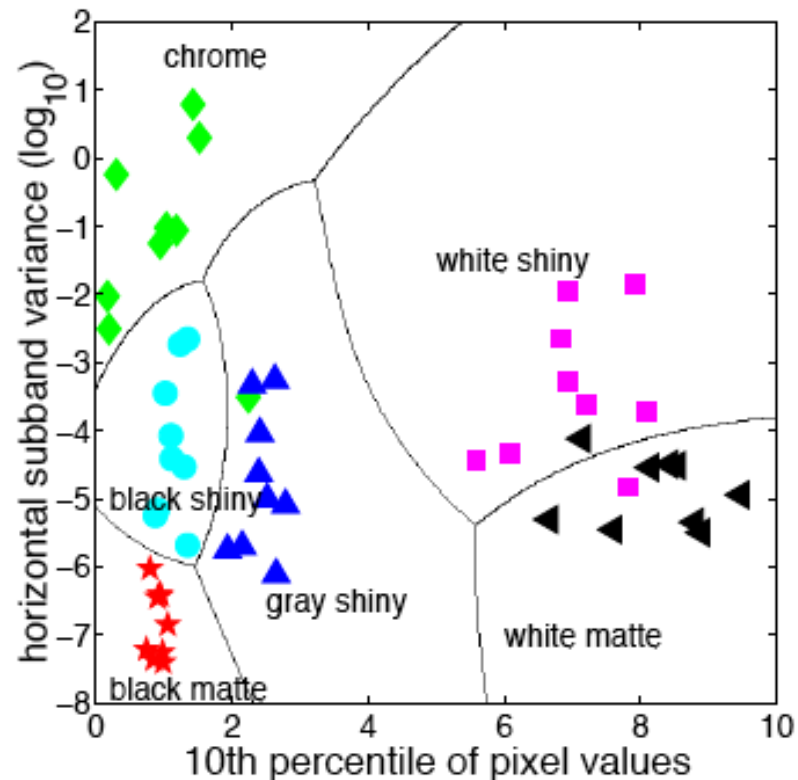


Figure 5.12. The curved lines separate regions assigned to different reflectances by a simple classifier based on two image features. The training examples are the images described in Figure 5.11. The classifier is a one-versus-all support vector machine, described in Section 6.1.1. Using additional image features improves classifier performance.

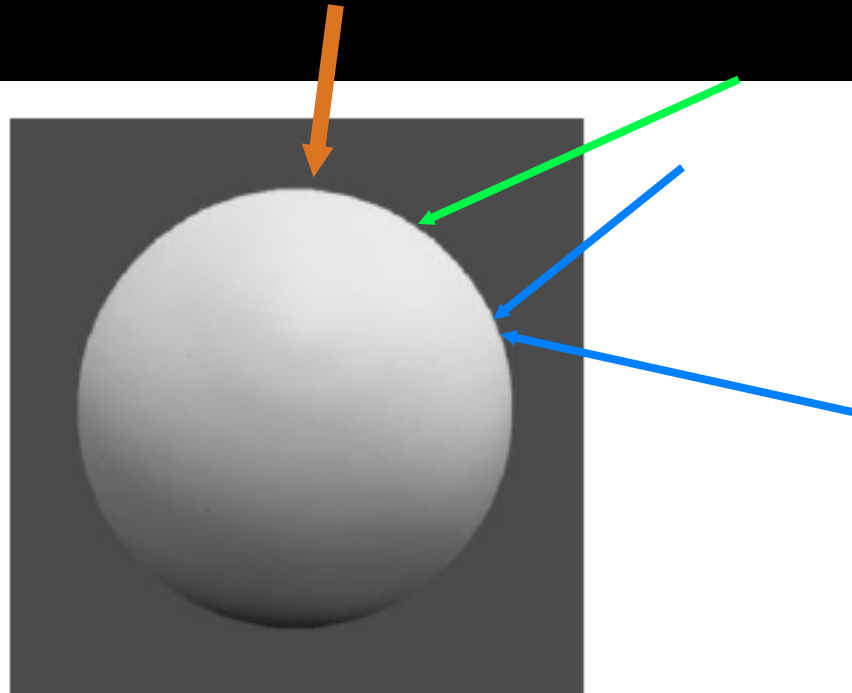


Figure 3.6. A photograph of a matte sphere, shown against a uniform gray background.

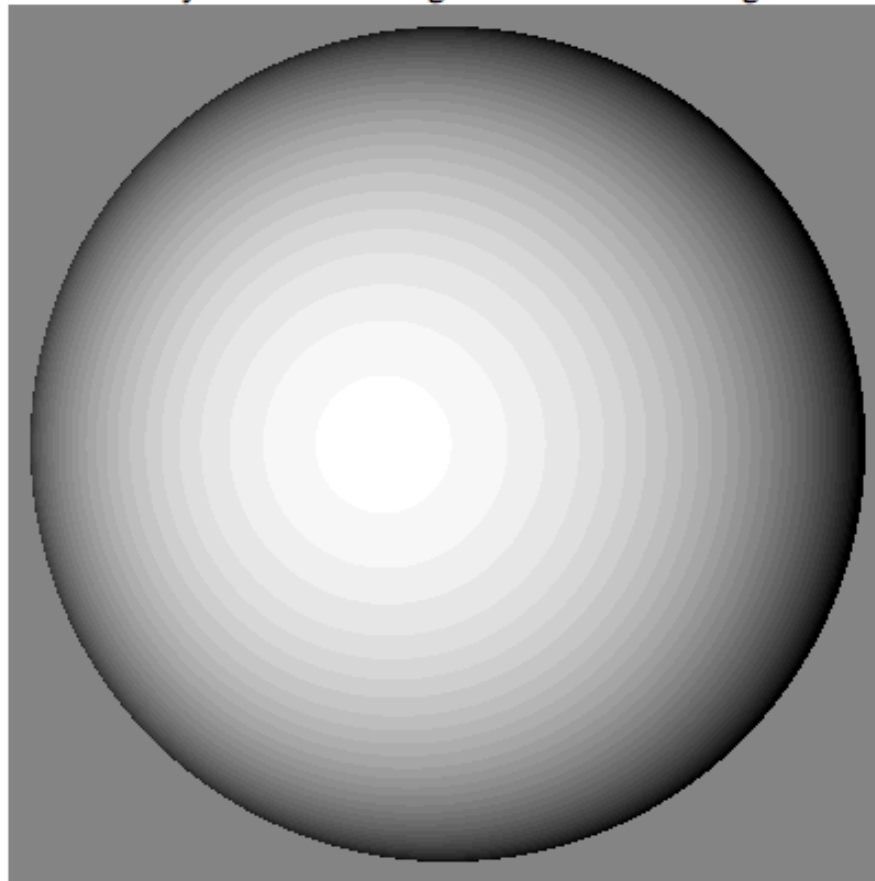
For Lambertian surface:

Viewer direction is irrelevant

Lighting direction is *very relevant*

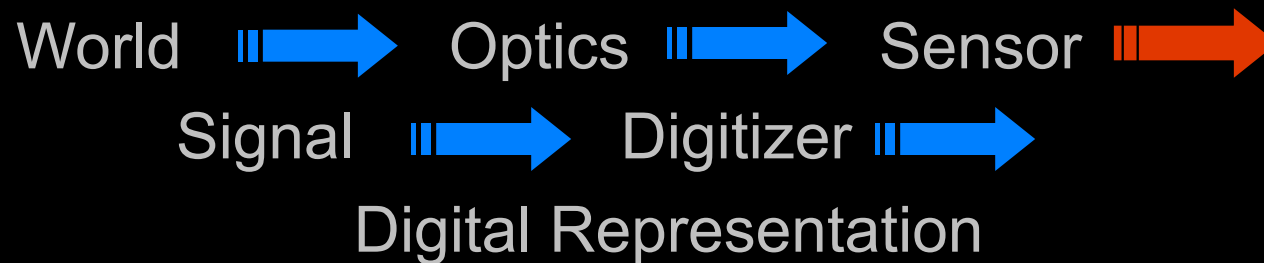
Lambertian Sphere

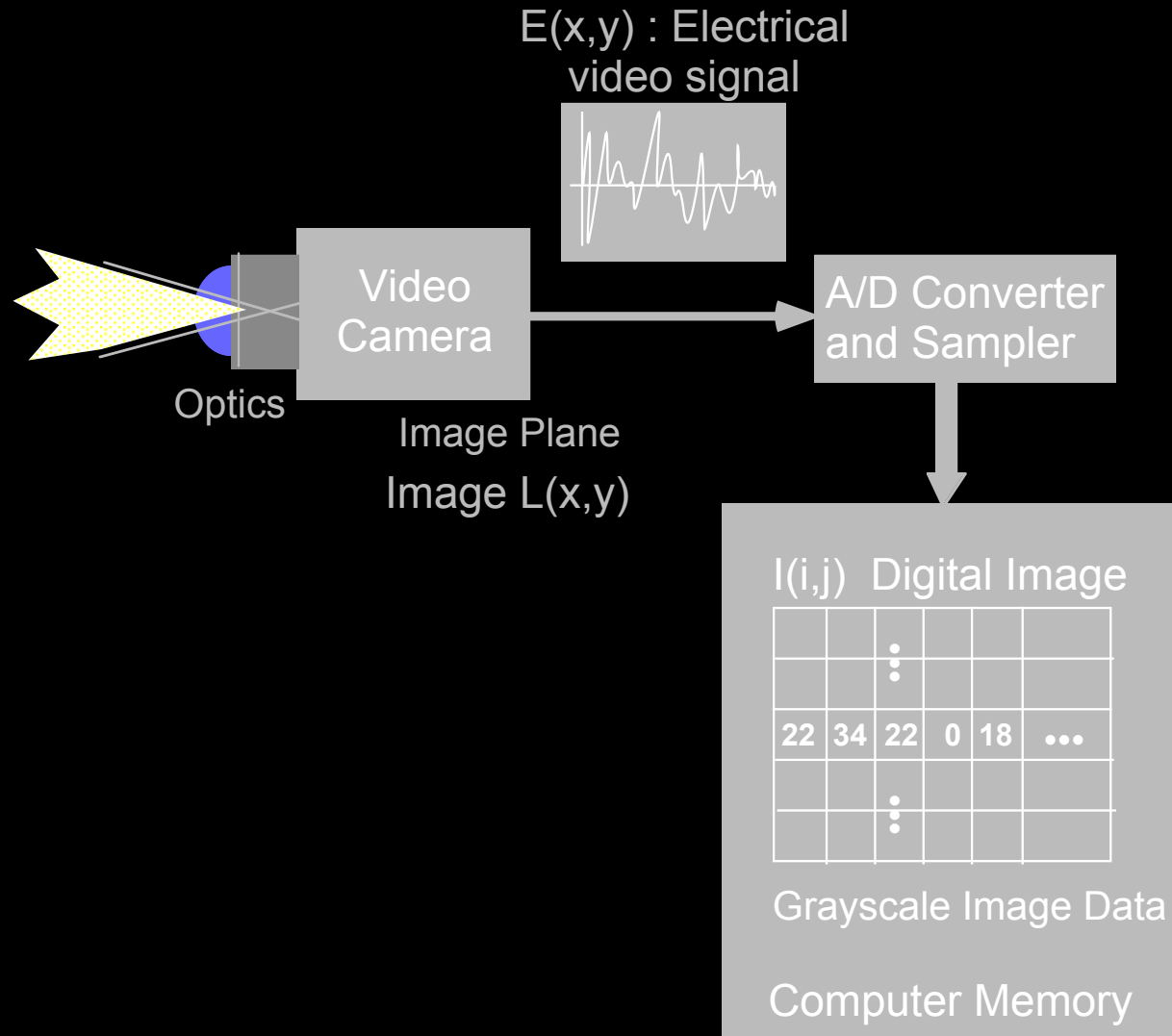
Orthogonal Projection,
Infinitely Distant Point Light from -90 to +90 degrees



- Photometry:

Concerned with mechanisms for converting light energy into electrical energy.

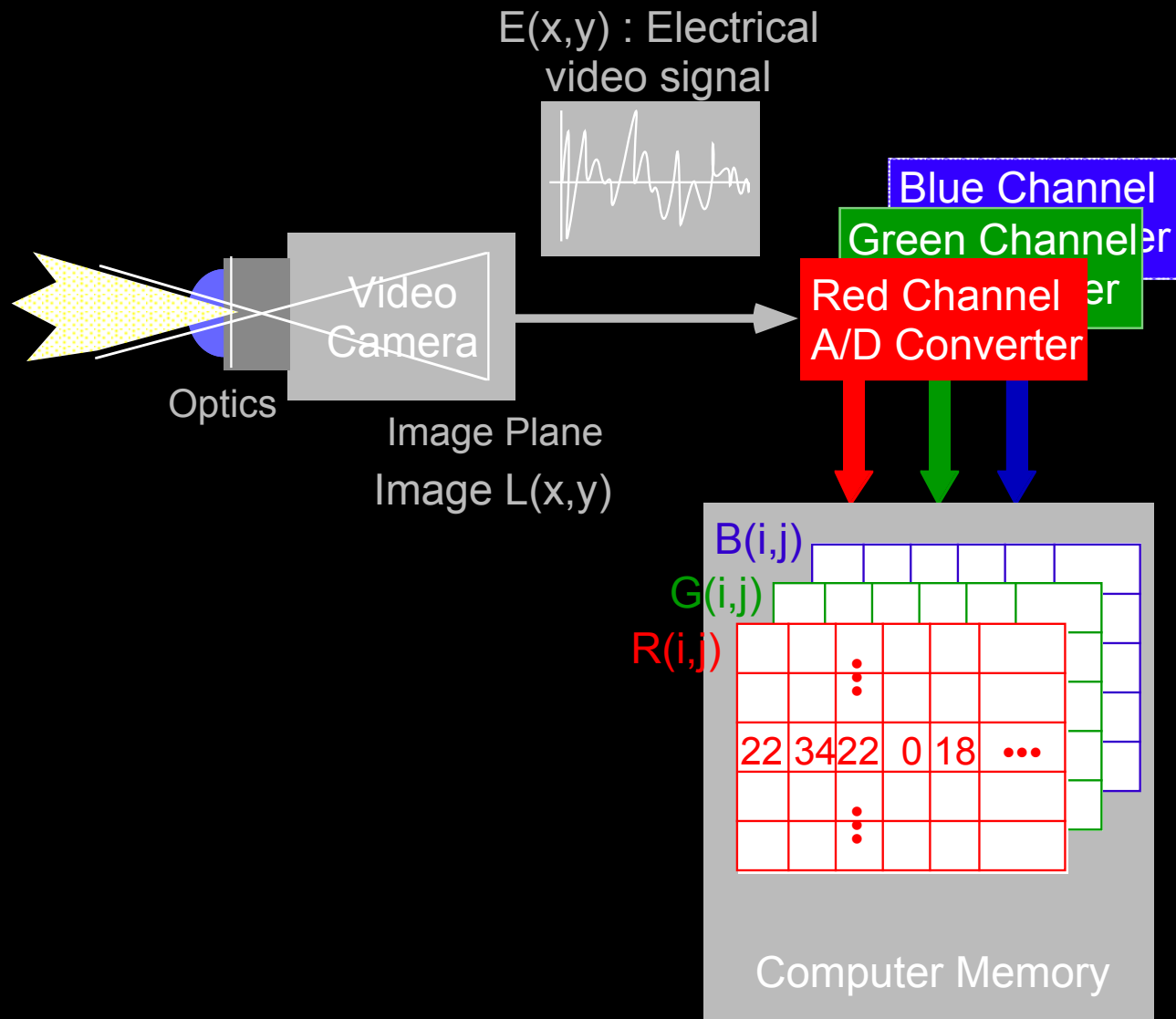




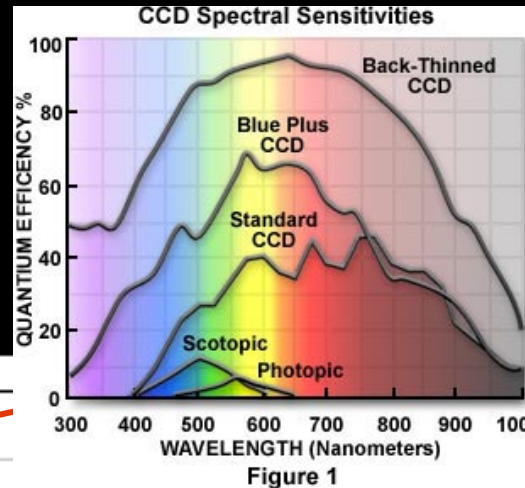
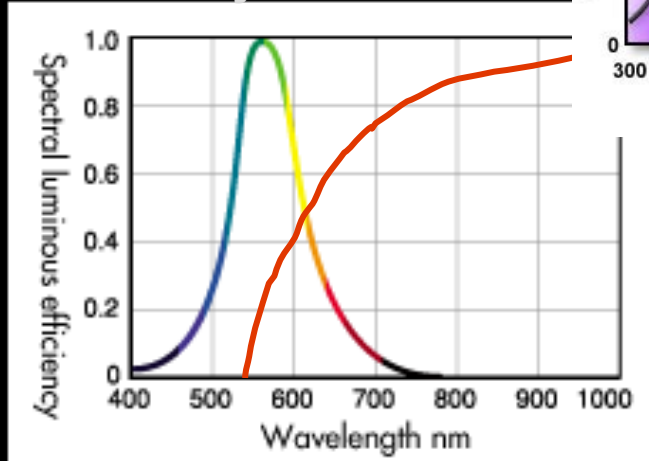
Introduction to

Computer Vision

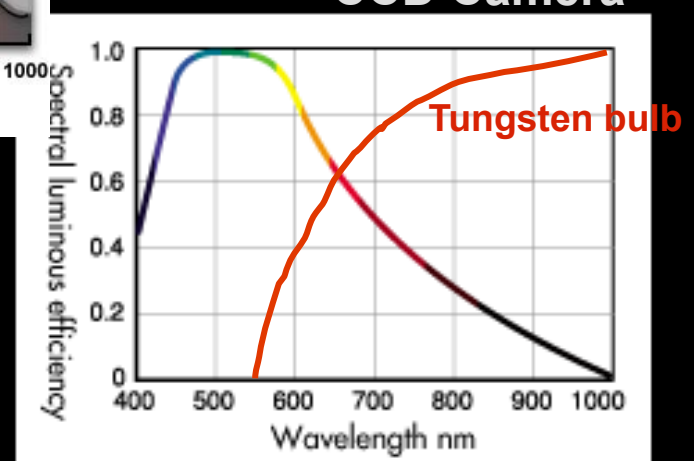
Color Video System



Human Eye



CCD Camera



- Figure 1 shows relative efficiency of conversion for the eye (scotopic and photopic curves) and several types of CCD cameras. Note the CCD cameras are much more sensitive than the eye.
- Note the enhanced sensitivity of the CCD in the Infrared and Ultraviolet (bottom two figures)
- Both figures also show a handdrawn sketch of the spectrum of a tungsten light bulb

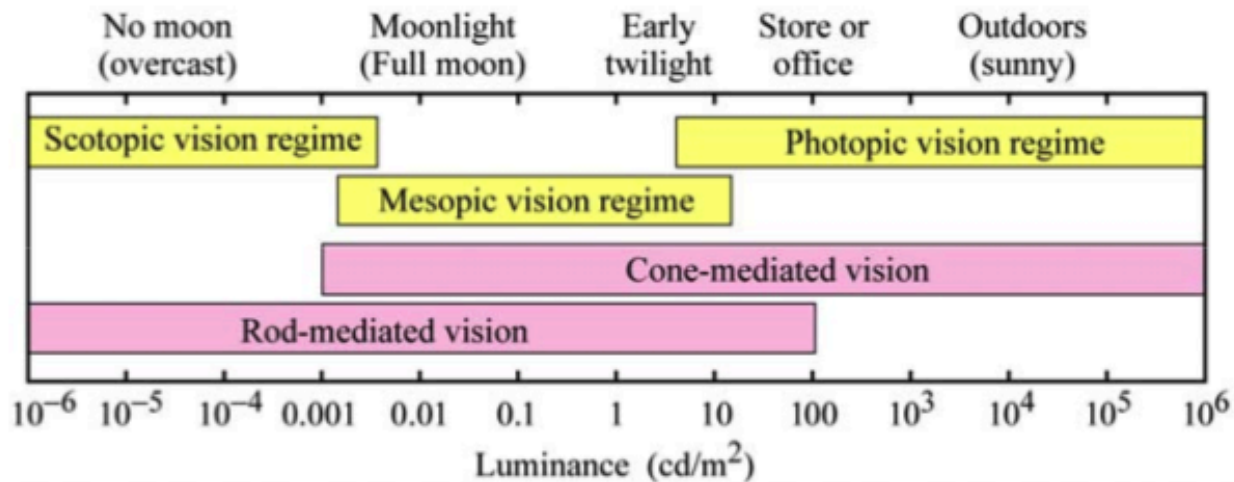


Fig. 16.2. Approximate ranges of vision regimes and receptor regimes (after Osram Sylvania, 2000).

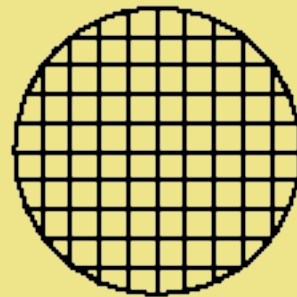
- In general, $V(x,y) = k E(x,y)^g$ where
 - k is a constant
 - g is a parameter of the type of sensor
 - $g=1$ (approximately) for a CCD camera
 - $g=.65$ for an old type vidicon camera
- Factors influencing performance:
 - Optical distortion: pincushion, barrel, non-linearities
 - Sensor dynamic range (30:1 CCD, 200:1 vidicon)
 - Sensor Shading (nonuniform responses from different locations)
- **TV Camera pros: cheap, portable, small size**
- **TV Camera cons: poor signal to noise, limited dynamic range, fixed array size with small image (getting better)**

- Optical Distortion: pincushion, barrel, non-linearities
- Sensor Dynamic Range: (30:1 for a CCD, 200:1 Vidicon)
- Sensor Blooming: spot size proportional to input intensity
- Sensor Shading: (non-uniform response at outer edges of image)
- Dead CCD cells

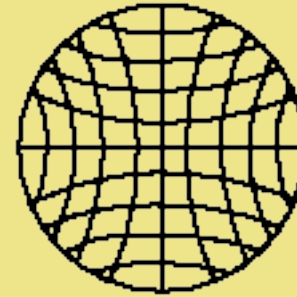
There is no “universal sensor”.
Sensors must be selected/tuned for
a particular domain and application.

- In an ideal optical system, all rays of light from a point in the object plane would converge to the same point in the image plane, forming a clear image.
- The lens defects which cause different rays to converge to different points are called aberrations.
 - Distortion: barrel, pincushion
 - Curvature of field
 - Chromatic aberration
 - Spherical aberration
 - Coma
 - Astigmatism

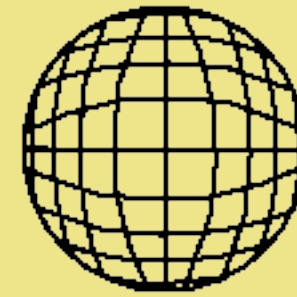
■ Distortion



Undistorted
Image

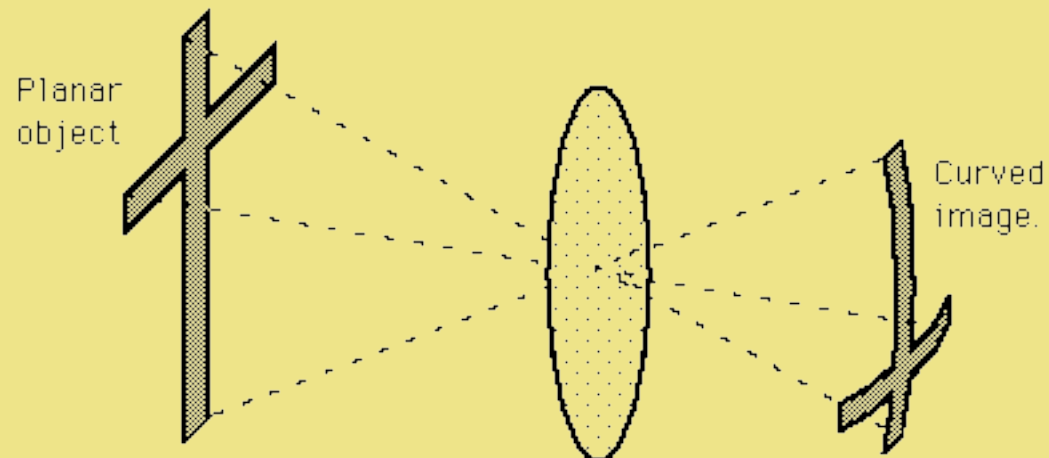


Pincushion
Distortion

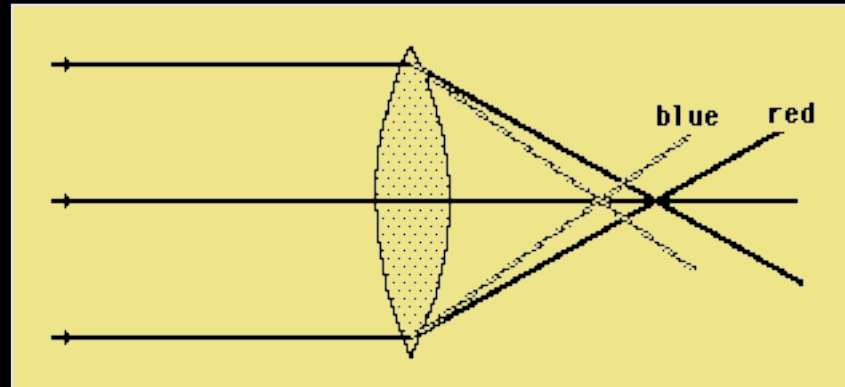


Barrel
Distortion

■ Curved Field

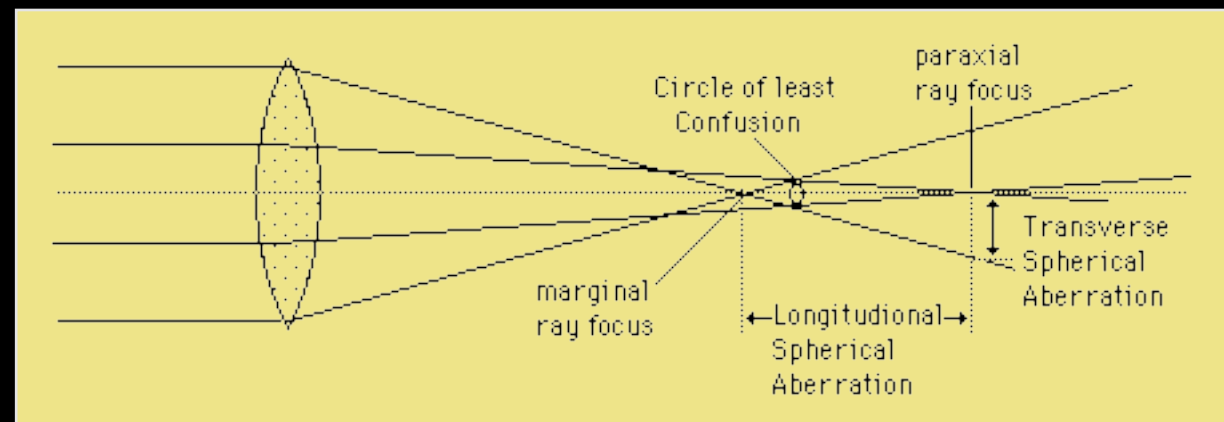


■ Chromatic Aberration



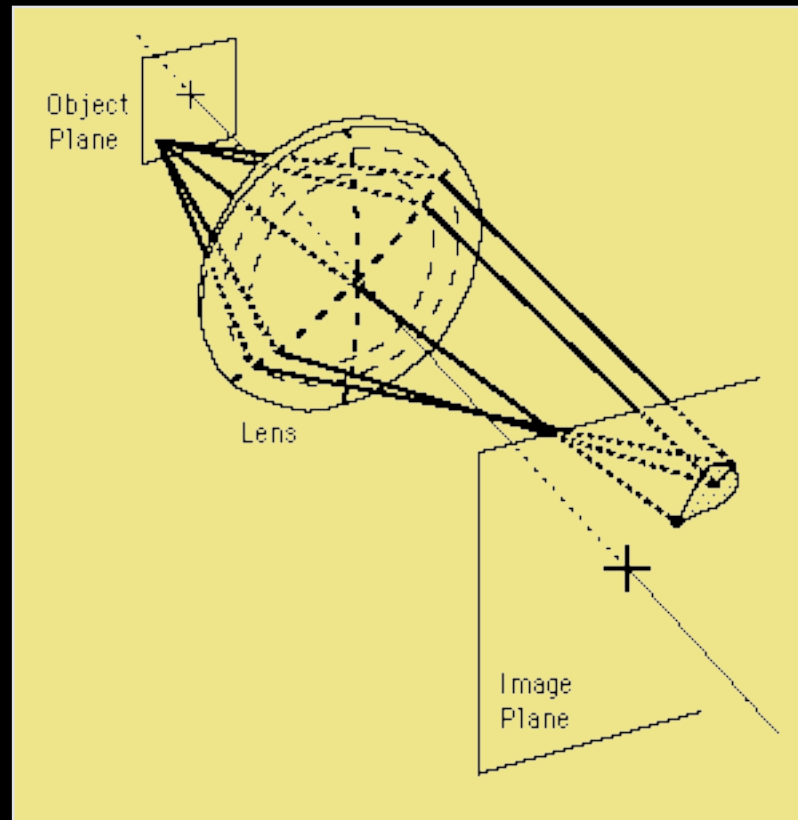
- Focal Length of lens depends on refraction and
- The index of refraction for blue light (short wavelengths) is larger than that of red light (long wavelengths).
- Therefore, a lens will not focus different colors in exactly the same place
- The amount of chromatic aberration depends on the dispersion (change of index of refraction with wavelength) of the glass.

Spherical Aberration



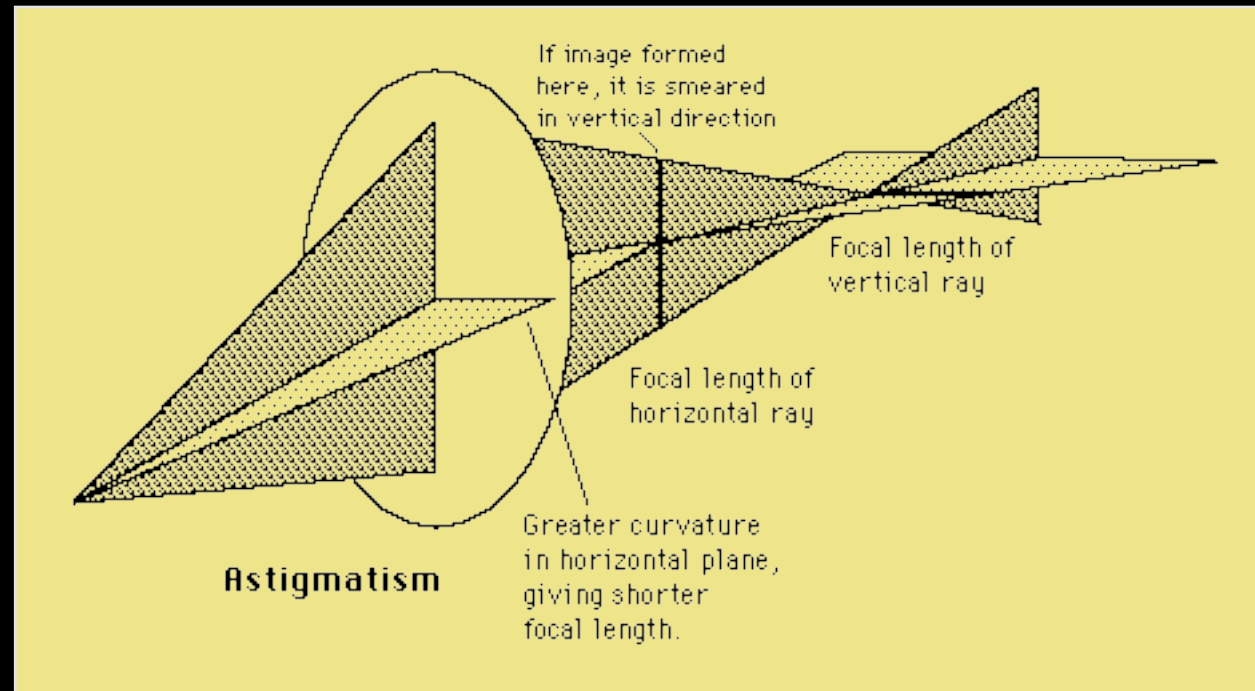
- Rays which are parallel to the optic axis but at different distances from the optic axis fail to converge to the same point.

■ Coma



- Rays from an off-axis point of light in the object plane create a trailing "comet-like" blur directed away from the optic axis
- Becomes worse the further away from the central axis the point is

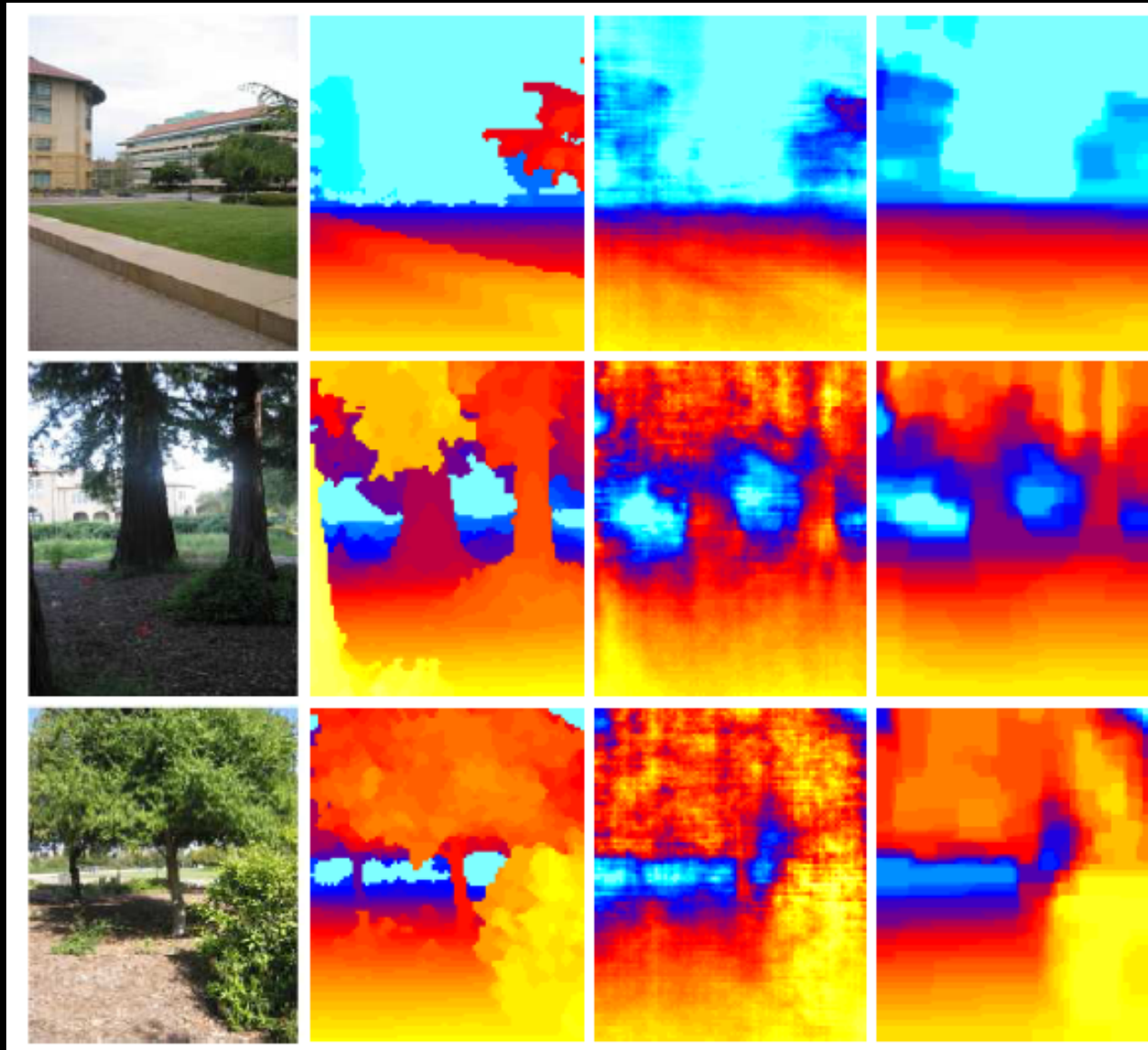
■ Astigmatism

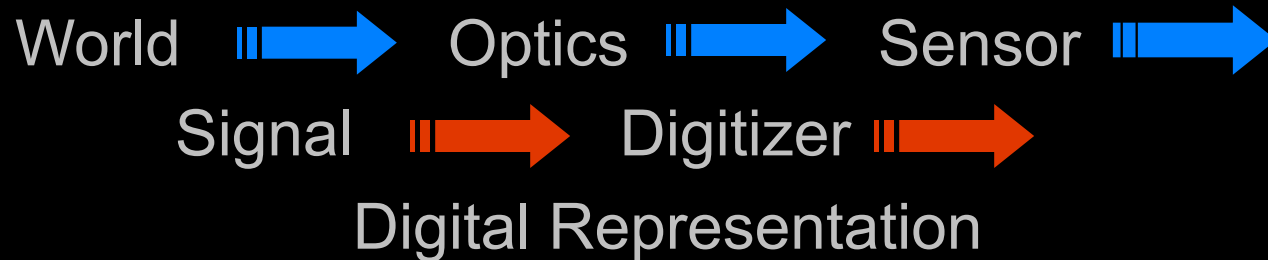


- Results from different lens curvatures in different planes.

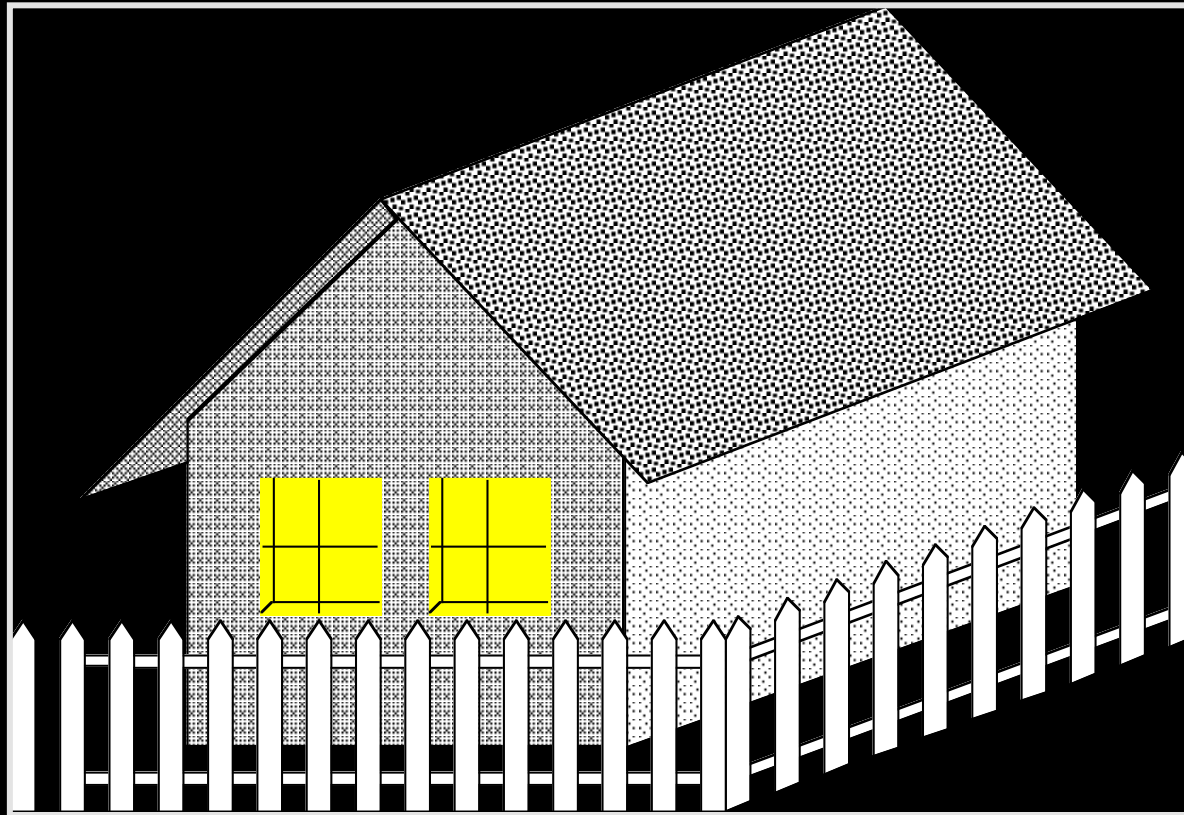
- Visible Light/Heat
 - Camera/Film combination
 - Digital Camera
 - Video Cameras
 - FLIR (Forward Looking Infrared)
- Range Sensors
 - Radar (active sensing)
 - sonar
 - laser
 - Triangulation
 - stereo
 - structured light
 - – striped, patterned
 - Moire
 - Holographic Interferometry
 - Lens Focus
 - Fresnel Diffraction
- Others
- Almost anything which produces a 2d signal that is related to the scene can be used as a sensor



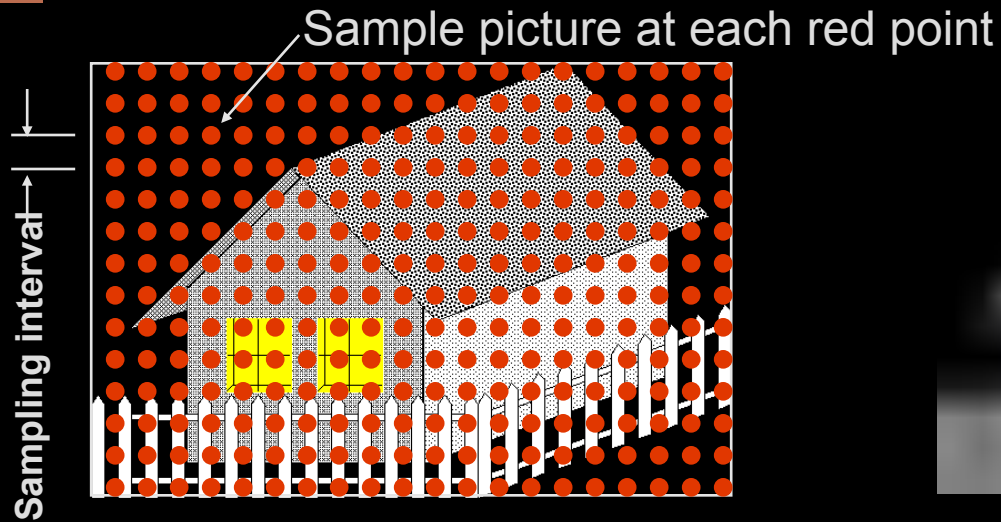




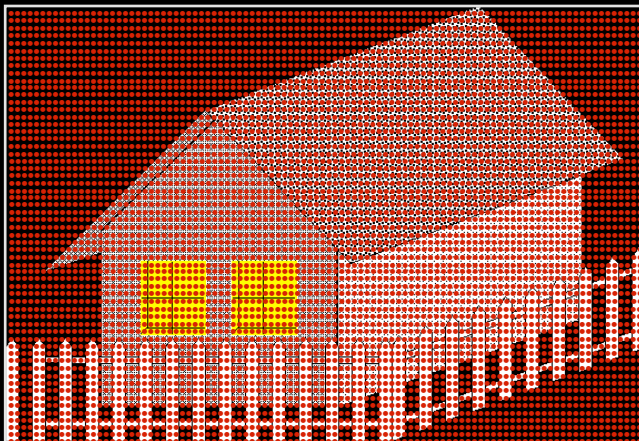
- Digitization: conversion of the continuous (in space and value) electrical signal into a digital signal (digital image)
- Three decisions must be made:
 - Spatial resolution (how many samples to take)
 - Signal resolution (dynamic range of values)
 - Tessellation pattern (how to 'cover' the image with sample points)



- Let's digitize this image
 - Assume a square sampling pattern
 - Vary density of sampling grid




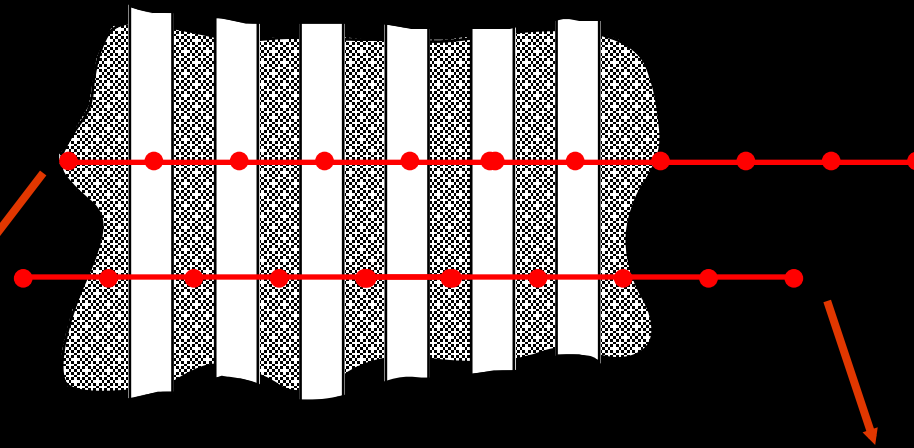
Coarse Sampling: 20 points per row by 14 rows



Finer Sampling: 100 points per row by 68 rows

- Look in vicinity of the picket fence:

Sampling Interval: 



100	100	100	100	100	100
100	100	100	100	100	100
100	100	100	100	100	100
100	100	100	100	100	100

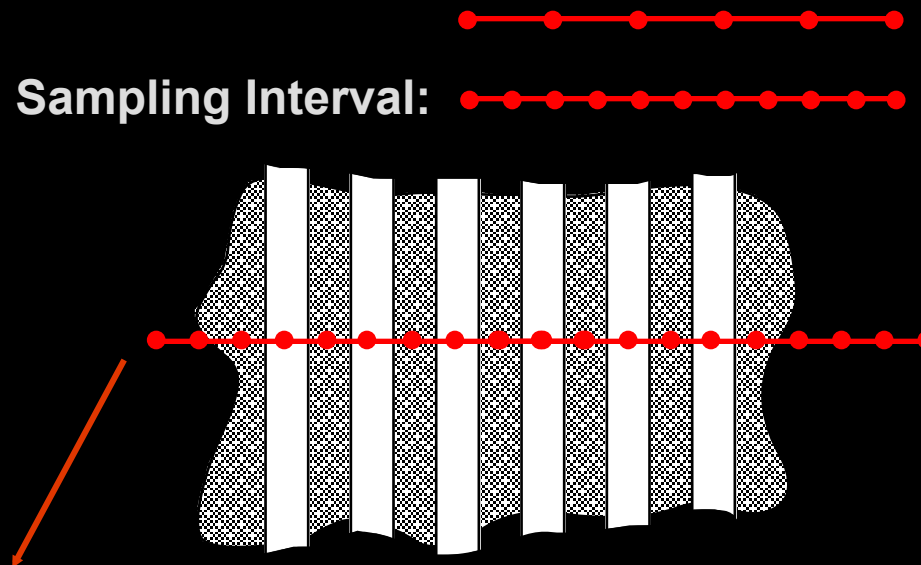
White Image!

**NO EVIDENCE
OF THE FENCE!**

40	40	40	40	40	40
40	40	40	40	40	40
40	40	40	40	40	40
40	40	40	40	40	40

Dark Gray Image!

- Look in vicinity of picket fence:

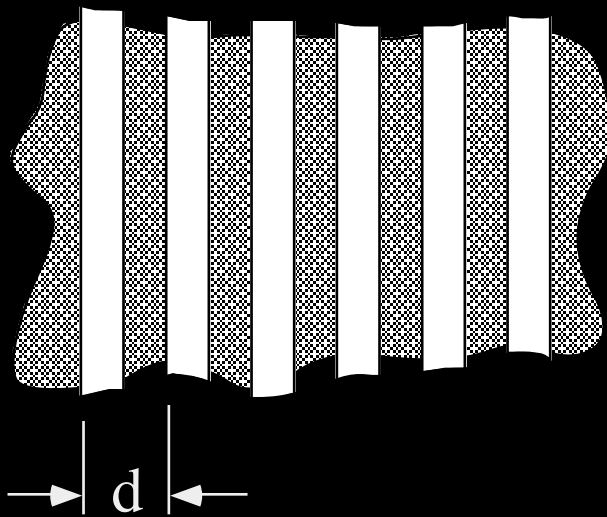


40	100	40	100	40
40	100	40	100	40
40	100	40	100	40
40	100	40	100	40

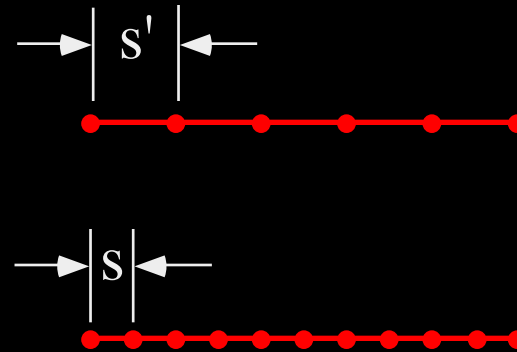
What's the difference between this attempt and the last one?

Now we've got a fence!

- Consider the repetitive structure of the fence:



Sampling Intervals



Case 1: $s' = d$

The sampling interval is equal to the size of the repetitive structure

NO FENCE

Case 2: $s = d/2$

The sampling interval is one-half the size of the repetitive structure

FENCE

- IF: the size of the smallest structure to be preserved is d
- THEN: the sampling interval must be smaller than $d/2$

- Can be shown to be true mathematically
- Repetitive structure has a certain frequency ('pickets/foot')
 - To preserve structure must sample at **greater** than twice the frequency
 - Holds for images, audio CDs, digital television....
- Leads naturally to Fourier Analysis

- Fine near the center of the retina (fovea)
- Coarse at the edges

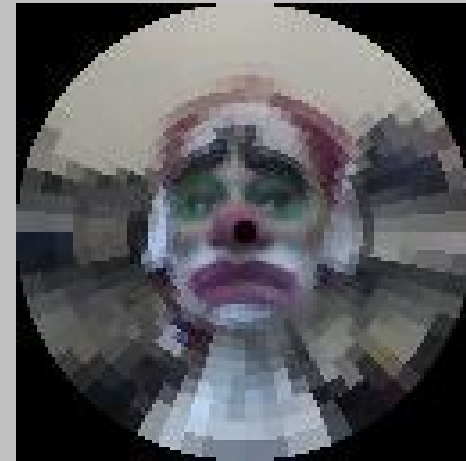
- Strategy:
 - Detect points of interest with low resolution sampling
 - “Foveate” to point of interest and use high resolution sampling.

Introduction to

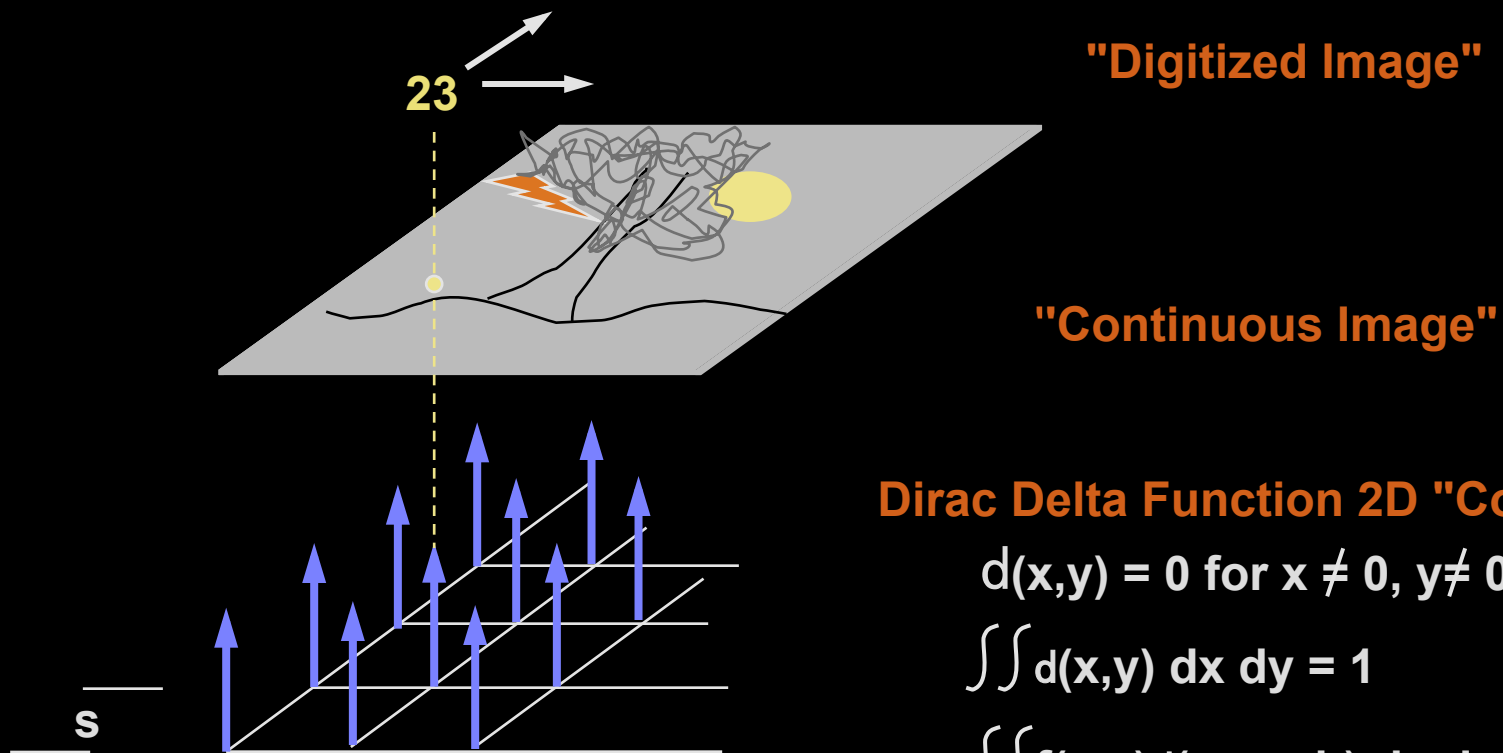
Computer Vision

Human Eye Sampling

Cartesian image ----- Log-Polar representation ----- Retinal representation



Rough Idea: Ideal Case



Dirac Delta Function 2D "Comb"

$$d(x,y) = 0 \text{ for } x \neq 0, y \neq 0$$

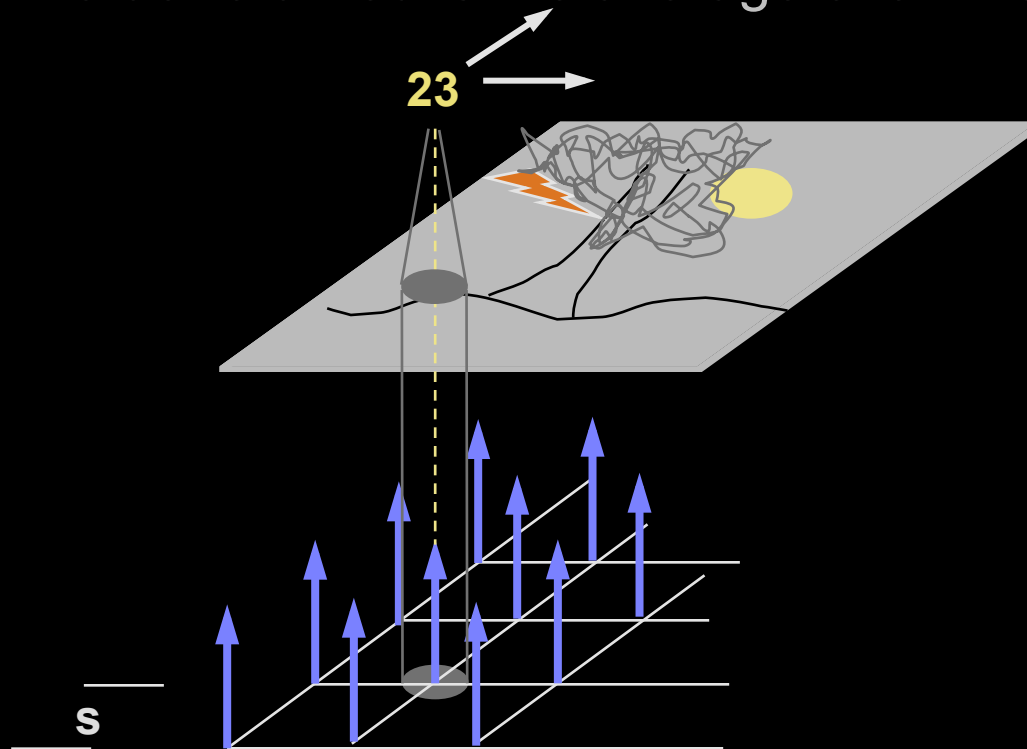
$$\iint d(x,y) dx dy = 1$$

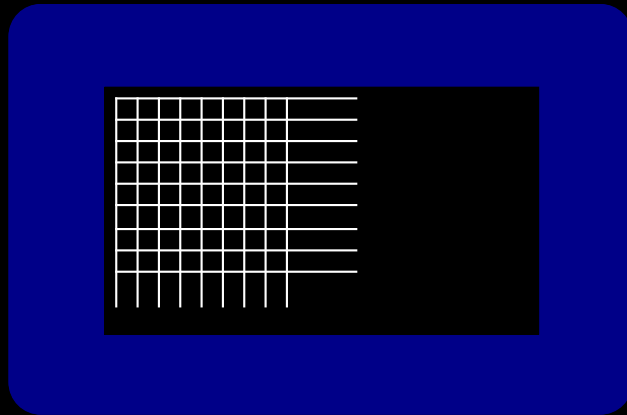
$$\iint f(x,y)d(x-a,y-b) dx dy = f(a,b)$$

$$d(x-ns,y-ns) \text{ for } n = 1 \dots 32 \text{ (e.g.)}$$

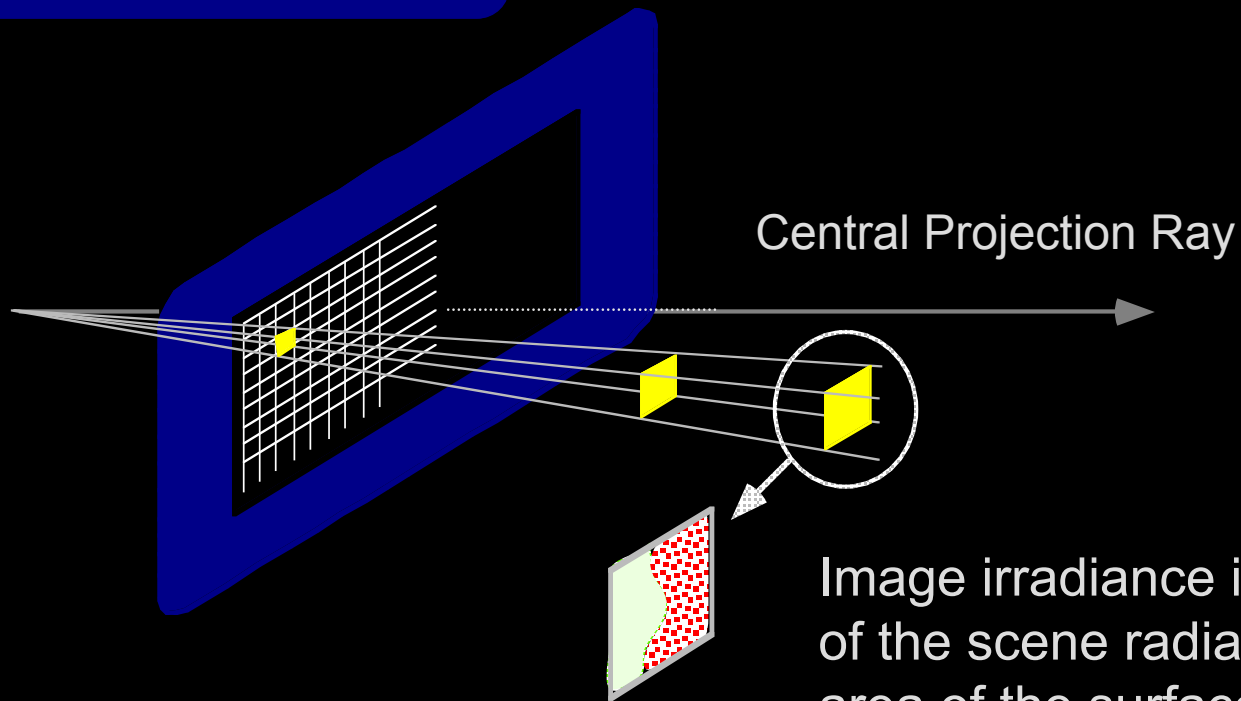
■ Rough Idea: Actual Case

- Can't realize an ideal point function in real equipment
- "Delta function" equivalent has an area
- Value returned is the average over this area





Digitized 35mm Slide or Film



Central Projection Ray

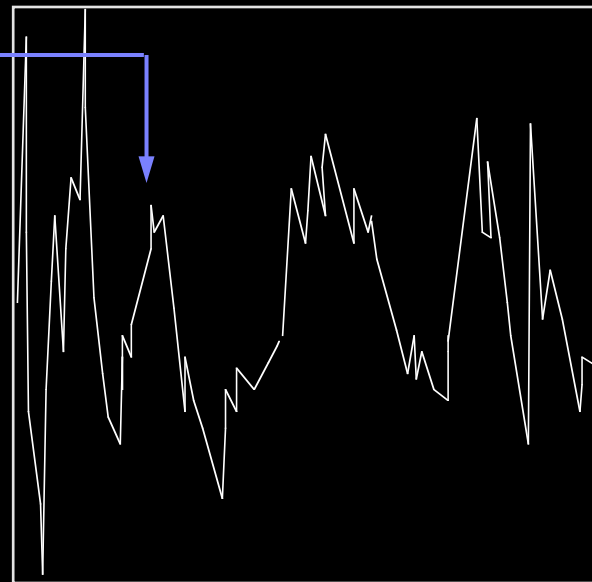
Image irradiance is the average of the scene radiance over the area of the surface intersecting the solid angle!



- Goal: determine a mapping from a continuous signal (e.g. analog video signal) to one of K discrete (digital) levels.

$I(x,y) = .1583$ volts

= ???? Digital
value

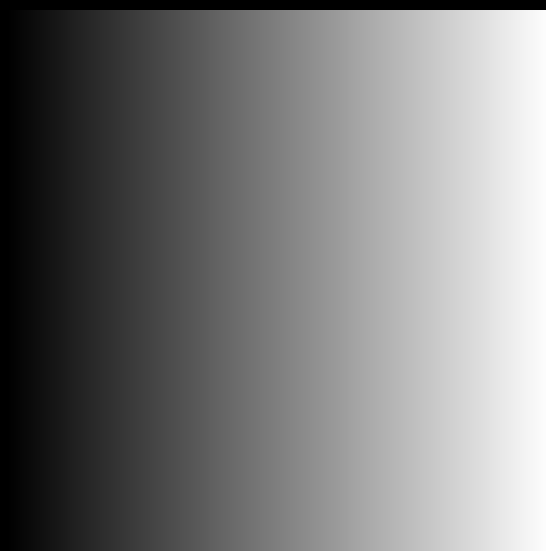


- $I(x,y)$ = continuous signal: $0 \leq I \leq M$
- Want to quantize to K values $0, 1, \dots, K-1$
- K usually chosen to be a power of 2:

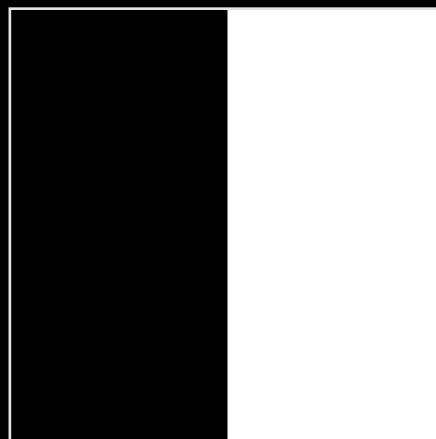
K: #Levels	#Bits
2	1
4	2
8	3
16	4
32	5
64	6
128	7
256	8

- Mapping from input signal to output signal is to be determined.
- Several types of mappings: uniform, logarithmic, etc.

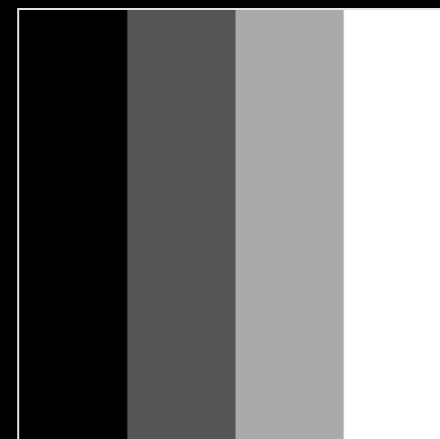
Original



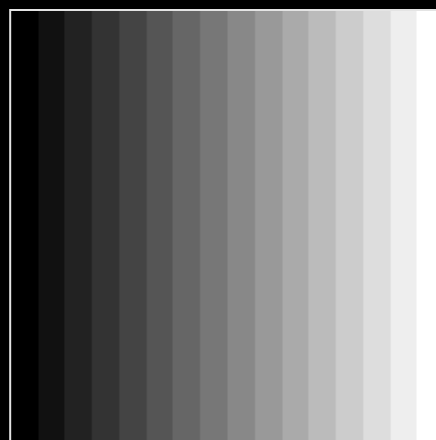
Linear Ramp



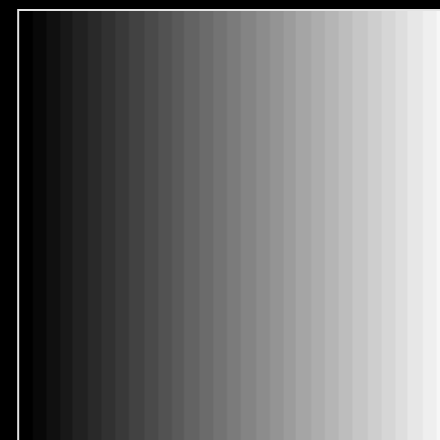
K=2



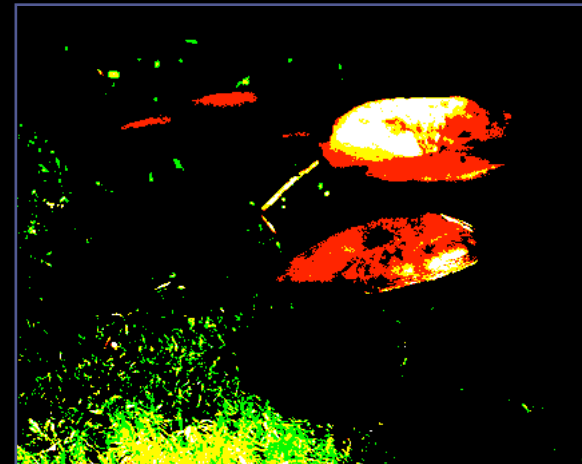
K=4



K=16



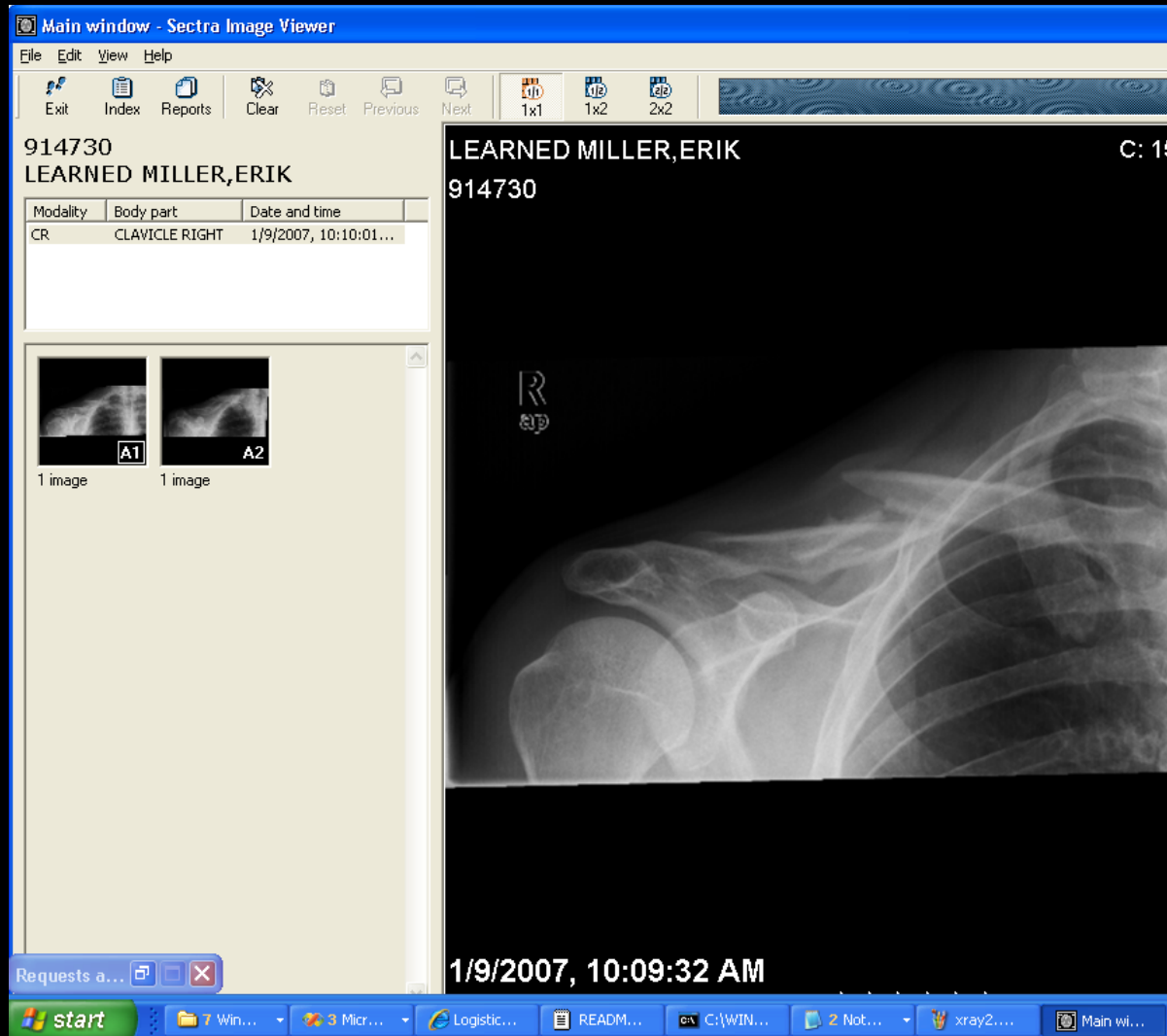
K=32



K=2 (each color)



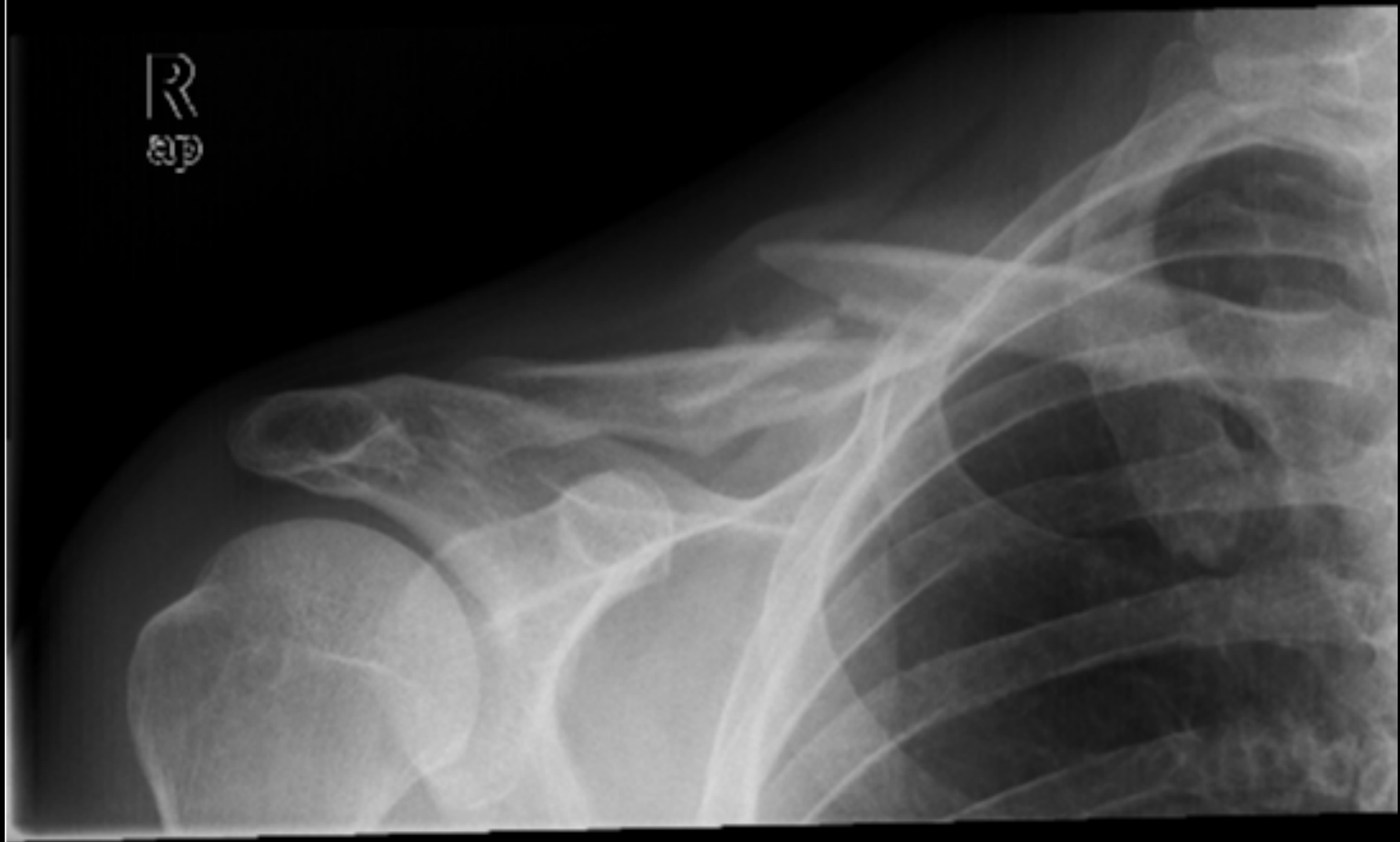
K=4 (each color)



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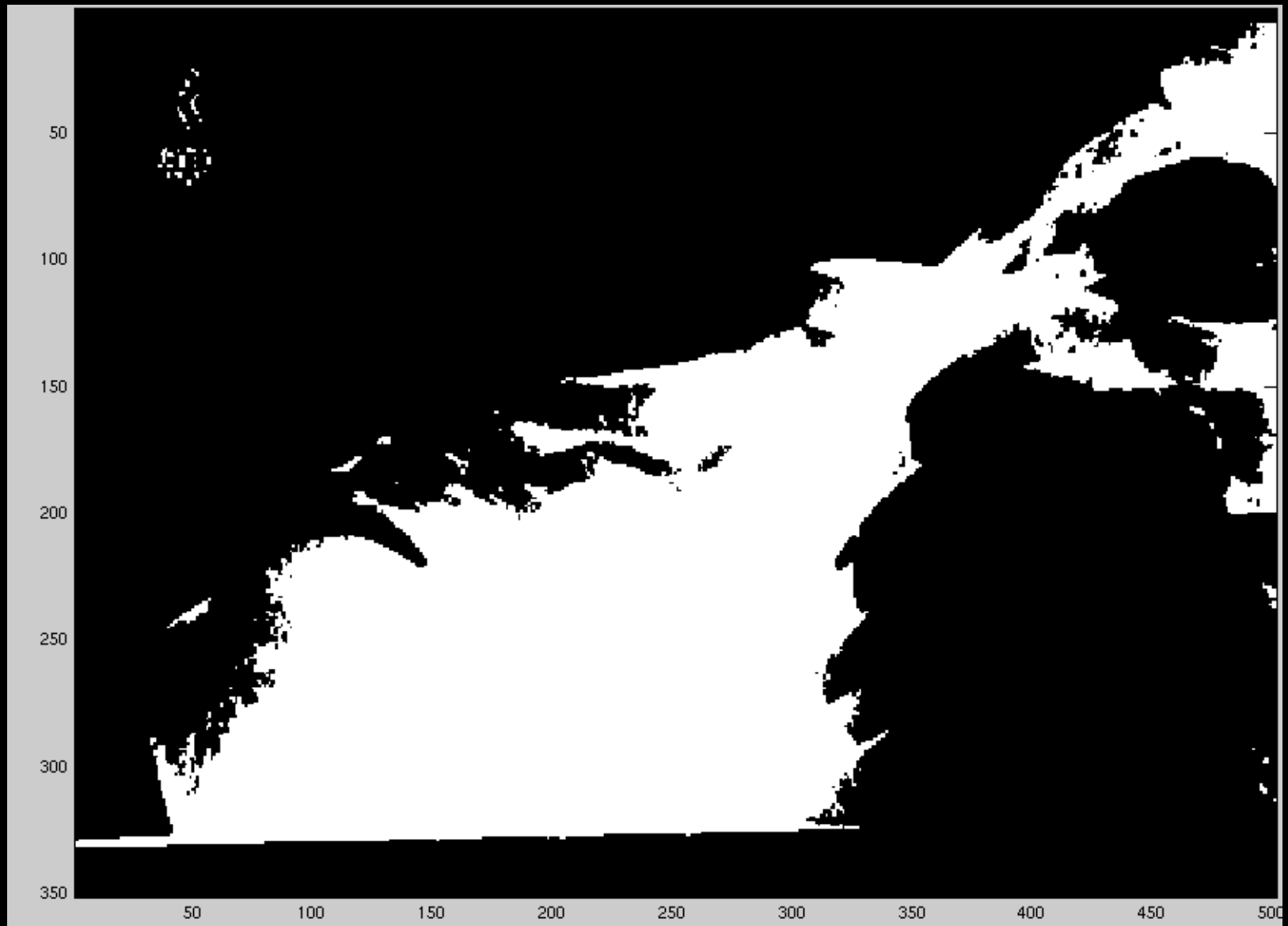
Digital X-rays: 8 is enough?



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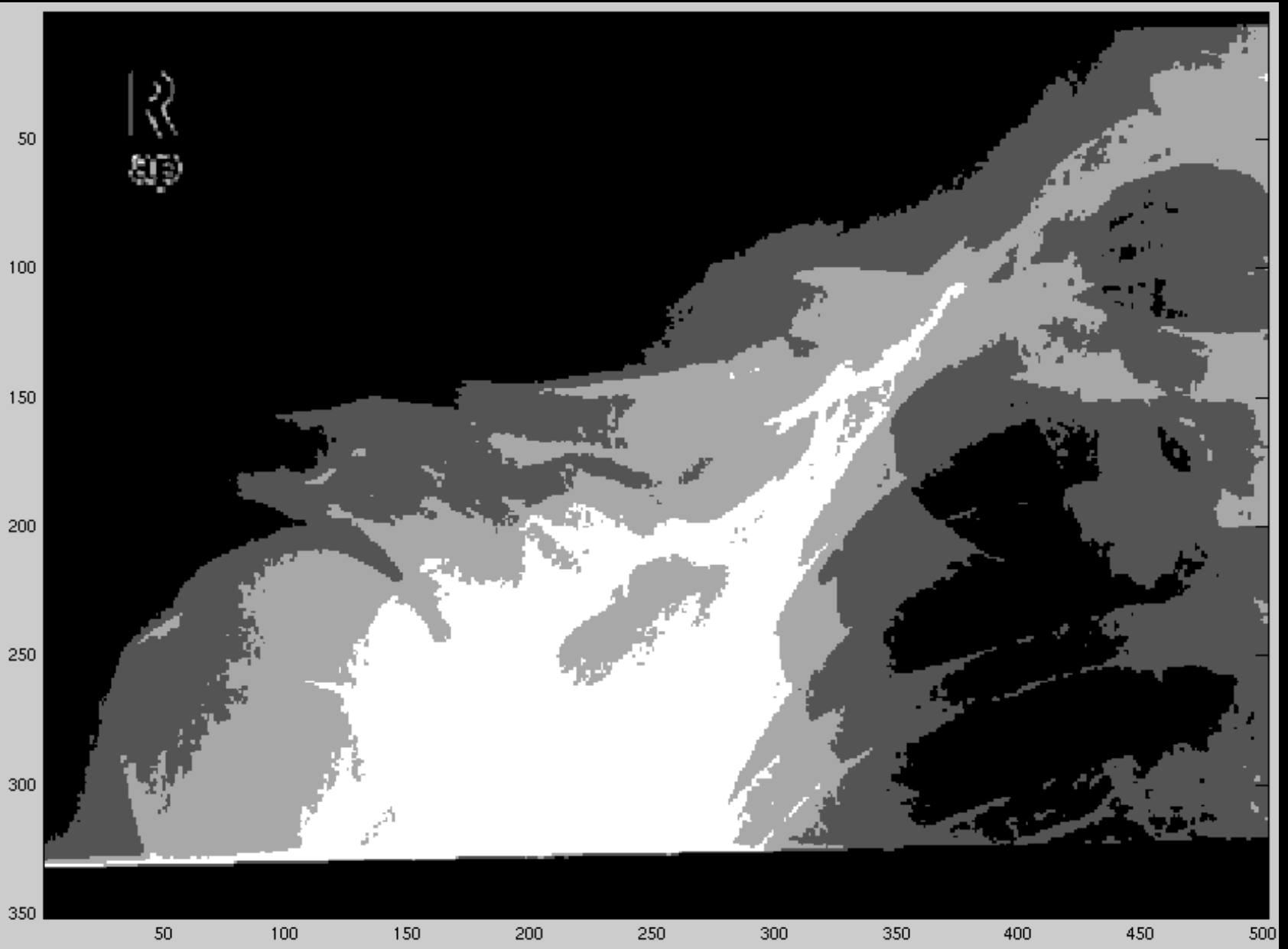
Digital X-rays: 1 bit



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Digital X-rays: 2 bits



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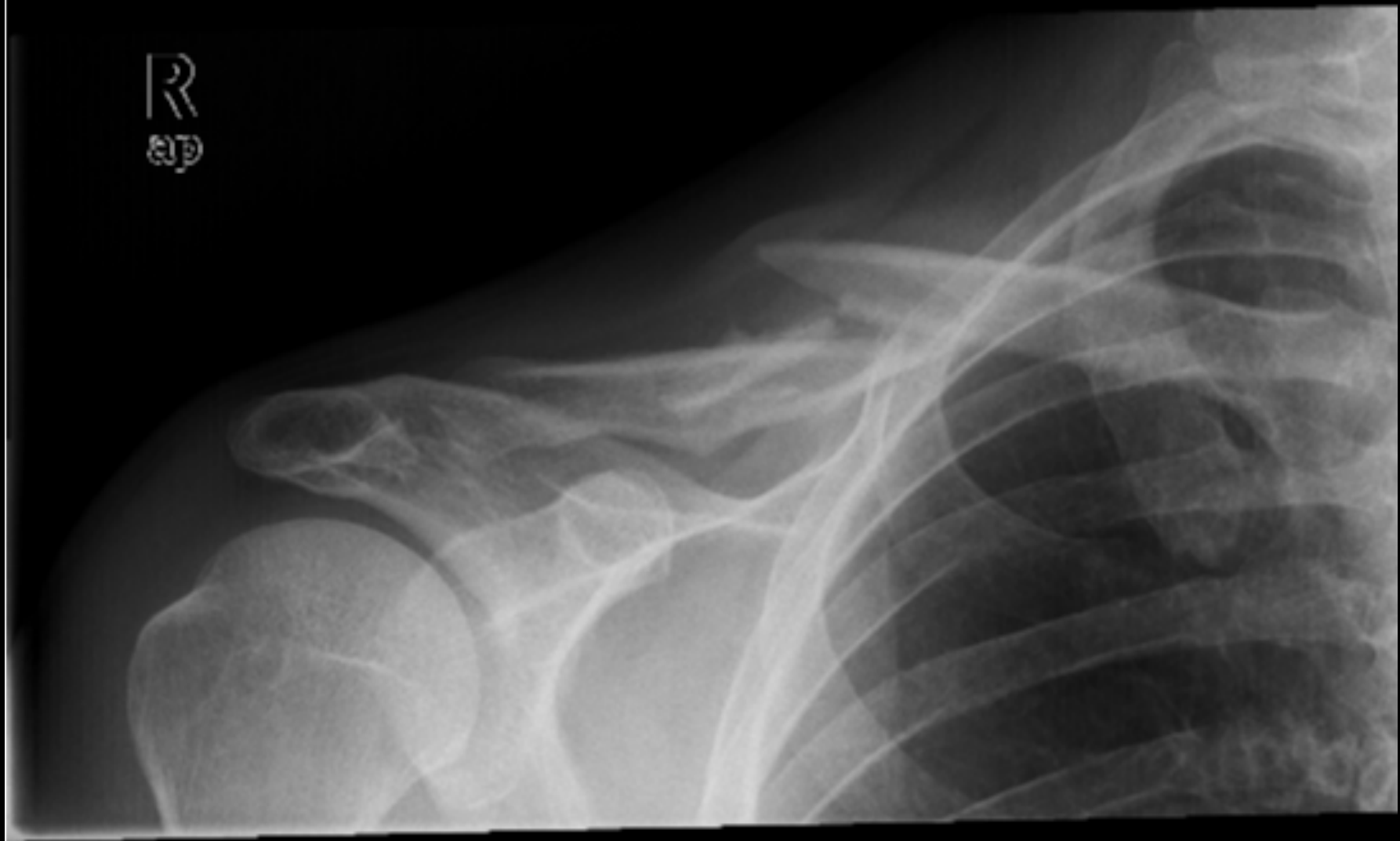
Digital X-rays: 3 bit



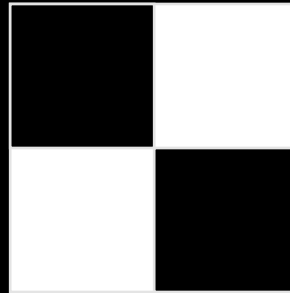
Introduction to

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Digital X-rays: 8 is enough?



- More gray levels can be simulated with more resolution.
- A “gray” pixel:

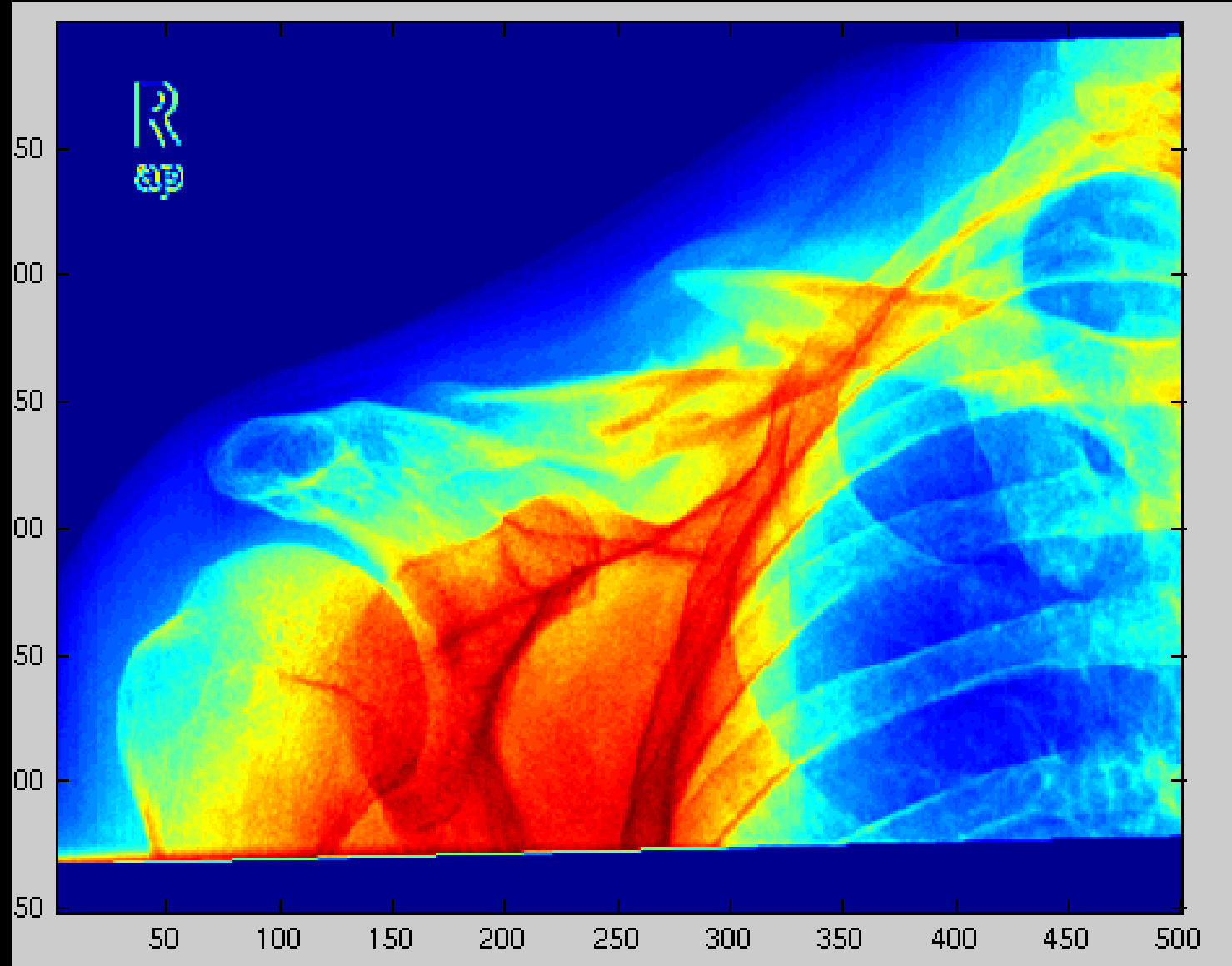


- Doubling the resolution in each direction adds at least four new gray levels. But maybe more?

Introduction to

Computer Vision

Pseudocolor



Introduction to

Computer Vision

Digital X-rays: 8 is enough?

R
axial

